Research Article

Neural Network Backstepping Controller Design for Fractional-Order Nonlinear Systems

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In this work, a backstepping controller design for fractional-order strict feedback systems is investigated and the neural network control method is used. It is noted that in the standard backstepping design, the fractional derivative of the virtual quantity needs to be calculated repeatedly, which will lead to a sharp increase in the number of controller terms with the increase of the system dimension and finally make the control system difficult to bear. To handle the estimation error, certain robust terms in the controller at the last step are designed. The stability of the controlled system is proven strictly. In addition, the proposed controller has a simple form which can be easily implemented. Finally, in order to verify our theoretical method, the control simulation based on a fractional-order chaotic system is implemented.

1. Introduction

Backstepping design is a recursive design method. It is a systematic design method for systems with uncertain parameters first proposed by Kanellakopoulos et al. in 1991 [1]. Its main ideas of this control method are to obtain a feedback controller by recursively constructing Lyapunov function of closed-loop system, select proper control law by deriving the Lyapunov function along the trajectory of closed-loop system, ensure the boundedness of closed-loop system trajectory, and guarantee the convergence of the tracking error. The backstepping design method is suitable for both linear and nonlinear systems, so it has been widely used as soon as proposed. In addition, the backstepping method can be used together with many other control methods, such as sliding mode control [2, 3], adaptive fuzzy control (AFC) [4, 5], and intermittent control [6], and it is very effective in controlling the strict feedback systems. Backstepping control has some advantages, such as global stability, easy design, and implementation of the controller. However, it also has a big weakness named “explosion of terms,” which is caused by repeatedly deriving the virtual controller. In fact, it is difficult to solve this problem completely. Meanwhile, it is well known that system uncertainties exist in most real-world systems. Hence, it is meaningful but difficult to investigate the backstepping control of uncertain nonlinear systems avoiding explosion of terms.

On the contrary, fractional calculus has almost the same history as the integer one. However, due to the complexity of the theory and the lack of corresponding physical background, it has not been developed as it should be. In 1983, Mandelbrot pointed out that there are a large number of fractional dimension phenomena in nature, and thus, fractional calculus has rapidly become a research hotspot. Studies show that many physical systems exhibit fractional-order dynamic behavior due to their special material and chemical properties, which are called fractional-order systems. Using fractional-order models to describe objects with fractional-order characteristics can better reveal the essential characteristics and behavior of objects [7]. Fractional calculus is the extension of integer calculus, and integral calculus is a special case of fractional calculus, so it is more universal to study...
fractional-order systems [8–10]. Compared with the integer-order model, the fractional-order model has clearer physical meaning and more concise expression in describing complex physical and mechanical problems; fractional-order control expands the degree of freedom of control and can obtain better control performance; fractional-order calculus has memory performance which ensures the influence of historical information on the present and future, and is conducive to improving the quality of control [11–14]. In the field of integer-order systems, based on Lyapunov stability theory, the control of nonlinear systems has been widely studied and a series of results have been obtained. However, due to the late start of fractional-order control and the complexity of the theory, the fractional-order stability theory and controller design method are far less developed than the control of integer-order systems.

In the last several decades, the nonlinear system control based on universal function approximators (neural networks and fuzzy system) has received much attention [4, 14–18]. It is shown that universal function approximators show an excellent performance in approximating system uncertainties. Therefore, backstepping control based on universal function approximators is an interesting research idea. In this aspect, many prior works have been given. In [4], fuzzy backstepping controller was designed for fractional-order systems, where the fractional virtual inputs are approximated by fuzzy systems. In [19], optimal backstepping control implemented for fractional-order systems was investigated. In [20], fuzzy backstepping control of strict-feedback fractional-order uncertain nonlinear systems was studied, and some interesting results were given. In [5], by using optimal control, type-2 fuzzy control, and sliding mode control, backstepping control of fractional systems is addressed, and it is shown that the backstepping control can be well mixed with many other control strategies. In [21], fuzzy backstepping control of fractional-order systems is addressed, and the saturation phenomenon in fractional systems was also studied. In [22], to avoid the chattering phenomenon in the traditional backstepping control, a novel control method was developed. Some recent works can be referred to [23–28] and the references therein.

The key idea of this paper is to try to solve the problem of “term explosion” in the backstepping control of fractional-order systems. Backstepping control technique is employed in the controller design. It should be emphasized that no prior knowledge about the system uncertainties and the unknown part of the fractional-order system is needed, and the term explosion problem is also solved by using neural networks to approximate the system uncertainties.

2. Preliminaries

2.1. Problem Description. In this paper, we will consider the fractional-order nonlinear systems listed as

\[
\begin{align*}
D^q_\tau \xi_1(t) &= f_1(\xi_1(t)) + \xi_2(t), \\
D^q_\tau \xi_2(t) &= f_2(\xi_2(t)) + \xi_3(t), \\
& \vdots \\
D^q_\tau \xi_n(t) &= f_n(\xi_n(t)) + u(t), \\
y(t) &= \xi_1(t),
\end{align*}
\]

with \( \xi_i = [\xi_1, \ldots, \xi_i]^T \in \mathbb{R}^i \), \( i = 1, \ldots, n \) being the state, \( y(t) = \xi_1(t) \) being the output, \( f_i(\xi_i) \), \( i = 1, \ldots, n \) being unknown functions, and \( u(t) \) representing the input. Apparently, system (1) represents a large class of strict feedback fractional-order systems.

Our aim is to design a proper controller such that the system output \( y(t) \) tracks the desired trajectory \( \xi_d(t) \) with certain accuracy. Since \( f_i(\xi_i) \) is assumed to be unknown, it can be approximated by neural networks, which will be introduced later in this section. In addition, to meet our objective, we need the following assumptions.

**Assumption 1.** The referenced function \( \xi_d \) is smooth and is known in advance.

**Assumption 2.** The signal \( \xi \) is always known.

2.2. Neural Network Description. In this part, we will give a brief description of a multilayer network that will be used later. The structure of the used neural networks is depicted in Figure 1.

In real-world applications, a neural network is represented in the following form:

\[
y_k(s, w_k) = \sum_{j=1}^{h} w_{kj} \varphi_k \left( \sum_{i=1}^{n} v_{ji} s_i + \theta_j \right) = w_k^T \psi_k(s), \tag{2}
\]

where \( w_k = \begin{bmatrix} w_{k1} & \vdots & w_{kh} \end{bmatrix}, \psi_k = \begin{bmatrix} \varphi_k(\sum_{i=1}^{n} v_{1i} s_i + \theta_{1j}) \\ \vdots \\ \varphi_k(\sum_{i=1}^{n} v_{nh} s_i + \theta_{h}) \end{bmatrix}, n, h \), and \( m \) are the number of neurons in input layer, hidden layer, and output layer, respectively, \( y_k \) denotes the output, and \( v_{ji} \) is selected randomly on the interval \([−1, 1]\). According to [29–31], \( \varphi(\cdot) \) is chosen as

\[
\varphi(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}.
\]

Thus, we have

\[
y = W^T \psi(s),
\]

with \( W = \begin{bmatrix} w_1^T & w_2^T & \cdots & w_m^T \end{bmatrix} \) and \( \psi(s) = \begin{bmatrix} \psi_1(s) & \cdots & 0 \\ 0 & \psi_2(s) & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \psi_m(s) \end{bmatrix} \).
Generally, we can use the above neural network to estimate a nonlinear function as

\[ f(\zeta(t)) = W^*^T(t)\psi(\zeta(t)) + \epsilon(\zeta(t)), \]

(5)

with \( \epsilon(\zeta(t)) \) being the optimal approximation error vector. \( W^* \) is defined by

\[ W^* = \arg \min_{W} [\sup_t |f(\zeta(t)) - f(\zeta(t))|]. \]

(6)

To facilitate the controller design, we need the following assumption.

**Assumption 3.** We can find some \( \bar{z}_i \) so that \( \epsilon_i \leq z_i \), with \( i = 1, 2, \ldots, m \).

### 2.3. Fractional Calculus

In this paper, the Caputo fractional-order derivative will be used, which is expressed by

\[ C_0^\alpha D_\alpha f(t) = \frac{1}{\Gamma(1-\alpha)} \int_0^t (t-\tau)^{-\alpha} f'(\tau) d\tau, \]

(7)

with \( 0 < \alpha \leq 1 \) being the order and \( \Gamma(\cdot) \) representing Euler’s function. In the following, we will use \( D_\alpha^\alpha \) to replace \( C_0^\alpha D_\alpha^\alpha \) for convenience.

The following results about the fractional calculus will be used.

**Lemma 1** (see [8]). Suppose that \( z(t) = 0 \) is an equilibrium of

\[ D_\alpha^\alpha z(t) = f(z(t)). \]

(8)

One can find a Lyapunov function \( V(t, z(t)) \) and three class-\( k \) functions \( \theta_i(t) \), \( i = 1, 2, 3 \), such that

\[ \theta_1(\|z(t)\|) \leq V(t, z(t)) \leq \theta_2(\|z(t)\|), \]

\[ D_\alpha^\alpha V(t, z(t)) \leq -\theta_3(\|z(t)\|). \]

(9)

Then, \( z(t) = 0 \) is asymptotical stability.

**Lemma 2** (see [21]). Suppose that \( z(t) \in \mathbb{R}^n \) is a smooth function. The following inequality holds:

\[ \frac{1}{2}D_\alpha^\alpha z^T(t)z(t) \leq x^T(t)D_\alpha^\alpha z(t). \]

(10)

### 3. Main Results

In this part, the controller design together with the stability analysis will be given based on the backstepping design procedure. To meet the control aim, let

\[ \begin{align*}
  z_1(t) &= \zeta_1(t) - \zeta_d(t), \\
  z_i(t) &= \zeta_i(t) - \alpha_{i-1}(t), & i = 2, \ldots, n,
\end{align*} \]

(11)

with \( \alpha_i \) being a virtual input to be designed. The controller can be designed recursively because in the traditional backstepping design, virtual input \( \alpha_{i-1}(t) \) depends on \( \alpha_i(t) \) and its derivative. Thus, the whole design process can be divided into \( n \) steps.

**Step 1.** According to the first equation in (11), we can obtain

\[ D_\alpha^\alpha z_1(t) = f(\zeta_1(t)) - D_\alpha^\alpha z_d(t) + z_2(t) = y_1(\zeta_1(t)) + z_2(t), \]

(12)

where \( y_1(\zeta_1(t)) = f(\zeta_1(t)) - D_\alpha^\alpha \phi(\zeta_1(t)) \) representing an unknown function to be approximated. Then, \( y_1(\zeta_1(t)) \) can be approximated using neural network (5) as

\[ \tilde{y}_1(\zeta_1(t), W_1(t)) = W_1^* t \psi(\zeta_1(t)). \]

(13)

Denote

\[ W^* = \arg \min_{W_1(t)} \left[ \sup_t |y(\zeta_1(t)) - \tilde{y}(\zeta_1(t), W_1(t))| \right]. \]

(14)

It should be emphasized that \( W_1^* \) is a constant vector whose exact value is not needed in the controller design. Let

\[ \zeta_1(t) = W_1(t) - W_1^*, \]

(15)

\[ \varepsilon_1(\zeta_1(t)) = y(\zeta_1(t)) - \tilde{y}(\zeta_1(t), W_1^*), \]

(16)

where \( \tilde{y}(\zeta_1(t), W_1^*) = W_1^* \psi(\zeta_1(t)) \). Like that, in the literature [32–34], it is reasonable to assume that \( \zeta_1(t) \) is bounded, i.e., \( |\varepsilon_1(\zeta_1(t))| \leq \varepsilon_1 \) with \( \varepsilon_1 \) being an unknown constant. Thus, it is easy to obtain that

\[ \begin{align*}
  \tilde{y}(\zeta_1(t), W_1(t)) - \tilde{y}(\zeta_1(t)) & = \tilde{y}(\zeta_1(t), W_1(t)) - \tilde{y}(\zeta_1(t), W_1^*) + \tilde{y}(\zeta_1(t), W_1^*) - \tilde{y}(\zeta_1(t)).
\end{align*} \]

(17)

Using (16), (17) can be written as

\[ \begin{align*}
  \tilde{y}(\zeta_1(t), W_1(t)) - \tilde{y}(\zeta_1(t), W_1^*) - \varepsilon_1(\zeta_1(t)) & = W_1(t)^T \psi(\zeta_1(t)) - \varepsilon_1(\zeta_1(t)).
\end{align*} \]

(18)

Substituting (15) and (18) into (17), we have

\[ \begin{align*}
  \tilde{y}(\zeta_1(t), W_1(t)) - \tilde{y}(\zeta_1(t)) & = W_1(t)^T \psi(\zeta_1(t)) - \varepsilon_1(\zeta_1(t)).
\end{align*} \]

(19)

Thus, the virtual control \( \alpha_1(t) \) is given by
\[ a_i(t) = -W_i^T(t) \psi(\tilde{z}_i(t)) - k_i z_i(t), \quad (20) \]

with \( k_i > 0 \) being a constant.

\[ a_i(t) = -\tilde{y}_i(t) - z_{i-1}(t) - k_i z_i(t) = -W_i^T(t) \psi(\tilde{z}_i(t)) - z_{i-1}(t) - k_i z_i(t), \quad (21) \]

with \( \tilde{y}_i(t) \) being the estimation of

\[ \gamma_i(\tilde{z}_i(t)) = f_i(\tilde{z}_i(t)) - \sum_{j=1}^{\infty} \left( \frac{\partial a_{i-1}(t)}{\partial \tilde{z}_j(t)} \right) \psi(\tilde{z}_j(t)) \right) \right), \quad (22) \]

Step \( n \). At this last step, we can construct the following controller:

\[ u(t) = -W_n^T(t) \psi(\tilde{z}_n(t)) - z_{n-1}(t) - k_n z_n(t) + u_c(t), \quad (23) \]

with \( u_c \) being a supervisory input which is used to handle the approximation errors of neural networks. To meet the control aim, the robust control term is given by

\[ u_c(t) = - \sum_{j=1}^{n} k_{ij} |z_j(t)|, \quad (24) \]

with \( k_{ij} > 0, j = 1, 2, \ldots, n \) being proper design parameters satisfying certain conditions (see, the conditions in Theorem 1).

Step 2. \( i, 2 \leq i \leq n - 1 \). We can design

\[ V_i(t) = V_{i-1}(t) + \frac{1}{2} \sum_{j=2}^{i} \psi(\tilde{z}_j(t)) - \psi(\tilde{z}_i(t)) \]

In the controller design, neural networks’ parameters are adjusted as

\[ D_i^\alpha \tilde{W}_i(t) = \lambda_i z_i(t) \psi(\tilde{z}_i(t)), \quad (25) \]

with \( \lambda_i > 0 \) being a design parameter.

The following theorem is presented to show the controlled system’s stability.

**Theorem 1.** Consider system (1) satisfying Assumptions 1–3. If the virtual inputs are given by (20) and (21) and the final controller is given by (23) with a robust term (24), then the tracking error \( z_1 \) converges to origin asymptotically, and all signals remain bounded in the control process.

Consider a Lyapunov function as

\[ V_1 = \frac{1}{2} z_1^2(t) + \frac{1}{2\lambda_1} \tilde{W}_1^T(t) \tilde{W}_1(t). \quad (26) \]

Noting that \( \zeta_2(t) = z_2(t) + a_1(t) \), by using Lemma 2 and using (1), (11), and (20), we have

\[ D_i^\alpha V_i(t) \leq z_i(t) D_i^\alpha z_i(t) + \frac{1}{\lambda_1} \tilde{W}_i^T(t) D_i^\alpha \tilde{W}_1(t) \]

Substituting (25) into (27), we have

\[ D_i^\alpha V_i(t) \leq -z_i(t) \bar{e}_i(\tilde{z}_i(t)) - k_i \bar{z}_i(t) + z_i(t) z_2(t). \quad (28) \]

Next, let the Lyapunov function be

\[ V_i(t) = V_{i-1}(t) + \frac{1}{2} \sum_{j=2}^{i} \tilde{z}_j^2(t) + \frac{1}{2\lambda_1} \sum_{j=2}^{i} \tilde{W}_j^T(t) \tilde{W}_j(t). \quad (29) \]

According to (1), (11), (20), (28), and Lemma 2, we have
\[
D_t^\alpha V_{n-1} \leq -z_1(t)e_1(\bar{\zeta}_1(t)) - k_1z_1^2(t) + z_1(t)z_2(t) + \sum_{j=2}^{n-1} z_j(t)D_t^\alpha z_j(t) + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t) \\
= \sum_{j=2}^{n-1} z_j(t) \left[ f_j(\bar{\zeta}_j(t)) + z_{j+1}(t) + \alpha_j(t) - \sum_{j=2}^{n-1} \left( \frac{\partial \alpha_{j-1}(t)}{\partial \zeta_i(t)} D_t^\alpha \bar{\zeta}_i(t) + \frac{\partial \alpha_{j-1}(t)}{\partial \zeta_i(t)} D_t^\alpha \bar{\zeta}_i(t) \right) \right] \\
- z_1(t)e_1(\bar{\zeta}_1(t)) - k_1z_1^2(t) + z_1(t)z_2(t) + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t) \\
= \sum_{j=2}^{n-1} z_j(t) \left[ z_{j+1}(t) + \alpha_j(t) + \gamma_j(\bar{\zeta}_j(t)) \right] - z_1(t)e_1(\bar{\zeta}_1(t)) - k_1z_1^2(t) + z_1(t)z_2(t) + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t)
\] (30)

Substituting (21) into (30) and using (25), we have

\[
D_t^\alpha V_{n-1} \leq \sum_{j=2}^{n-1} z_j(t) \left[ z_{j+1}(t) + \alpha_j(t) + \gamma_j(\bar{\zeta}_j(t)) \right] - z_1(t)e_1(\bar{\zeta}_1(t)) - k_1z_1^2(t) + z_1(t)z_2(t) + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t) \\
= \sum_{j=2}^{n-1} z_j(t) \left[ z_{j+1}(t) - W_j^T(t)\psi(\bar{\zeta}_j(t)) - z_{j-1}(t) - k_1z_1^2(t) + \gamma_j(\bar{\zeta}_j(t)) \right] + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t) \\
- z_1(t)e_1(\bar{\zeta}_1(t)) - k_1z_1^2(t) + z_1(t)z_2(t) \\
\leq \sum_{j=2}^{n-1} k_1z_1^2(t) + \sum_{j=2}^{n-1} z_j(t) \left[ z_{j+1}(t) - W_j^T(t)\psi(\bar{\zeta}_j(t)) - z_{j-1}(t) + \gamma_j(\bar{\zeta}_j(t)) \right] + \frac{1}{\lambda_j} \sum_{j=2}^{n-1} \bar{W}_j^T(t)D_t^\alpha W_j(t) \\
- z_1(t)e_1 + z_1(t)z_2(t) \\
\leq \sum_{j=2}^{n-1} k_1z_1^2(t) - z_{n-1}(t)z_n(t) + \sum_{j=2}^{n-1} \bar{\zeta}_j(t)z_j(t).
\] (31)

Finally, let
\[
V_n(t) = V_{n-1}(t) + \frac{1}{2}z_1^2(t) + \frac{1}{2\lambda_1} \bar{W}_n^T(t)\bar{W}_n(t).
\] (32)

Then, after some manipulations, we have

\[
D_t^\alpha V_n \leq -\sum_{j=1}^{n} k_1z_1^2(t) + \sum_{j=1}^{n} \bar{\zeta}_j(t)z_j(t) - \sum_{j=1}^{n} k_{1j}z_j(t).
\] (33)

Thus, if the parameter \( k_{1j} \) is chosen such that
\[
k_{1j} \geq \bar{\zeta}_j,
\] (34)

and according to Lemma 1, the tracking error \( z_j(t) \) tends to zero asymptotically. This ends the proof of Theorem 1.

### 4. Simulation Studies

In this part, to check our theoretical derivation, an example will be given. Consider the control problem of fractional-order Arneodo system, which is given by [35, 36]

\[
D_t^\alpha \zeta_1(t) = f(\zeta_1(t), \zeta_2(t), \zeta_3(t)), \\
D_t^\alpha \zeta_2(t) = f(\zeta_1(t), \zeta_2(t), \zeta_3(t)), \\
D_t^\alpha \zeta_3(t) = -b_1\zeta_1(t) - b_2\zeta_2(t) - b_3\zeta_3(t) + b_4\zeta_4(t) + u(t). \\
\] (35)

Let the initial condition be \( \zeta_1(0) = -2.0, \zeta_2(0) = 5.01, \) and \( \zeta_3(0) = 2.02. \) Firstly, if we assume that \( f(\zeta_1(t), f(\zeta_2(t), \zeta_3(t)), \) and \( u(t) \) are not considered and let \( b_1 = 5.50, b_2 = 3.50, b_3 = 0.80, b_4 = 1.01, \) and \( \alpha = 0.935, \) the chaotic behavior of the system (35) is as given in Figure 2. Let \( f(\zeta_1(t)) = 4.5\zeta_1^{e_1(t)}, f(\zeta_1(t), \zeta_2(t)) = 3\zeta_1^2(t) + \zeta_2^3, \) \( k_1 = k_2 = k_{11} = k_{12} = 0.95, \) and \( \lambda_1 = \lambda_5 = 25. \) Define the referenced signal \( \zeta_d(t) \) as

\[
D_t^\alpha \zeta_d(t) = \zeta_c(t), \\
D_t^\alpha \zeta_d(t) = 25\zeta_d(t) - 9\zeta_c(t) + 25\zeta_c(t), \\
\] (36)

where \( \zeta_c(t) \) is given by
In the simulation, we should use 3 neural networks, whose nodes are 9, 81, and 729, respectively. The simulation results are shown in Figures 3–7. Figure 3 mainly depicts the performance of signal $\zeta_1(t)$ tracking the signal $\zeta_d(t)$ which is defined by (36) and (37). From this figure, we can see that in the first 15 seconds, that is, when $\zeta_d(t)$ is a constant, the tracking performance is good. When the time $t$ is more than 15 seconds, the reference signal $\zeta_d(t)$ has a sudden change, but after control, the output of the system can track $\zeta_d(t)$ in a very short time. This also shows that the method has very good robustness. Figure 4 gives the virtual inputs $a_1(t)$ and $a_2(t)$. Figure 5 depicts the final controller $u(t)$. From the above two pictures, we can see that all the inputs are smooth. Figure 6 shows the tracking errors $z_1(t)$, $z_2(t)$, and $z_3(t)$. Finally, Figure 7 depicts the norm of $W_1(t)$, $W_2(t)$, and $W_3(t)$. Generally speaking, our
5. Conclusion

This paper concerns the control problem uncertain fractional-order nonlinear systems by using neural network backstepping technique. First, in the backstepping design, all virtual control inputs’ fractional-order derivatives are approximated together with the system uncertainties by using 3-layer neural networks. By using this method, we need not calculate the fractional-order derivative of virtual input repeatedly and thus the problem of “explosion of terms” is overcome. To handle the approximation error, a robust term is needed. Finally, simulation studies illustrate the effectiveness of the proposed method. Noting that the nonlinear input is not considered in this work, how to solve this problem is one of our future research directions.

Data Availability

All datasets generated for this study are included in the manuscript.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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