

Additional material for Figures 3, 4 and 5

Figure 3:

MASTER: normal

FOLLOWER: normal

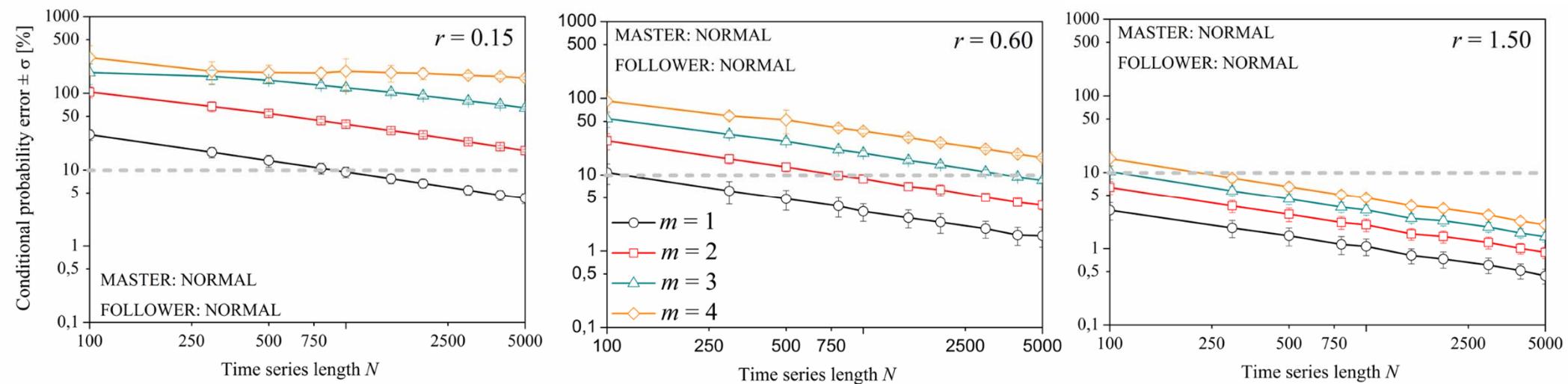


Figure 3: Conditional probability error [%] for a usual threshold value $r = 0.15$ (left panel), higher threshold $r=0.60$ (middle panel) and unusually high threshold $r=1.50$ (right panel) ; gray dashed horizontal line marks 10% error; results are presented in a log-log plane as mean $\pm \sigma$ (standard deviation).

Figure 3:

MASTER: normal

FOLLOWER: uniform

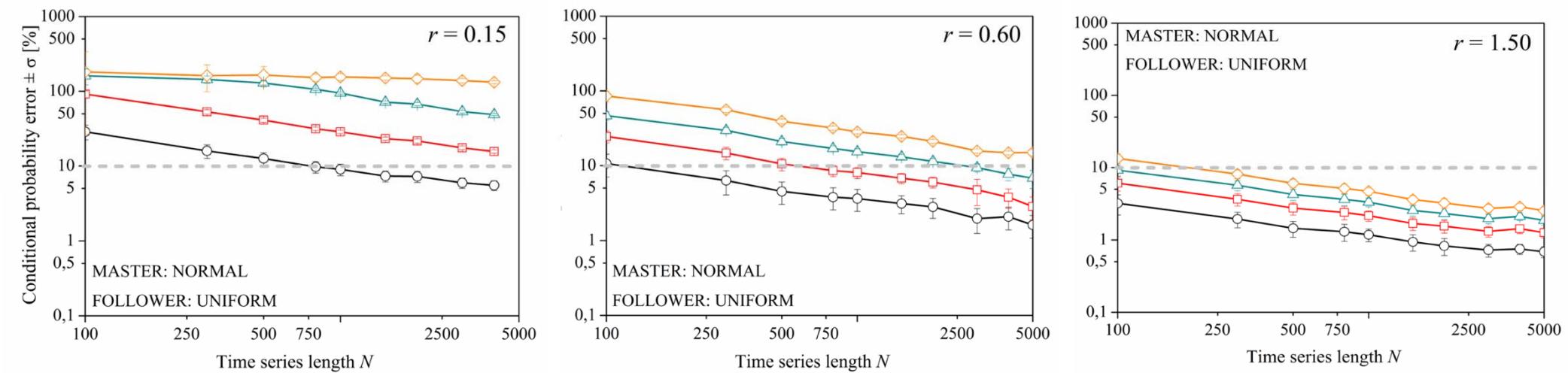


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Figure 3:
 MASTER: uniform
 FOLLOWER: normal

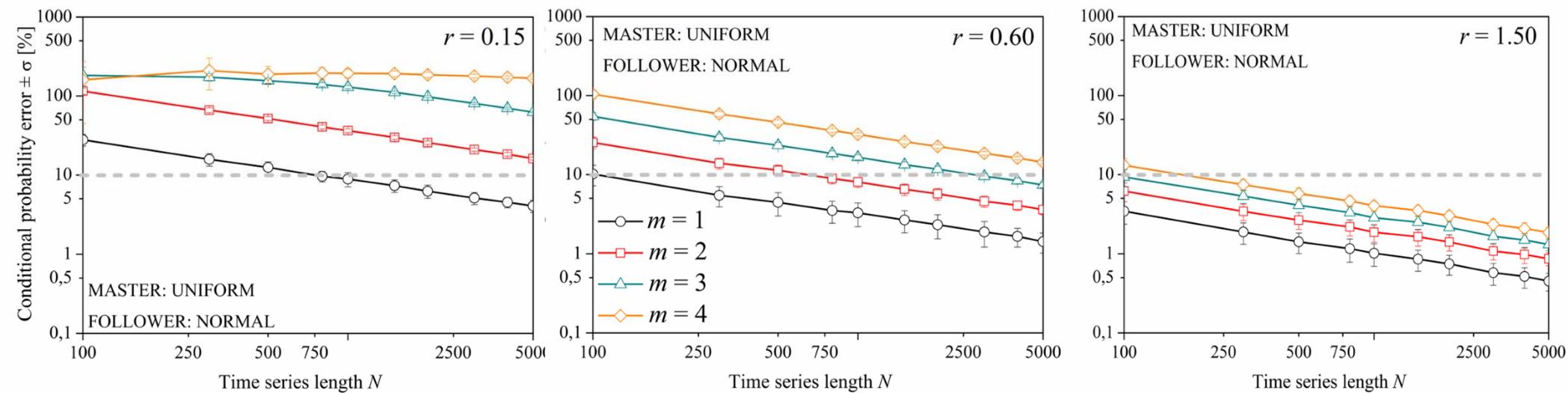


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Figure 3:
 MASTER: uniform
 FOLLOWER: uniform

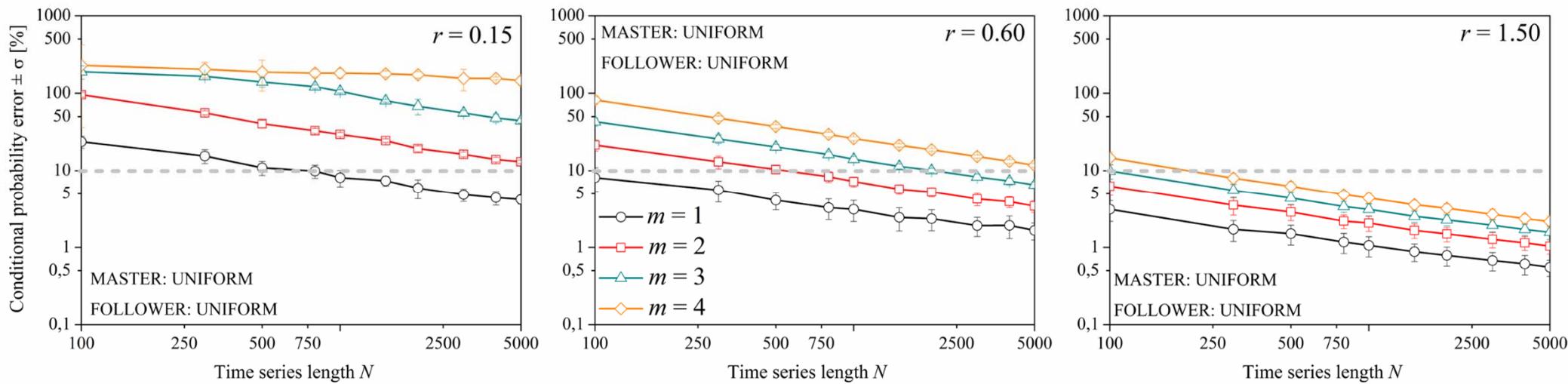


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X and Y normally distributed

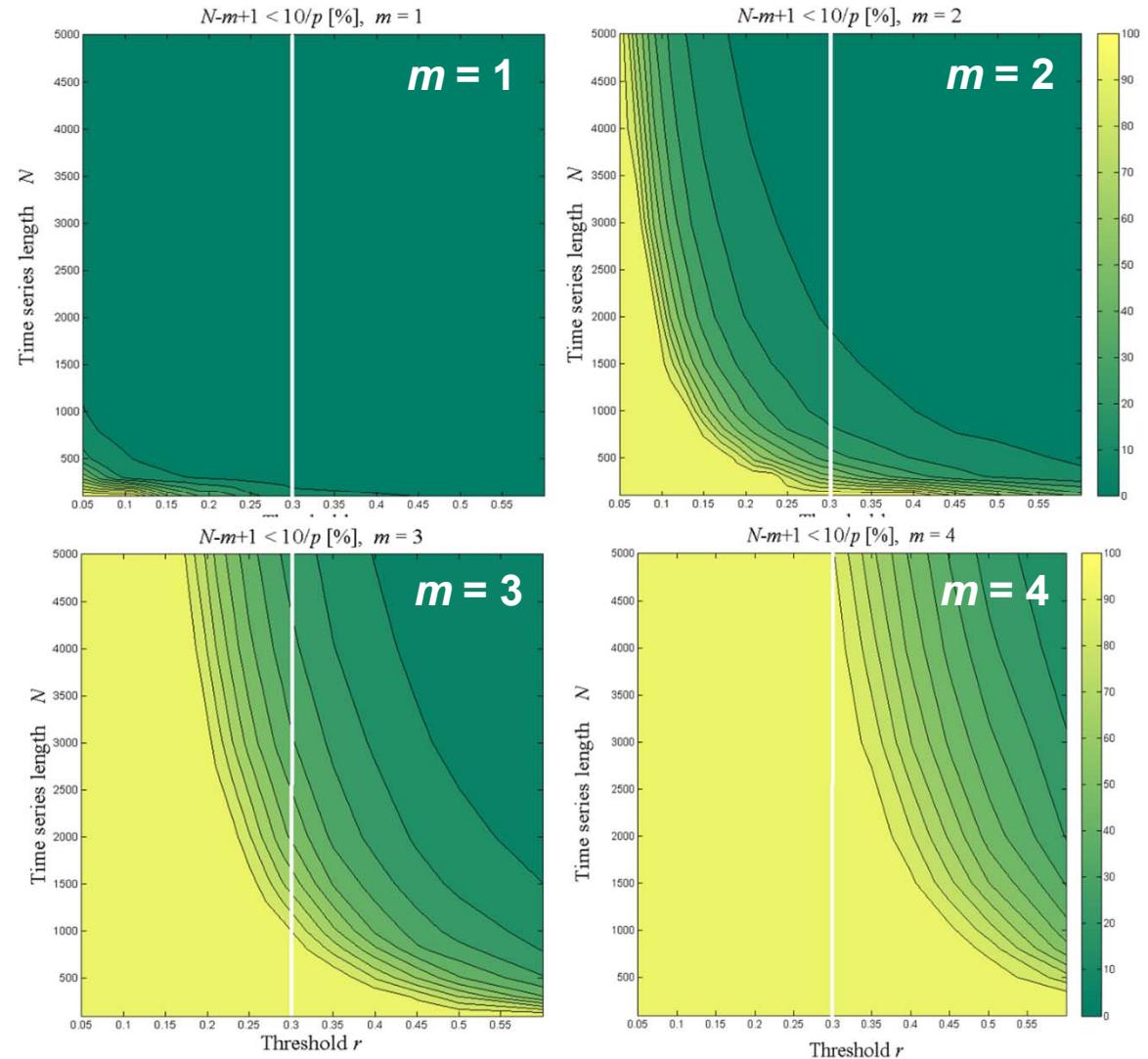


Figure 4: Percentage of probability estimates that fail to satisfy the criterion $N-m+1 \geq 10/\text{probability} [\%]$, presented in threshold-length (r - N) plane.

X axis: threshold r
Y axis: series length N

Panels correspond to $m = 1, 2, 3, 4$

Failures are presented by color changes from green (0% failures) to yellow (100% failures);

White vertical line cuts each plane at threshold value $r = 0.3$.

Figure 4: Percentage of probability estimates that fail to satisfy the criterion $N-m+1 \geq 10/\text{probability} [\%]$. presented in threshold-length ($r-N$) plane.

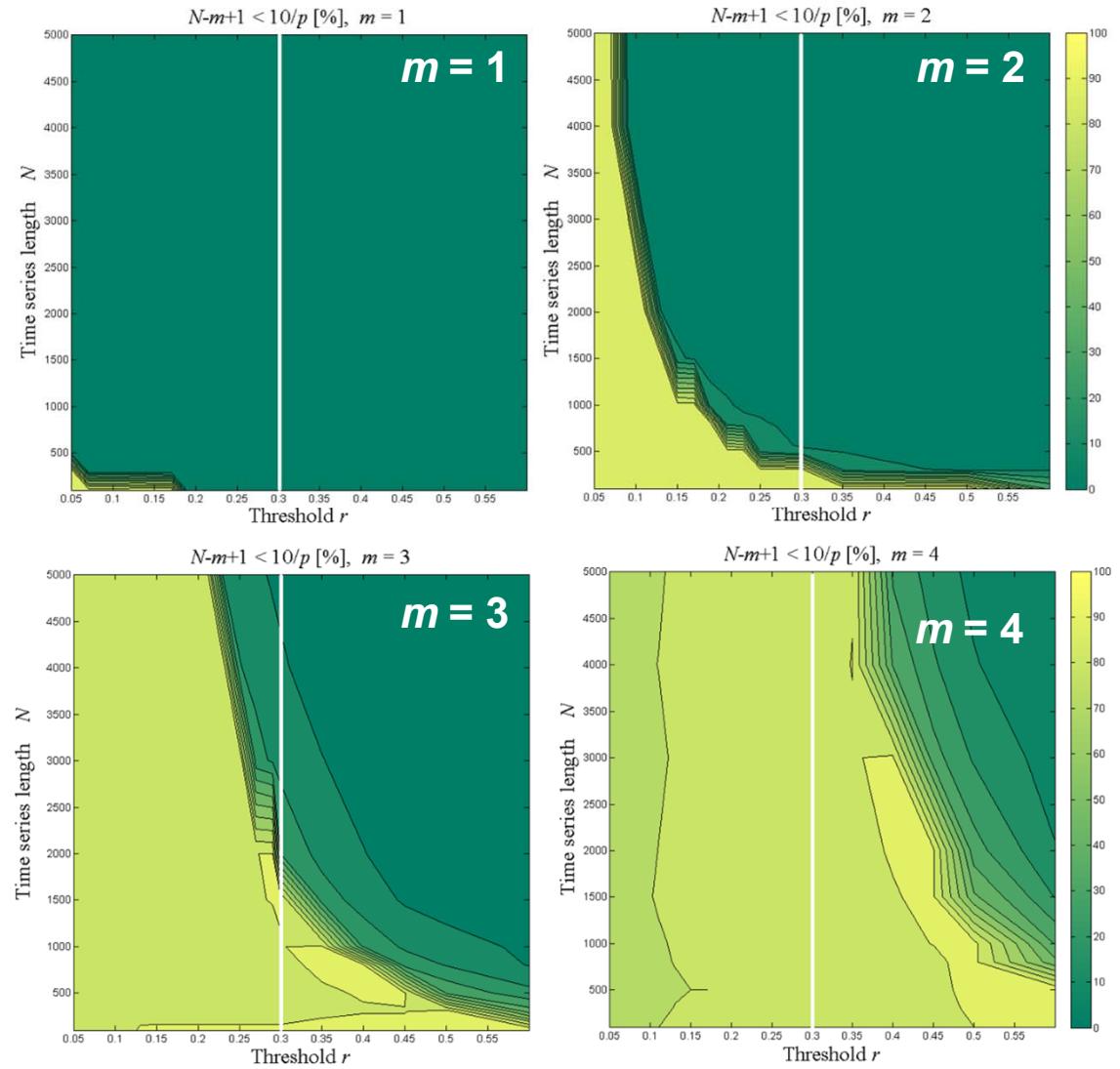
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X normally distributed, Y uniformly distributed



X uniformly distributed, Y normally distributed

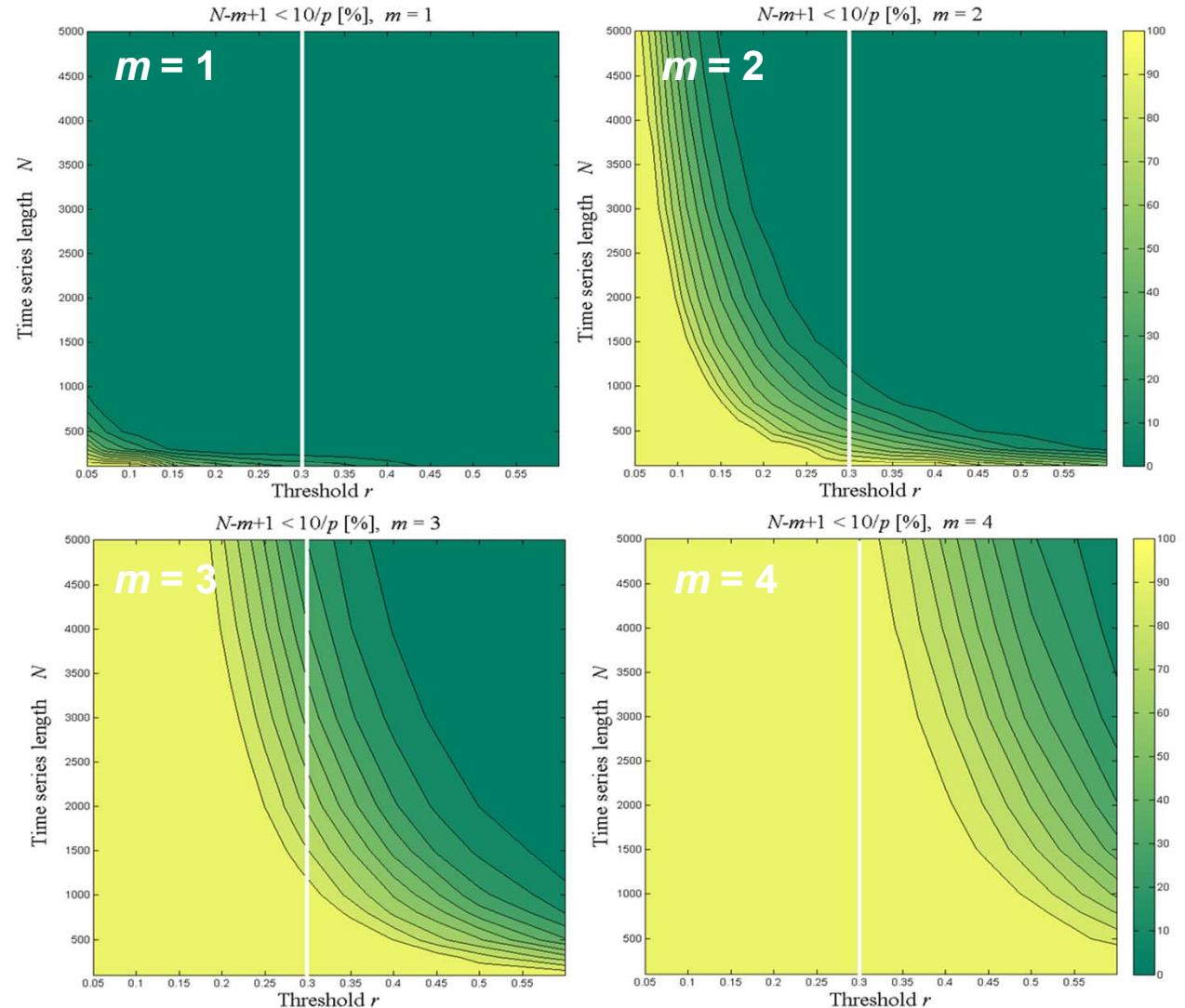
Figure 4: Percentage of probability estimates that fail to satisfy the criterion $N-m+1 \geq 10/p$ [probability [%]]. presented in threshold-length ($r-N$) plane.

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Y axis: series length N

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X and Y uniformly distributed

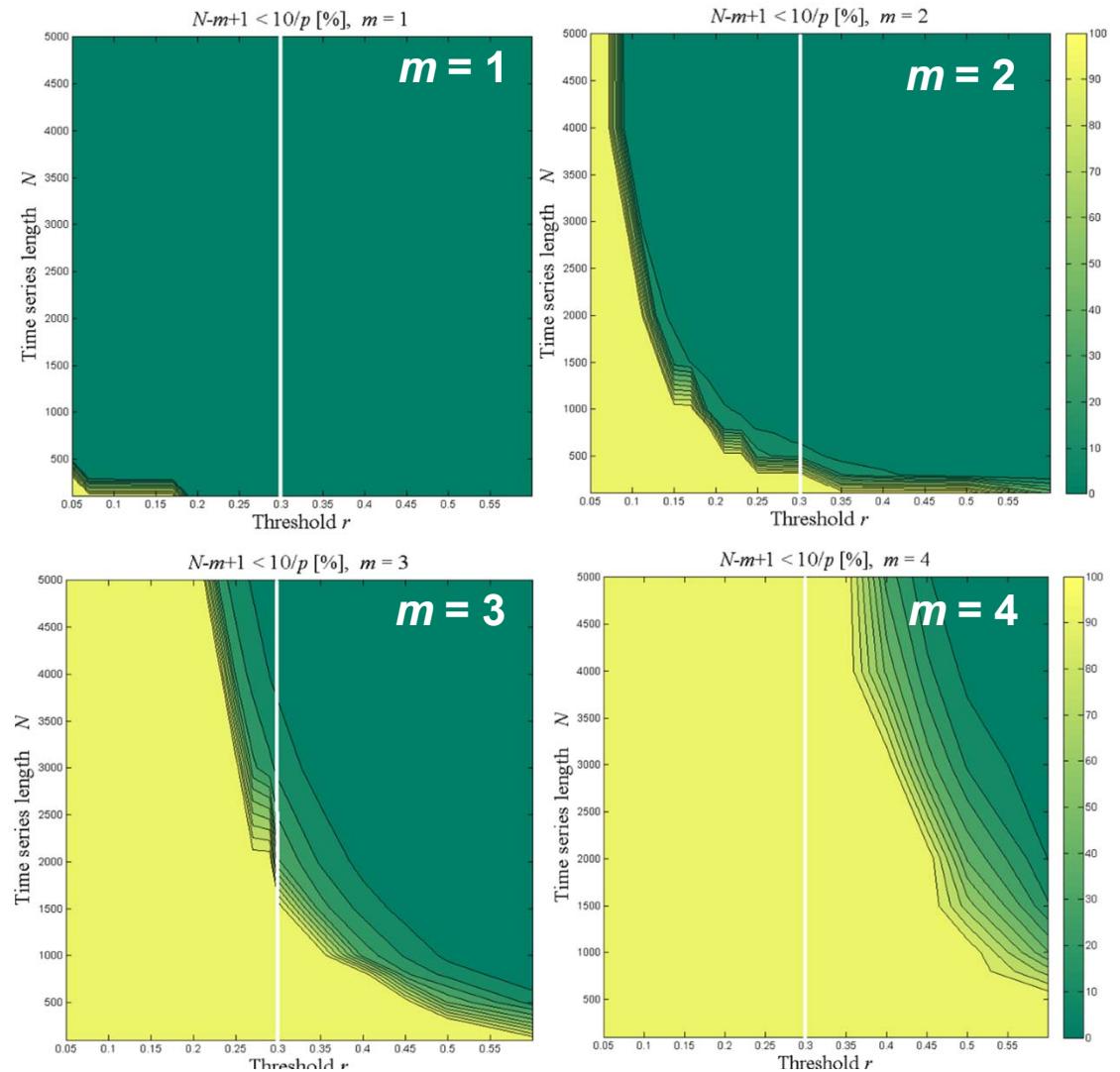


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X and Y normally distributed

Figure 5: Number of estimates for which probability = 0 in threshold-length (r - N) plane [%].

X axis: threshold r

Y axis: series length N

Panels correspond to $m = 1, 2, 3, 4$

Number of zero estimates is presented by color changes from green (0% zero estimates) to yellow (100% zero estimates);

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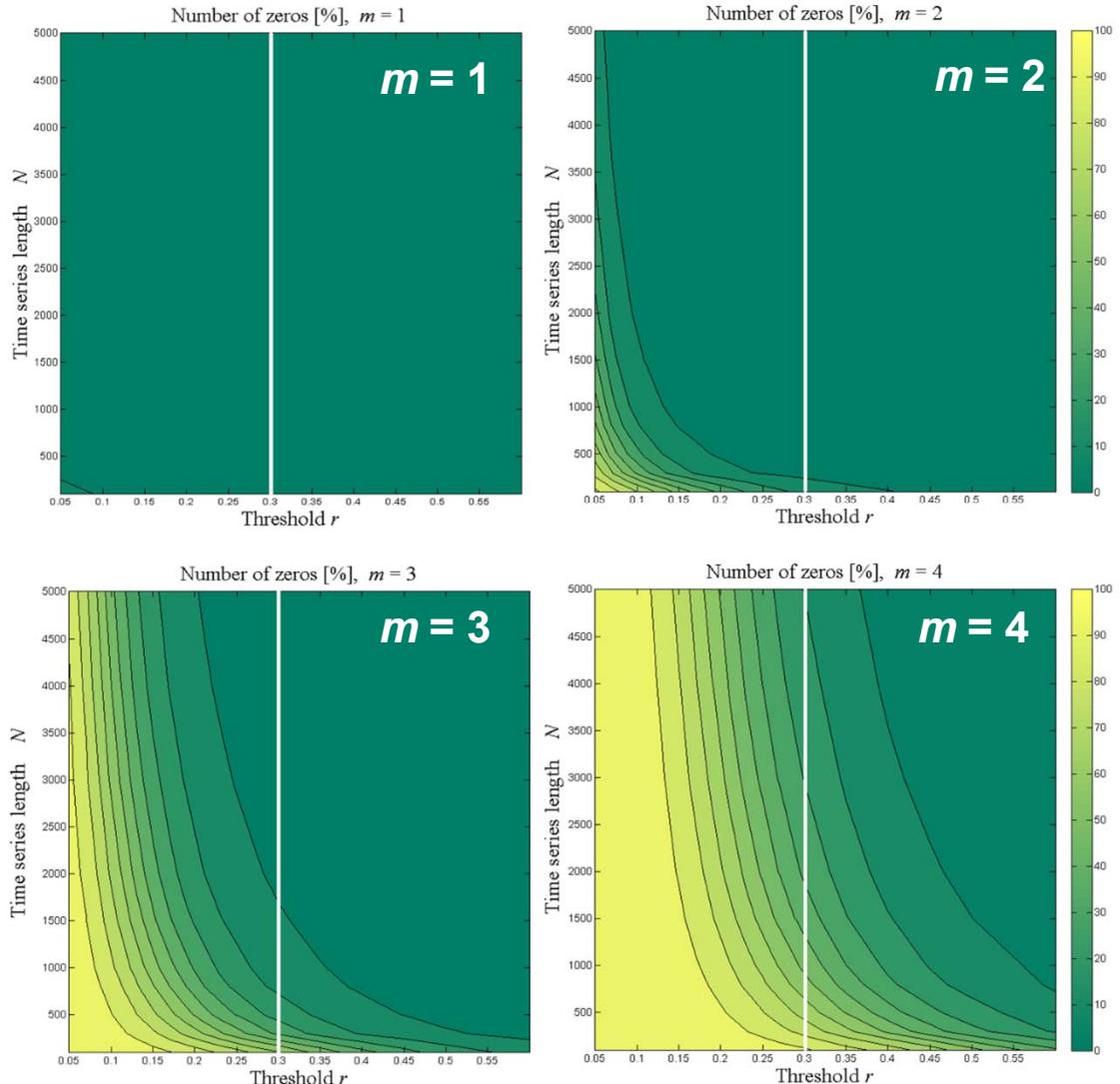


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X normally distributed, Y uniformly distributed

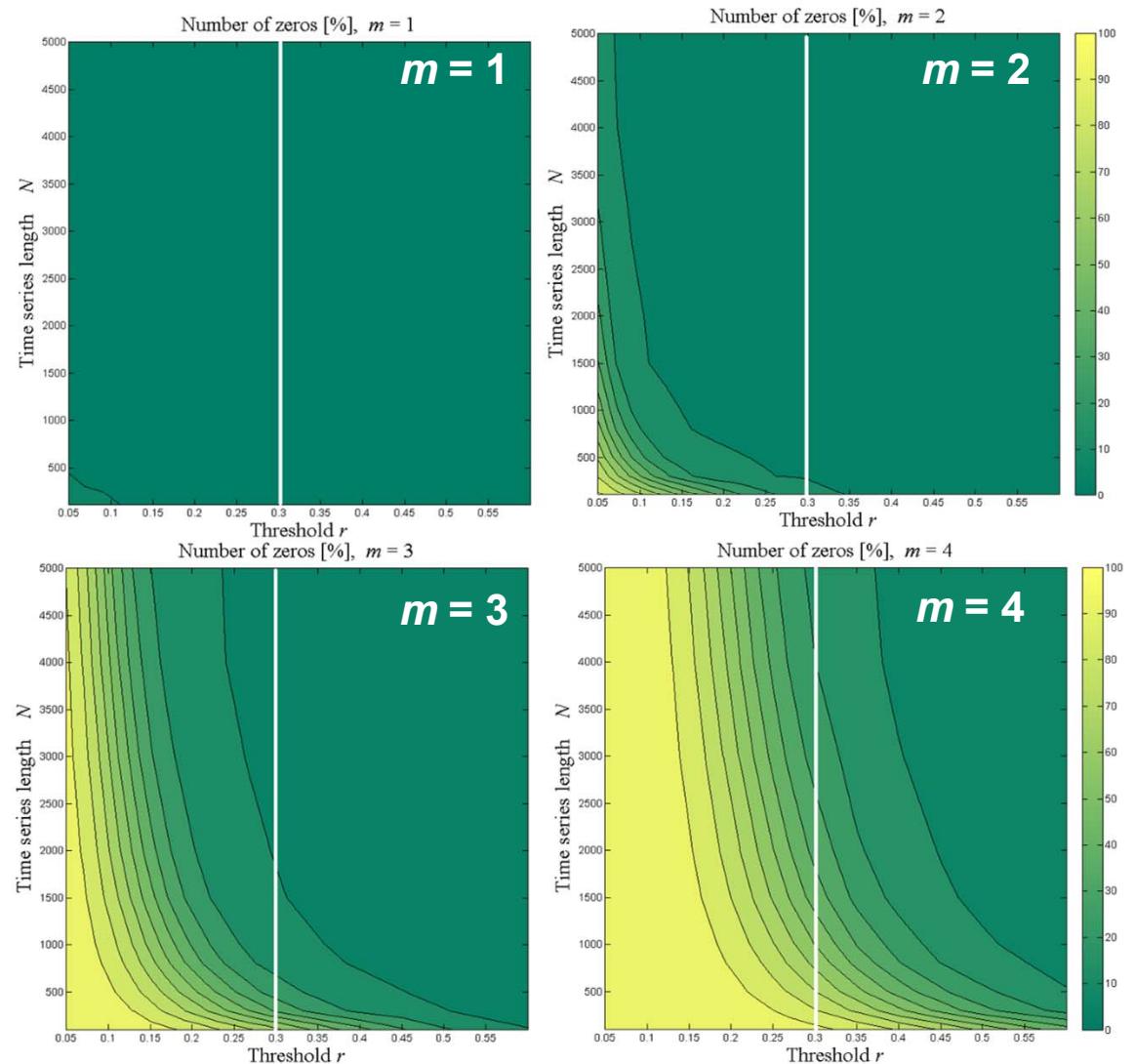


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X uniformly distributed, Y normally distributed

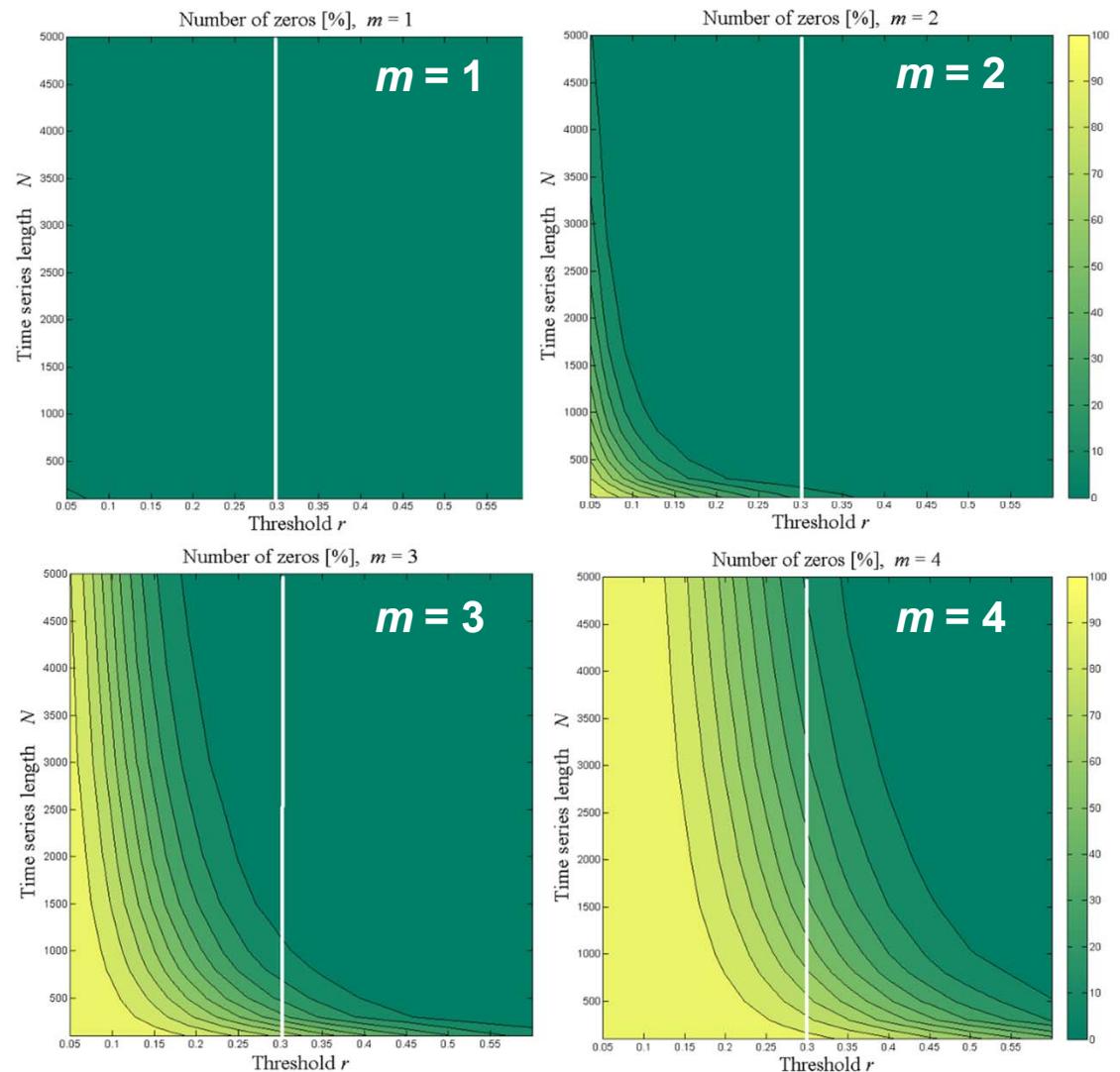


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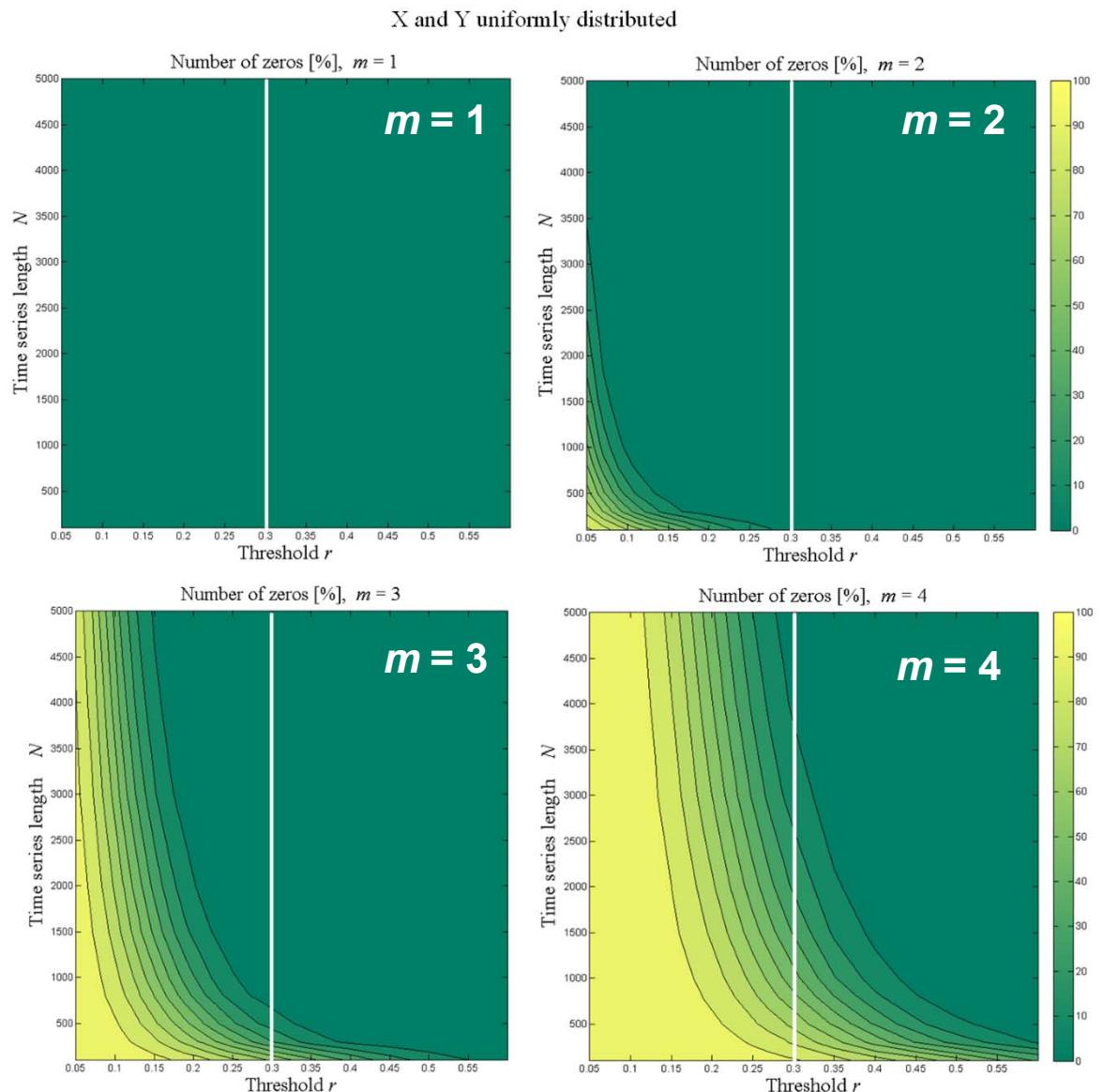
X axis: threshold r

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Procedure for $XApEn$ estimation

- A BRIEF EXPLANATION -

● STEP 1: Pre-processing

Each one of time series in study should comprise the same number of data points N ($N <$ length of the shortest recorded signal).

As for any analysis, all data series have to be examined in order to remove the artifacts.

Slow trend (occurring in moving patients and in freely moving laboratory animals) should be removed. We use a filter targeted for cardiovascular signals [25].

[25] M.P. Tarvainen, P.O. Ranta-aho, P.A. Karjalainen, "An advanced detrending approach with application to HRV analysis," *IEEE Trans. Biomed. Eng.*, vol. 42, no. 2, pp. 172–174, Feb., 2002.

After the detrending, the time series have to be wide sense stationary. It can be checked by software or, as some researchers prefer, it can be checked visually.

● STEP 2: Standard scoring

Estimate mean and standard deviation of each time series (already of length N and without the trend and artifacts). For the i^{th} time series \mathbf{X}_i , with mean m_i and standard deviation σ_i , get the series with mean 0 and standard deviation 1 as follows:

$\mathbf{X}_{si} = (\mathbf{X}_i - m_i) / \sigma_i$, meaning that from each sample its mean m_i should be subtracted, and the result divided by σ_i .

● STEP 3: Threshold calculation for maximal ApEn:

Chose which signal would be master (e.g. \mathbf{X} = SBP), and which signal would be its follower (e.g. \mathbf{Y} = PI). Form a differential time series of master signal, $x_D(i) = x(i+1) - x(i)$, $i = 1, \dots, N-1$. Find a standard deviation σ_{DX} of differential time series \mathbf{X}_D . Chose a vector length m (2 or 3). Calculate theoretical threshold $r_{\text{TH-A}}$ of **master** time series \mathbf{X} using equations (19).

$$r_{\text{TH-A}}(m) = \frac{e(m) + f(m) \cdot \sqrt{\sigma_{DX}/\sigma}}{\sqrt[4]{N/1000}}, \quad \sigma = 1, \quad (e, f) = \begin{cases} (-0.01, 0.05), & m = 1 \\ (-0.02, 0.23), & m = 2 \\ (-0.06, 0.43), & m = 3 \\ (-0.11, 0.65), & m = 4 \end{cases}$$

- **STEP 4: Threshold calculation for maximal XApEn:**

Form a differential time series of follower signal, $y_D(i) = y(i+1) - y(i)$, $i = 1, \dots, N-1$. Find a standard deviation σ_{DY} of differential time series \mathbf{Y}_D . Calculate theoretical threshold r_{TH-X} of master time series \mathbf{X} using equations (18).

$$r_{TH-X}(m) = r_{TH-A}(m) + \left| a(m) + \frac{b(m) + c(m) \cdot \sqrt{(\sigma_{DX} + \sigma_{DY})/2}}{\sqrt[4]{N/1000}} \right|, \quad (a, b, c) = \begin{cases} (0, -0.015, 0.03), & m=1 \\ (-0.02, 0, 0.023), & m=2 \\ (0, -0.006, 0.043), & m=3 \\ (0, -0.11, 0.13), & m=4 \end{cases}$$

- **STEP 5: Thresholds calculation for reliable XApEn estimation:**

Calculate threshold r_{XW} that would be used as a parameter for XApEn estimation using Equation (20) that ensures a fulfillment of weak reliability criteria (prefered).

$$r_{XW}(m) = 0.2 \cdot (m+1) + r_{TH-X}(m), \quad m \leq 4, N \leq 500,$$

$$r_{XW}(m) = 0.17 \cdot (m+1) + r_{TH-X}(m), \quad m \leq 4, 500 < N \leq 2000,$$

$$r_{XW}(m) = 0.15 \cdot (m+1) + r_{TH-X}(m), \quad m \leq 4, N > 2000$$

If signals are very long, strong reliability criteria might be used. Than the threshold should be calculated using Equation (21):

$$r_{XS}(m) = (m+1 + 10^5/N^2) \cdot (r_{TH-X}(m) + (5-m)/10), \quad m \leq 4.$$

- **STEP 5: XApEn estimation:**

Estimate XApEn using N and m as chosen parameters, and threshold r_{XW} (or r_{XS} if applicable) as calculated parameter.