Research Article

Parallel Machine Production and Transportation Operations’ Scheduling with Tight Time Windows

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This study addresses a parallel machine production and transportation operations’ scheduling problem with a tight time window associated with the transfer and delivery process. The orders located at the parallel machines need to be delivered to customers by train. Each order must be processed within a limited completion time in order for the product to be matched with the optimal trip to its destination within the delivery period. A mathematical analysis method is used to reveal the impact of tight time windows on the scheduling of production and transportation operations. The order transfer redundancy time and order transfer waiting time are employed to reflect the impact scheduling of production on the transfer process. The order delivery redundancy time and order delivery waiting time are used to describe delivery operations. The goal is to maximize the coordination level of order transfer and delivery, which are reflected in the order transfer time and the order delivery time, respectively. Additionally, a simulated annealing algorithm using the column generation technique was developed to solve this problem. The results show that the use of the system coordination model in this method obviously improves the number of successful transfers and deliveries.

1. Introduction

Made-to-order or time-sensitive goods are a hot topic that has been addressed by many researchers (Shu et al. [1] and Federgruen et al. [2]), and completed orders are usually required to be delivered to customers within tight time windows. It is believed that benefits are anticipated for integrating production scheduling with transportation operations [3–5]. The sharing of manufacturing resources means that raw materials and semifinished products located at different suppliers and customers are transferred widely and frequently [6, 7].

The scheduling of parallel batch production adding transportation operations should integrate tight time windows associated with rail transport plans to ensure that time-sensitive orders are met. The integrated scheduling problem features several special characteristics. Compared with a normal distribution system design problem, the time-critical aspect means that the longest lead-time from a production line to any accessible trip’s destination is subject to time-deadline restrictions that limit the order completion time. Furthermore, the orders should be transferred onto the selected trips within tight time windows imposed by the rail transport plan (Goossens et al. [8] and Fu et al. [9]). The challenges of rail time windows for time-sensitive products can be inferred according to Kang et al. [10] and Wu et al. [11]. Meanwhile, a trip can ship multiple orders to multiple destinations along the same railway line, which enriches the diversity of production schedules and trip selection (Diaz-Madronero et al. [12] and Cao et al. [13]).

With the development of off-site production businesses, it is increasingly urgent to coordinate the activities of both production and transportation operations to facilitate the dispatch and receipt of goods. The contributions of this paper are summarized as follows. First, a mathematical formula is developed to describe the relationships between
the order transfer redundancy time (OTR), order transfer waiting time (OTW), order delivery redundancy time (ODR), and order delivery waiting time (ODW). The comprehensive formula can be used to improve the connecting relationship between the production line and trains. Meanwhile, the formula is also used to distinguish between the last feasible connecting train and the nonlast ones and to judge whether the feasible connecting trains will be missed. Moreover, a parallel machine production and distribution model is proposed to optimize transport and delivery considering tight time windows. The complexity of the problem is based primarily on the use of a large set of discrete variables. A simulated annealing algorithm combined with a column generation approach (SACG) is designed to address the numerical testing network model. The results of the numerical example show that the quantitative performances of the delivery timeliness improved by the connecting quality (OT) are much better than those from the view of the delivery time window (OD).

In the remainder of this study, we first address some synergistic indexes first to measure the effect of tight time windows on production and transportation operations in Sections 3.1 and 3.2. A mathematical method is employed to reveal the relationships between OTR and OTW, and a similar scenario analysis approach is also applied to ODR and ODW for transportation operations. Section 3.3 develops a coordination scheduling model of parallel machine production and transportation operations to maximize the coordination level of order transfer and delivery, which reflects OT and OD. A simulated annealing algorithm using the column generation technique was developed, and we conduct a case study in Section 4. Finally, we conclude this study in Section 5 with discussions on possible extensions.

2. Literature Review

Research on the integration of scheduling models of production and distribution, which is known as integrated production-distribution planning or scheduling, has been relatively recent and includes studies such as Pandoor and Chen [5], Pornsing et al. [14], Zhong and Jiang [15], Russel et al. [16], Kishimoto et al. [17], and Ma et al. [18]. Many made-to-order or time-sensitive products are often needed to be delivered to their customers in time-critical modes in which tasks must be executed within a tight time frame. Most extant studies consider only the determination of location decisions or production scheduling through the application of mixed-integer programming (MIP) models (Chen [3]). Their objective functions are to minimize the total operating cost, service time, or budget input [19–27]. These models are subjected to production capacity, fleet size, job processing, or batching constraints, e.g., Cheng et al. [28], Devapriya et al. [29], and Noroozi et al. [30]. For example, Hajighaeri-Keshtei et al. [21] formulated a mathematical model to study the production and transportation system and capacity and the cost of rail transportation, which were the focus of their article. Jiang et al. [31] applied a scenario analysis method to establish performance measures to minimize the total waiting time. One of the tasks of this paper is to handle tight time windows and limit the deadline-dependent lead time within a given time window. The time deadlines in the transfer and delivery process that are imposed to guarantee on-time delivery have an impact on parallel batch scheduling and transfer trip selection. In particular, parallel batch scheduling complicates the model construction and solution.

Parallel batch scheduling problems under the influence of rail timetables are the focus of our research. In previous studies related to production and distribution system design problems, trucks and planes were used to serve customers as an important transport mode, and mathematical models were proposed to optimize the production and road and air transportation coordination problem (Chang and Lee [20], Chen and Vairaktarakis [4], Zhong and Jiang [15], Moons et al. [32], Wang and Cheng [33], Xuan [34], Zhong et al. [35], Seyedhosseini and Ghoreyshi [36], Gong et al. [37], Zandieh and Molla-Alizadeh-Zavaredehi [38], and Delavar et al. [39]). For instance, an integrated production and distribution scheduling problem was considered by Devapriya et al. [29], and in this research, the trucks’ routes and fleet size are the important decisions to be made. Azadian et al. [40] researched the order contract producing problem from a manager’s perspective and proposed an integrated scheduling model on the coordination of production and transportation planning. It is not difficult to see that this class of problems employed a vehicle routing problem to satisfy its delivery shipments. The coordination between production and rail transportation in an operational time dimension is one of the less focused-upon aspects and is our major task and focus. The mode of railway transportation is quite different from that of air transportation in transport plans and rolling stock (Pemberton [41]; Ho and Leung [38]). The distribution system design integrates the knowledge of path selection, and the time window caused by the rail timetable makes our focus more novel and interesting. To the best of our knowledge, few studies have investigated these topics in the context of railway timetables.

In conclusion, our method not only takes relevant accessibility into account but also takes delivery timelessness as a time window constraint into account. Of course, this approach is common in other articles. However, more importantly, not only delivery timeliness (customer service levels at the individual order level) is guaranteed by the tight delivery time window but a comprehensive formula is also introduced to measure delivery timeliness or customer service levels at the individual order level. The comprehensive formula can be used to distinguish between the last feasible connecting train and the nonlast ones and to judge whether the feasible connecting trains will be missed. Meanwhile, the formula is employed to improve the connecting relationship between the production line and trains. This formula is summarized in the scenario analysis introduced in our research.
3. Integrated Scheduling Coordination Model

3.1. Order Transfer Redundant Time and Order Transfer Waiting Time. The OTR describes whether the transfer relationship can be established successfully. If OTR is equal to or greater than 0, it means that the transfer can be carried out, as shown in scenarios (a) and (b) in Figure 1. However, the order may miss all the feasible trips to its destination when OTR is less than 0, as shown in scenario (c) in Figure 1.

The OTW is the waiting time for order \( i \) when it transfers from the production line \( l \) to its selected connecting trip \( l' \). As shown in Figure 1, the OTW is forced to be \( M \) when order \( i \) misses all the feasible trips, where \( M \) represents an infinite value.

The OTR and OTW can be calculated by the following equation:

\[
\begin{align*}
\tau^D_{i,l} &= \tau_A^{i,l} - \tau_{i,l}' - (1 - \gamma_{i,l}) \cdot M, \\
\tau^w_{i,l} &= \max\left\{\tau^{\text{beg}}_{i,l} - \tau_A^{i,l} + \tau_{i,l}' + (1 - \gamma_{i,l}) \cdot M, 0\right\} + M \cdot \max\left\{\gamma_{i,l} \cdot \tau_{i,l}' - \tau_{i,l}^{\text{end}} - (1 - \gamma_{i,l}) \cdot M, 0\right\}.
\end{align*}
\]

Furthermore, some interconnections between OTR and OTW can be found in Figure 1. Based on the three different relationships between the order completion time and feasible trip departure time, OTW is introduced in equation (2). In each scenario, two timelines are included: production and transportation. To facilitate modeling, \( \theta \) is a fixed value that represents the penalty value for missing feasible connecting trips.

\[
\begin{align*}
\tau^h_{i,l} &= \begin{cases} 
\tau_{i,l}' - \tau_{i,l}' - \tau^A_{i,l} - \tau_{i,l}' - \tau_{i,l}' - (1 - \gamma_{i,l}) \cdot M, & \text{when } \gamma_{i,l} \cdot \tau_{i,l}' - \tau_{i,l}^{\text{end}} - (1 - \gamma_{i,l}) \cdot M, 0 \\
\tau^{\text{beg}}_{i,l} - \tau_{i,l}' + \tau_{i,l}' + \tau_{i,l}' & \text{when } \gamma_{i,l} \cdot \tau_{i,l}' - \tau_{i,l}^{\text{end}} - (1 - \gamma_{i,l}) \cdot M, 0 \\
\tau_{i,l}' - \tau_{i,l}' & \text{when } \gamma_{i,l} \cdot \tau_{i,l}' - \tau_{i,l}^{\text{end}} - (1 - \gamma_{i,l}) \cdot M, 0 \\
\end{cases}
\end{align*}
\]

3.2. Order Delivery Redundant Time and Order Delivery Waiting Time. The ODR is a measure of delivery success. If the ODR is greater than 0, the delivery is successful, as shown in scenarios (a) and (b) of Figure 2. However, the order may violate the tight time window when the ODR is less than 0, as shown in scenario (c) of Figure 2.

The ODW is the waiting time for order \( i \) before the delivery is allowed by the tight time window. As shown in Figure 2, the ODW is forced to be \( M \) when order \( i \) violates the tight time window, where \( M \) represents an infinite value.

The ODR and ODW are formulated in the following equation:

\[
\begin{align*}
\text{Max } T &= \sum_{s \in S} \sum_{l \in L} \sum_{i \in I} \sum_{j \in J} r_{i,j} + \sum_{s \in S} \sum_{l \in L} \sum_{i \in I} \sum_{j \in J} t_{i,j}.
\end{align*}
\]

(1) For any production line \( l \), if \( i \) and \( j \) are processed continuously, then the order completion time is formulated in (6); if \( i \) is the first order on \( l \), then see equation (7).

\[
\begin{align*}
t_{i,j}^A + \rho_i Q_i &= t_{i,j}^A, & \text{when } \sum_{j \in J} \sum_{i \neq j} r_{i,j} = 1, & \forall i \in L, \\
t_{i,j}^A &= \rho_i Q_i, & \text{when } \sum_{j \in J} \sum_{i \neq j} r_{i,j} = 0, & \forall i \in L.
\end{align*}
\]

(2) Constraints imposed by integer programming:

\[
\begin{align*}
\sum_{l} \sum_{j \neq i} r_{i,j} &= 1, \\
\rho_i &= \{0, 1\}, & \forall i \in I, l \in L = 1, \\
y_{i,l} &= \{0, 1\}, & \forall i \in I, l' \in L'.
\end{align*}
\]

(3) The total number of processing steps should not exceed the capacity of each production line.
Figure 1: Three different relationships between the order completion time and feasible trip departure time.

Figure 2: Three different relationships between the order arrival time and the tight time window.
Simulated annealing (SA) has been proven by many researchers to be an effective method for solving combinatorial optimization problems. Its efficiency and effectiveness in solving a variety of real-world issues, e.g., SA combined with local search for solving vehicle routing problems with time windows (Lin et al. [45]), flow path and location problems (Hamzeei et al. [46]), timetabling problems (Daduna and Vo [47]), network design optimization (Friesz et al. [48]), and distribution center problems (Wei and Zhou. [49]), have been proven. Meanwhile, Ahin and Türkçay [50] presented that the approximate Pareto optimal sets we have found include almost all the previously obtained results and many more approximate Pareto optimal solutions. The results indicated that SA can determine the best solution most times. Therefore, we have a reason to believe that our proposed algorithm is effective and can be applied to solve our problem.

Column generation (CG) is an effective method to solve large-scale linear programming problems, especially for large-scale models. The CG technique has been widely used to solve a variety of real-world issues, e.g., crew scheduling (Soumis [51]), production scheduling (Chen and Powell [52]), vehicle routing (Skitt and Levary [53]), air transport (Liang et al. [54]), and issues in the medical and health-related industries (Wang et al. [55]). The detailed branch and price flow chart is shown in Figure 3. In our problem, CG is employed to obtain the parallel batch scheduling solution. The framework of the developed SACG in our research is shown in Figure 4.

The encoding style of solutions in Figure 5 is a matrix representation. As shown, rows indicate the production line set, and the columns indicate the order set. We used blank cells to fill in some rows since the number of orders in each production line may not be equal. Each order cell must be covered in a certain production line, and the number of cells is equal to the total number of orders.

After generating an initial solution, replacing moves are performed to search the alternative set. When a dropping move is called, it tries to select the trip. However, due to the condition of the production schedule, it may fail to find a transfer trip or deliver successfully, which may cause the infeasibility of transfer or delivery. The cooling function defines the temperature $T_i$ for each step of the algorithm $i$. It has a strong impact on the success of the SA algorithm. In the proposed algorithm, the linear strategy for updating the temperature is selected.

$$T_i = \text{Initial Temperature} - (i \times \text{Cooling Rate}),$$

where $T_i$ represents the temperature at iteration $i$ and Cooling_Rate and Initial_Temperature are the specified constant value and the initial temperature, respectively.

Last, in the proposed algorithm, the number of iterations and the number of reduced temperatures with no improvement are used as stopping criteria.

4.2. Numerical Test. Figure 6 is an example network including multiple production lines, six railway stations, ten orders, and eight railway trips. The starting point of all trips is considered as the location of the production facility. The timetable of all trips is shown in Table 1. The second column indicates the departure time of each trip. Nonzero elements in columns 3 to 8 of Table 1 characterize the path of each trip, and each element indicates the arrival time of the trip at the corresponding station. If the path of a trip covers the destination of an order and the order completion time is before the trip departs, it is a feasible solution that the order selects the trip.

4.2.1. Network Solution. We test the model and SACG algorithm on a personal computer with Intel Core i5, 2.60 GHz CPU, and 4 GB RAM. We set the initial temperature to 500, the descent rate to 0.95, and the terminal condition to 0.1. Let $\theta = 100, \alpha = 10, \mu = 10$, and $\delta = 100$. The cost of the parallel production line is defined as 0 at first, and it will be deeply discussed in the subsequent analysis. The SACG can solve the model in a very short time, and the detailed results are shown in Table 2. The OTW, $t_{\text{tw}}$, is the key indicator to measure the production success connection. It shows that 100% of orders achieve successful transfer in the sample network. Meanwhile, ODW is used to judge whether the delivery is successful. From Table 2, we can see that orders 1 and 6 fail to deliver. We obtain the same performance as the experiment in Jiang et al. [31], and the number of successful deliveries is 8. The success rate of order transfer is much better than that in Jiang et al. [31].

4.2.2. Algorithm Performance. The iteration trace of SACG is shown in Figure 7. It can be seen that the genetic algorithm finds the optimal solution in a very short time. The iteration becomes stable after 10 iterations, and the optimal solution with the objective function is $-99.5$. The detailed results are presented in the first row of Table 3. Compared with the solution given in [31], the optimized solution we found decreases the total cost by nearly 50%.

We adopt a genetic algorithm to solve the numerical network again and compare the performance with SA. The results of all algorithms are similar, and the correctness of the algorithm is verified (Table 3).
Two major algorithm parameters related to iteration times are tested here, and the results are shown in Table 4. Different combinations of $T_0$ and $q$ are used to solve the problem. The results show that when we set a larger initial temperature ($T_0$) and a larger descent rate ($q$), the optimal result can be improved to a certain extent. When $T_0 = 0$ or $q = 0$, the SACG algorithm cannot work.

4.2.3. Comparison of Different Goals. To verify the proposed model (Max OT + OD), we compare the other two objectives, i.e., Max OT and Max OD. The experiment is completed under the same conditions and with the same data. Table 5 lists the details of the results.

There are ten successful transfers and seven successful deliveries when maximizing OT. Meanwhile, maximizing OD can obtain eight successful transfers and eight successful
deliveries. Compared with Max OT and Max OD, Max (OT + OD) achieves an obvious improvement in the objective function.

4.2.4. Analysis of Related Parameters. In this section, we test the influence of relevant parameters on the scheduling model. First, we set the parallel production line cost as $-\infty$ and the capacity of each parallel production line as $\infty$. The result shows that only one production line is needed. The function value is $-209$, the number of successful transfers is 9, and the number of successful deliveries is 8. We obtained the same optimal solutions as in [31]. Second, we keep other conditions unchanged and test the sensitivity of capacity values when the parallel production line cost is 0. The details are shown in Table 6, and the trend draws the conclusion that the number of successful transfers is 10, and the number of successful deliveries is 8. We can seek some explanation

\begin{table}[h]
\centering
\caption{Timetable of the sample network.}
\begin{tabular}{|c|c|c|c|c|c|c|c|}
\hline
Train line & Departure time & 1 & 2 & 3 & 4 & 5 & 6 \\
\hline
1 & 1 & 3.5 & — & — & 5 & — & 7.5 & — \\
2 & 1.5 & — & 4.5 & — & — & — & — \\
3 & 2 & 3 & — & 4.5 & — & — & 6 \\
4 & 2.5 & 4.5 & — & 5.5 & — & 8 & — \\
5 & 3 & 5 & — & — & 6.5 & — & — \\
6 & 3.5 & 4.5 & — & 6.5 & — & 7.5 & — \\
7 & 4 & — & 5.5 & — & — & — & — \\
8 & 4.5 & 5.5 & — & — & 7 & — & — \\
\hline
\end{tabular}
\end{table}
Table 2: Solution for the sample network.

<table>
<thead>
<tr>
<th>Processing time/quality</th>
<th>0.1/1</th>
<th>0.3/1</th>
<th>0.4/2</th>
<th>0.1/3</th>
<th>0.1/5</th>
<th>0.4/1</th>
<th>0.2/1</th>
<th>0.2/1</th>
<th>0.2/4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Delivery time window</td>
<td>[1, 7]</td>
<td>[1, 10]</td>
<td>[1, 9]</td>
<td>[1, 8]</td>
<td>[1, 5]</td>
<td>[1, 6]</td>
<td>[1, 6]</td>
<td>[1, 8]</td>
<td>[1, 4]</td>
</tr>
<tr>
<td>Production scheduling and train allocated</td>
<td>6 10 9 7 3 1 4 2 8 5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>√</td>
<td>√</td>
<td></td>
<td></td>
<td></td>
<td>√</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
<td>√</td>
<td></td>
<td></td>
<td></td>
<td>√</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
<td></td>
<td></td>
<td>√</td>
<td></td>
<td></td>
<td></td>
<td>√</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>√</td>
<td></td>
<td></td>
<td></td>
<td>√</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td></td>
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<td>7</td>
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<tr>
<td>8</td>
<td></td>
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<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Same results for operation scheduling using different algorithms.

<table>
<thead>
<tr>
<th>Method</th>
<th>Successful connections</th>
<th>Successful deliveries</th>
<th>Objective function</th>
<th>OT ($t_{\text{ot}}^{\text{all}}$)</th>
<th>OD ($t_{\text{od}}^{\text{all}}$)</th>
<th>Parallel production lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>SA</td>
<td>10</td>
<td>8</td>
<td>-99.5</td>
<td>20.5</td>
<td>-120</td>
<td>3</td>
</tr>
<tr>
<td>GA</td>
<td>10</td>
<td>8</td>
<td>-99.5</td>
<td>20.5</td>
<td>-120</td>
<td>3</td>
</tr>
</tbody>
</table>

Table 4: Different objective values corresponding to varying SA parameters.

<table>
<thead>
<tr>
<th>$T_0$</th>
<th>0</th>
<th>0.75</th>
<th>0.8</th>
<th>0.85</th>
<th>0.9</th>
<th>0.95</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>100</td>
<td>0</td>
<td>-102</td>
<td>-102.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
</tr>
<tr>
<td>200</td>
<td>0</td>
<td>-101.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
</tr>
<tr>
<td>500</td>
<td>0</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
</tr>
</tbody>
</table>

Table 5: Results of different objectives.

<table>
<thead>
<tr>
<th>Objective</th>
<th>Successful transfers</th>
<th>Successful deliveries</th>
<th>Objective function</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max OT</td>
<td>10</td>
<td>7</td>
<td>-210</td>
</tr>
<tr>
<td>Max OD</td>
<td>8</td>
<td>8</td>
<td>-104.5</td>
</tr>
<tr>
<td>Max (OT + OD)</td>
<td>10</td>
<td>8</td>
<td>-99.5</td>
</tr>
</tbody>
</table>
from equation (3). Taking order 1 as an example, regardless of whether the order selects any trip, the earliest arrival time at its destination is 4.5. The earliest arrival time including the transit time is larger than its delivery time window upper bound. Therefore, variations in the capacity only change the number of parallel production lines and have no effect on delivery success. However, as the capacity gradually increases, the number of parallel production lines will stabilize at a certain value.

In addition, we also tested the effect of the cost change on the function value, and the function value also changes when the cost increases gradually. However, almost the same conclusion is always reached: in the sample system, the number of successful transfers is 10, and the number of successful deliveries is 8. The detailed results are shown in Table 7.

### 5. Conclusions

Many studies focus on production allocation, but few pay attention to the coordination and scheduling of orders and transportation in a time-critical mode. This paper focuses on the parallel batch scheduling of production and transportation with respect to synergy in the time dimension. We adopt a scenario analysis method to reveal some internal mechanisms in the transfer and delivery process. Several interconnections between OTR and OTW in the transfer process are found, and OT is introduced based on these findings. Similarly, ODR and ODW in the delivery process are commonly expressed by OD. A column-generation-based simulated annealing algorithm is proposed to solve the problem. Compared with Max OT and Max OD, Max (OT + OD) achieves an obvious improvement in the objective function. Meanwhile, the results of our research are compared with those of similar studies, and the model and algorithm are proven to be workable.

Our research can be further expanded. In practice, due to some unexpected situations, train schedules may change, so it would be worth studying how to formulate strategies to eliminate any negative effects of such changes.

### Table 6: Variation with respect to the production line capacity.

<table>
<thead>
<tr>
<th>Capacity</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>15</th>
<th>20</th>
<th>1000 (Inf)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parallel production lines</td>
<td>6</td>
<td>5</td>
<td>4</td>
<td>4</td>
<td>3</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>Objective function</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
<td>-99.5</td>
</tr>
<tr>
<td>Successful connections</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>Successful deliveries</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
</tr>
</tbody>
</table>

### Table 7: Changes in objective function values under different costs.

<table>
<thead>
<tr>
<th>Production line cost</th>
<th>0</th>
<th>-10</th>
<th>-20</th>
<th>-30</th>
<th>-40</th>
<th>-50</th>
<th>-60</th>
<th>-70</th>
<th>-80</th>
<th>-90</th>
<th>-100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Production line</td>
<td>3</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Objective function</td>
<td>-100</td>
<td>-122</td>
<td>-141</td>
<td>-161</td>
<td>-182</td>
<td>-203</td>
<td>-221</td>
<td>-242</td>
<td>-262</td>
<td>-281</td>
<td>-301</td>
</tr>
<tr>
<td>Successful connections</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>Successful deliveries</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
<td>8</td>
</tr>
</tbody>
</table>

### Notations

- \( i, i' \): The set of order \( i, i' \in L \); \( i \) and \( i' = 1, 2, \ldots, k \)
- \( Q_i \): The quantity of order \( i \)
- \( p_i \): The processing time of order \( i \)
- \( e_i \): The destination of order \( i \in l \)
- \( L \): The set of production lines, \( l \in L, L = [l|l = 1, 2, \ldots, n] \), where \( n \) is the total number of production lines
- \( L' \): The set of trips in the network, \( l' \in L' \), \( L' = [l'|l' = 1, 2, \ldots, m] \), where \( m \) is the total number of trip indexes
- \( S(l') \): The set of stations on trip \( l', s \in S(l') \), \( S(l') = [s|s=1,2,\ldots,p] \), where \( p \) is the total number of stations
- \( t_{\text{Tra}_{sll}} \): The order transfer operating time from \( l \) to \( l' \) at station \( s \)
- \( t_{\text{D}_{sll}} \): The departure time of the last feasible connecting trip at station \( s \)
- \( t_{D}_{sll} \): The departure time of the selected connecting trip at station \( s \); if the selected connecting trip is the last feasible trip, \( t_{D}_{sll} = t_{\text{D}_{sll}} \)
- \( t_{A}_{sll} \): The arrival time of trip \( l' \) at the destination of order \( i \)
- \([t_{{e}_{i}^{\begin{scriptsize}beg\end{scriptsize}}}, t_{{e}_{i}^{\begin{scriptsize}end\end{scriptsize}}}] \): The delivery time window of order \( i \)
- \( t_{\text{Tra}_{i}^{\begin{scriptsize}end\end{scriptsize}}} \): The order delivery operating time from trip \( l' \) to its destination
- \( \theta \): The penalty cost of missing a feasible connecting trip
- \( \alpha \): The delivery earliness penalty cost
- \( \delta \): The delivery tardiness penalty cost
- \( \mu \): The delivery timely contribution benefit
- \( \text{Cap}_{l'} \): The capacity of trip \( l' \)
- \( t_{A}_{sll} \): The completion time of order \( i \) on production line \( l \) at station \( s \)
- \( t_{D}_{sll} \): OTR, the time difference between \( t_{D}_{sll} \) and \( t_{A}_{sll} \)
- \( t_{T_{\text{W}_{sll}}} \): OTW, the waiting time for order \( i \) when it transfers from production line \( l \) to its selected connecting trip \( l' \)
- \( t_{T_{\text{W}_{sll}}} \): OT, the order transfer time
- \( t_{\text{Tra}_{i}^{\begin{scriptsize}end\end{scriptsize}}} \): ODR, the time difference between \( t_{{e}_{i}^{\begin{scriptsize}end\end{scriptsize}}} \) and \( t_{{e}_{i}^{\begin{scriptsize}A\end{scriptsize}}} \)
\( t_{w\because \cdot} \): ODW, the waiting time for order \( i \) until the delivery is allowed by \( t_c^{\text{beg}} \).

\( t_{d\cdot} \): OD, the order delivery time.

\( y_{ij}\cdot \): = 1 if order \( i \) selects trip \( t_j \); = 0, otherwise.

\( r_{ij}\cdot \): = 1 if the processing of order \( i \) is followed by order \( j \) on production line \( t_i \); = 0, otherwise.

**Data Availability**

The data used to support the findings of this study are included within the article.

**Conflicts of Interest**

The authors declare no conflicts of interest.

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**References**


