

## Research Article

# Stability Evaluation of Slope Based on Global Sensitivity Analysis

Zhaoxia Xu <sup>1,2,3</sup>, Xiuzhen Wang <sup>1,4</sup>, Lu Guo,<sup>1</sup> and Teng Yu<sup>1,3</sup>

<sup>1</sup>School of Civil Engineering and Architecture, Suqian University, Suqian 223800, China

<sup>2</sup>School of Civil Engineering, Chongqing University, Chongqing 400045, China

<sup>3</sup>Key Laboratory of Geological Environment and Engineering Health Monitoring, Suqian University, Suqian 223800, China

<sup>4</sup>Jiangsu Prefabricated Building and Intelligent Construction Engineering Research Center, Suqian University, Suqian 223800, China

Correspondence should be addressed to Xiuzhen Wang; wangxiuzhen@vip.qq.com

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The uncertainty of parameters will have a significant impact on slope stability, where sensitivity analysis is a commonly used method in uncertainty research. However, traditional sensitivity analysis method costs much computation time. When calculating the sensitivity index of one parameter, all other parameters are taken as fixed values, and the uncertainty of all parameters cannot be considered simultaneously. Therefore, the variance-based and the moment-independent global sensitivity analysis (GSA) methods are both introduced to determine the influence of geotechnical parameters on slope stability in this study. To solve the importance index of GSA, the least angle regression algorithm, the kernel density estimation, and orthogonal polynomial estimation methods are developed to obtain variance-based importance index and the moment-independent importance index, respectively. The proposed methods allow all variables to change simultaneously within their variation range and have high computational efficiency. The results are in good at with those obtained by the variance-based Monte Carlo simulation method, which is considered as the exact solution for obtaining the importance index. The influence of the correlation between the shear strength parameters ( $c$  and  $\varphi$ ) on the importance index is also studied, which indicates that the negative correlation will have a great impact on the importance index, which in turn affects the safety assessment of slope. Three engineering cases have been studied for engineering application, and the compared results indicate that the impact of the geotechnical parameters uncertainty on the safety factor ( $F_s$ ) and failure probability ( $p_f$ ) are different. Therefore, the approaches based on GSA which can integrate the  $F_s$  with  $p_f$  will be a promising approach for slope stability evaluation.

## 1. Introduction

It is well-known that the uncertainty of random variables will greatly affect the output response. It is important for engineering risk assessment to determine the influence of the uncertainty of random variables on output response [1]. There are many uncertainties in the actual slope engineering, so it is important to study these uncertainties for slope stability. For example, Cai et al. [2] proposed an adaptive sampling method based on limit equilibrium model and stochastic condition method in slope stability analysis to reduce the uncertainty. In order to determine the availability of qualitative and quantitative methods for uncertainty analysis in rock slope stability, Abdulai and Sharifzadeh [3]

analyzed and summarized the uncertainty and uncertainty analysis methods, problems, and development in geotechnical engineering modeling. Zhao and Li [4] used artificial bee colony and relevance vector machine to establish a model to describe the relationship between displacement increments and geomechanical parameters so as to predict rock mass deformation and related uncertainties. Under the combined action of continuous rainfall and water level fluctuation, Su et al. [5] studied the stability of reservoir slope using the deterministic method and uncertain method (the Monte Carlo simulation method). It is worth noting that although there are many studies focusing on the uncertainty of geological parameters, while the sensitivity analysis method costs much computation time. When calculating the

sensitivity index of one parameter, all other parameters are taken as fixed values, and the uncertainty of all parameters cannot be considered simultaneously. Further research is needed to quantify and distinguish the impact of this uncertainty on the slope stability [6, 7].

Sensitivity analysis is a commonly used method in uncertainty research, and the global sensitivity analysis (GSA) method has got more and more attention in recent years. GSA, also known as importance measurement analysis, considers changes in geotechnical parameters simultaneously and allows them to change over their entire range of distribution (i.e., uncertainty range). According to the importance index of each variable, the relatively important and unimportant parameters can be distinguished, and the relative contribution of the uncertainty of each random variable to the uncertainty of the model output response can be quantified. In slope engineering activities, focusing on the uncertainty of parameters with high importance index can greatly reduce the uncertainty of output response, thus effectively improving the efficiency of slope engineering design and optimization.

Among the global sensitivity analysis methods, the variance-based method and the moment-independent method are widely used, and the first method is usually considered to be an exact solution, which is often used to verify other methods. A large amount of literature has conducted in-depth research on these two methods. For example, Alexanderian et al. [8] developed a variance-based sensitivity analysis method that uses the correlation structure of the problem under study and uses alternative models to speed up the calculation. Subramanian and Mahadevan [9] proposed a semianalytical method based on variance-based sensitivity analysis for calculating the sensitivity index of linear systems with Gaussian random process inputs and nonlinear systems with non-Gaussian random process outputs. Yun et al. [10] proposed a new method to calculate moment-independent importance index based on the law of total expectation in the successive intervals without overlapping and Bayes theorem. Xu et al. [11] proposed a moment-independent method combined with the kernel density estimate to analysis the uncertainty of the geotechnical parameters for slope stability. Khan et al. [12] proposed and tested a method for accelerating global sensitivity analysis in the context of free-form shape optimization.

Therefore, considering the uncertainty of the impact factor of the slope stability, the variance-based global sensitivity analysis method combined with the least angle regression algorithm and the moment-independent global sensitivity analysis method combined with kernel density estimation and orthogonal polynomial estimation are developed to determine the influence of the uncertainty of the influence parameters of slope stability.

## 2. Methods of the Global Sensitivity Analysis

**2.1. Least Angle Regression (LARS) Algorithm.** The essence of GSA of geotechnical parameters in slope stability is data mining, and feature selection techniques can be used to evaluate the importance of these parameters under a certain standard. Among feature selection methods, supervised feature selection algorithms have been increasingly used, such as the forward selection algorithm and the forward gradient algorithm. Combining the advantages of the forward selection algorithm and the forward gradient algorithm, Efron et al. [13] proposed the LARS algorithm. LARS improves the disadvantage that the forward gradient algorithm only advances a small step in each fitting and regression process and improves the operation efficiency. However, its step size is less than the step size of the forward selection algorithm to ensure the accuracy of the results.

The main operation process of LARS algorithm is as follows: first, all the coefficients in the regression model are set to 0, and the input variable with the greatest correlation with the output response is found. Second, find a second input variable in the direction of this input variable that maximizes the correlation coefficient with the current residual vector. Finally, follow the direction of the angle bisector of the abovementioned two input variables to find the third variable in the same way, and so on until all input variables are selected into the regression model or reach the set threshold, and finally, all regression coefficient vectors and predicted value are obtained. The predicted value of the response can be obtained by the LARS algorithm in  $n$  steps ( $n$  represents the number of input variables), which is much smaller than the forward gradient algorithm (it needs thousands of steps). Therefore, the computational efficiency has been significantly improved. The regression model of the LARS algorithm can be expressed as follows [14]:

$$\begin{aligned} \min S(\hat{\beta}) &= \|y - \hat{\mu}\| \\ &= \sum_{i=1}^n (y_i - \hat{\mu}_i)^2 = \sum_{i=1}^n \left( y_i - \sum_{j=1}^m x_{ij}\beta_j \right)^2, \end{aligned} \quad (1)$$

where  $(x_{i1}, x_{i1}, \dots, x_{im})$  and  $y_i$  are the input variables and output response corresponding to the  $i^{\text{th}}$  sample, respectively;  $\hat{\mu}_i$  is the predictive value of the output response; and  $\beta_j$  is the regression coefficient of  $x_{ij}$ . To make  $S(\hat{\beta})$  reach the minimum value, it is necessary to continuously adjust  $\beta_j$  through the LARS algorithm, and the following conditions are met:

$$\sum_{j=1}^m |\beta_j| \leq t_c, \quad (2)$$

where  $t_c$  is the constraint value, and  $t_c \geq 0$ .

Then, the variance-based importance measure index  $S_i$  can be expressed as follows:

$$S_i = \frac{\text{Var}(\hat{Y})}{\text{Var}(Y)} \quad (3)$$

where  $i = 1, 2, \dots, n$ , and  $\text{Var}(Y)$  and  $\text{Var}(\hat{Y})$  are expressed as follows, respectively:

$$\text{Var}(Y) = \frac{1}{N-1} \sum_{k=1}^N (y_k - \bar{y})^2, \quad (4)$$

$$\text{Var}(\hat{Y}) = \frac{1}{N-1} \sum_{k=1}^N (\hat{\mu}_k - \bar{\mu}_k)^2, \quad (5)$$

where  $\bar{y}$  is the mean of the output response  $Y$ ,  $\hat{\mu}_k$  is the predictive value, which can be obtained by LARS, and  $\bar{\mu}_k$  is the mean value of  $\hat{\mu}_k$ .

According to the abovementioned principles, the function of  $Y$  needs to run  $N$  times to obtain the importance index, where  $N$  is the sample size of the random variables.

$S_i$  obtained by Monte Carlo simulation is considered to be an exact solution and is usually used to verify the results of other methods in the global sensitivity analysis. Therefore,  $S_i$  was used for the comparative analysis in this study, which is expressed as follows [15]:

$$S_i^v = \frac{\text{Var}(E(Y|x_i))}{\text{Var}(Y)}, \quad (6)$$

where  $E(Y|x_i)$  is the conditional mean value of  $Y$ .

It is well-known that the function of  $Y$  needs to run  $(nN+1)N$  times to obtain the importance index, where  $n$  is the number of the random variables, and  $N$  is the same as abovementioned.

**2.2. Moment-Independent Method.** It is pointed out that the variance-based GSA method only considers variance, and  $S_i$  will inevitably lead to the loss of parameter information and lack of moment independence. In view of this, Borgonovo [16] proposed a moment-independent importance index based on the comprehensive consideration of the requirements of Satelli, Helton, and Davis for the importance index (i.e., globality, universality, quantification, and moment independence). The principle of moment-independent method is to study the average influence of the uncertainty of the input parameters on the probability density function or cumulative distribution function of the model output response, so as to determine the influence of the input parameters on the output response. It can obtain a global estimate of the importance of the input parameters in the model, and its computational efficiency is much higher than that of variance-based GSA methods.

The process of the moment-independent method is as follows: Substitute the random variables  $X_1, X_2, \dots, X_n$  into the function  $Y = G(X_1, X_2, \dots, X_n)$  to calculate the actual value of the output response  $Y$ . When  $X_i$  takes each realized value, the cumulative influence of  $X_i$  on the probability density or probability distribution of  $Y$  is expressed as follows:

$$s(X_i) = \int_{-\infty}^{+\infty} |f_Y(y) - f_{Y|X_i}(y)| dy, \quad (7)$$

where  $s(X_i)$  is the shift between  $f_Y(y)$  and  $f_{Y|X_i}(y)$ , and  $f_Y(y)$  and  $f_{Y|X_i}(y)$  are, respectively, the unconditional probability density function and the conditional probability density function of  $Y$ .

The moment-independent importance index  $\delta_i$  is defined as follows:

$$\delta_i = \frac{1}{2} E_{X_i}[s(X_i)], \quad (8)$$

where  $E_{X_i}[s(X_i)]$  is the expectation of  $s(X_i)$ , which can be obtained by

$$\begin{aligned} E_{X_i}[s(X_i)] &= \int_{-\infty}^{+\infty} f_{X_i}(x_i) s(X_i) dx_i \\ &= \int_{-\infty}^{+\infty} f_{X_i}(x_i) \left[ \int_{-\infty}^{+\infty} |f_Y(y) - f_{Y|X_i}(y)| dy \right] dx_i. \end{aligned} \quad (9)$$

It can be seen from equations (4) and (5) that the key to obtain  $\delta_i$  is to determine  $f_Y(y)$  and  $f_{Y|X_i}(y)$  of  $Y$ , which is also the difficulty of moment-independent GSA. The kernel density estimation (KDE) method and orthogonal polynomial estimation (OPE) can directly fit the probability distribution according to the characteristics of the data samples themselves, and the accuracy is high, which are more representative methods among the nonparametric estimation methods.

The kernel density estimate of  $f_Y(y)$  and  $f_{Y|X_i}(y)$  can be expressed as follows:

$$\hat{f}_Y(y) = \frac{1}{Nh} \sum_{i=1}^N K\left(\frac{y - y_i}{h}\right), \quad (10)$$

where  $\hat{f}_Y(y)$  is the kernel density estimation of  $f_Y(y)$ ,  $h$  is the bandwidth parameter,  $N$  and  $y_i$  are, respectively, the sample size and function value of  $Y$ , and  $K(\cdot)$  is the kernel density function, which needs to satisfy the following condition:

$$K(y) \geq 0, \int_{-\infty}^{+\infty} K(y) dy = 1. \quad (11)$$

The Gaussian kernel function is adopted to estimate  $\hat{f}_Y(y)$  in this study, which is expressed as follows:

$$K\left(\frac{y - y_i}{h}\right) = \frac{1}{\sqrt{2\pi}} e^{-((y - y_i)/h)^2/2}. \quad (12)$$

In order to avoid large errors caused by a single nonparametric estimation method, an orthogonal polynomial estimation method is introduced in this study. Considering that Hermite polynomial is simple and easy to implement, this study chooses it to approximate  $f_Y(y)$ . The main process is listed as follows: the probability density function  $f(x)$  can be estimated by the expansion of the higher-order moment, which means  $f(x)$  is nearly equal to the product of the orthogonal polynomial function and the weight function according to the principle of the Hermite orthogonal polynomial, which is expressed as follows:

$$\hat{f}(x) = \rho(x) \sum_{i=0}^n a_i H_i(x), \quad (13)$$

where  $\rho(x) = (1/\sqrt{2\pi}\sigma)e^{[-(x-\mu)^2/2\sigma^2]}$ ,  $\mu$  and  $\sigma$  are the mean and standard deviation, respectively,  $a_i$  is the undetermined coefficient, which is determined by  $a_i = \sum_{j=0}^i a_{ij} u_j(x)/h_i$ , where  $a_{ij}$  is a constant,  $u_j(x)$  is the  $j^{\text{th}}$  order central moment of the distribution function, and  $h_i = 2^i i! \sqrt{\pi}$ .

Then,  $f_Y(y)$  is estimated by

$$\hat{f}_Y(Y) = \rho(y) \sum_{i=0}^n a_i H_i(y). \quad (14)$$

The calculation process of  $f_{Y|X_i}(y)$  is similar to that of  $f_Y(y)$ .

Set  $\delta_i^p$  as the moment-independent importance measure index of failure probability, which is expressed as follows [17]:

$$\begin{aligned} \delta_i^p &= \frac{1}{2} E \left[ \left| p_{fY} - p_{fY|X_i} \right| \right] \\ &= \frac{1}{2} \int_{-\infty}^{+\infty} \int_F f_Y(y) dy - \int_F f_{Y|X_i}(y) dy \Big| f_{X_i}(x_i) dx_i \\ &= \frac{1}{2} \int_{-\infty}^{+\infty} \left| p_{fY} - p_{fY|X_i} \right| f_{X_i}(x_i) dx_i, \end{aligned} \quad (15)$$

where  $E(\cdot)$  is expectation;  $p_{fY}$  and  $p_{fY|X_i}$  are, respectively, the unconditional failure probability and conditional failure probability of  $Y$ ;  $F = \{X: G(X) \leq c_s\}$ , in which  $X$  is the random variable and  $X = (X_1, X_2, \dots, X_n)$ ;  $G(X)$  is the function of  $Y$ ;  $c_s$  is a constant; and  $f_{X_i}(x_i)$  is the probability density function of  $X_i$ .

Figure 1 shows the flowchart, and the function of  $Y$  needs to run  $(n+1)N$  times to obtain the importance index, where  $n$  and  $N$  are the same as abovementioned.

### 3. Case Study

**3.1. GSA of the Landslide Stability along PR303.** The landslides caused by the Wenchuan earthquake are widely distributed in the southwest of China, and some of the landslide debris accumulates on the steep terrain, which is easily affected by external factors (such as aftershocks and rainfall infiltration) and leads to instability and damage again. For example, the landslides induced by the Wenchuan earthquake distributed from K1 to K18 of the province road (PR) 303 are prone to reconstruction under the action of heavy rainfall (as shown in Figure 2(a)). With the help of site survey and GIS technology, 53 loose deposits landslides have been identified between K2 and K7 along PR303 (as shown in Figure 2(b)). These loose deposits landslides are considered as the representative instability slope. According to statistics, there were many landslides during the rainy season from 2009 to 2011, resulting in a large number of casualties and property losses. Tang and Zhang [18] predicted that slope failure would continue to occur in the next few years.

According to reference [18], the stability of the above-mentioned landslides can be analyzed by the infinite slope model. The safety factor ( $F_s$ ) of an infinite slope can be calculated by equation (13) as follows [19, 20]:

$$F_s = \frac{cL + N_t \tan \varphi}{(1 - k_v)(W_n + W_{\text{sat}}) \sin \xi + F_w + k_h(W_n + W_{\text{sat}}) \cos \xi} \quad (16)$$

where  $c$  and  $\varphi$  are, respectively, the cohesion and internal friction angle;  $L$  and  $\xi$  are the length of a slice and the slope angle, respectively;  $k_v$  and  $k_h$  are, respectively, the vertical and horizontal seismic acceleration coefficients;  $F_w$  and  $N_t$  are, respectively, the seepage force and the normal force on the sliding surface;  $W_{\text{sat}}$  and  $W_n$  are, respectively, the saturated zone and the weights of slices associated with the natural zone, and these forces are expressed as follows:  $W_n = \gamma L(H-h)\cos \xi$ ,  $W_{\text{sat}} = \gamma_{\text{sat}} Lh \cos \xi$ ,  $N_t = (1 \pm k_v)(W_n + W_{\text{sat}})\cos \xi - k_h(W_n + W_{\text{sat}})\sin \xi$  and  $F_w = \gamma_w Lh \sin \xi \cos \xi$ , where  $H$  and  $h$  are, respectively, the thicknesses of the whole soil and saturated part of the soil, and  $h = mH$  ( $m$  is the saturation index); and  $\gamma_n$ ,  $\gamma_{\text{sat}}$  and  $\gamma_w$  are, respectively, the natural unit weight, saturated unit weight of soil, and the unit weight of water.

In order to evaluate the influence of the parameters on the stability of the abovementioned loose deposit landslides,  $c$ ,  $\varphi$ ,  $\gamma$ ,  $\gamma_{\text{sat}}$ ,  $k_h$ ,  $k_v$ ,  $\xi$ ,  $H$ , and  $m$  are taken as random variables for GSA in this study. There are 53 statistical data for  $\gamma$ ,  $\gamma_{\text{sat}}$ ,  $\xi$ , and  $H$  according to reference [18].  $\gamma$  and  $\gamma_{\text{sat}}$  follow lognormal distribution, and  $\xi$  and  $H$  follow normal distribution based on the statistical analysis of these data. There is no statistical data for random variable  $c$ ,  $\varphi$ ,  $m$ ,  $k_h$ , and  $k_v$ . Only the mean value of  $c$  and  $\varphi$  are known. The probability density distributions of  $c$  and  $\varphi$  are considered to follow normal or lognormal distributions [21, 22]. Wang et al. [23] suggested that the lognormal distribution is more suitable for simulating  $c$  and  $\varphi$  because of their physical meaning. Hence,  $c$  and  $\varphi$  are considered to follow the lognormal distribution in this case study. According to Li et al. [24], the negative correlation between  $c$  and  $\varphi$  varies from  $-0.20$  to  $-0.92$  based on the statistical information. Due to the lack of experimental data, the negative correlation coefficient between  $c$  and  $\varphi$  is assumed to be  $-0.5$  in this case study. For  $m$ ,  $k_h$ , and  $k_v$ , they vary equally between  $[0, 1]$ ,  $[0.1, 0.6]$ , and  $[0.05, 0.45]$ , respectively, according to reference [20], so this paper assumes that they all follow uniform distribution. In summary, the statistical information of random variables is shown in Table 1. Other parameter values are as follows:  $\gamma_w = 9.81 \text{ kN/m}^3$  and the sample size  $N = 1 \times 10^3$ .

Taking  $F_s$  as the output response, the importance index of the nine random variables calculated by MC, LARS, KDE, and OPE are shown in Figure 3. It can be seen from Figure 3(a) that the importance indexes of  $\xi$ ,  $k_h$ , and  $m$  are much larger than other random variables, which means that  $\xi$  and  $k_h$  have a greater impact on the stability of the loose deposit landslides when the correlation between  $c$  and  $\varphi$  is ignored. The importance indices of  $m$  and  $\varphi$  are slightly smaller than  $\xi$  and  $k_h$ , which indicates that their influence on slope stability is also very important. The importance indices

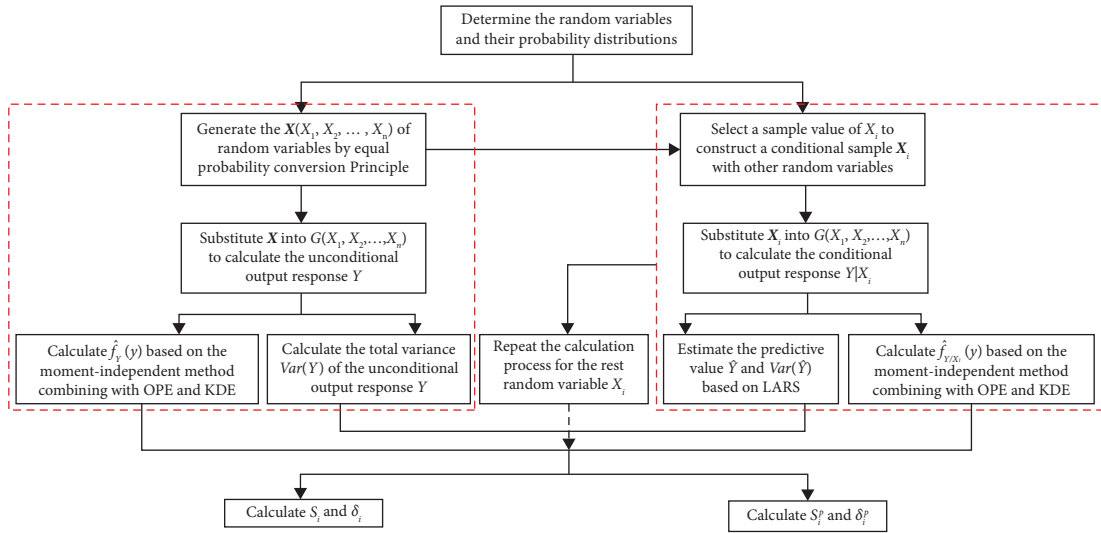
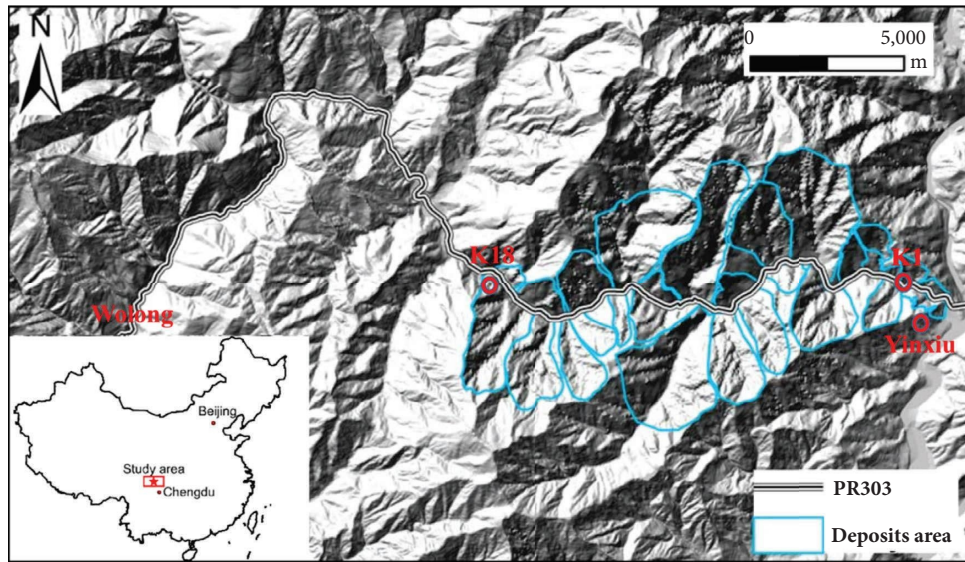


FIGURE 1: Calculation process of the importance index.



(a)

FIGURE 2: Continued.

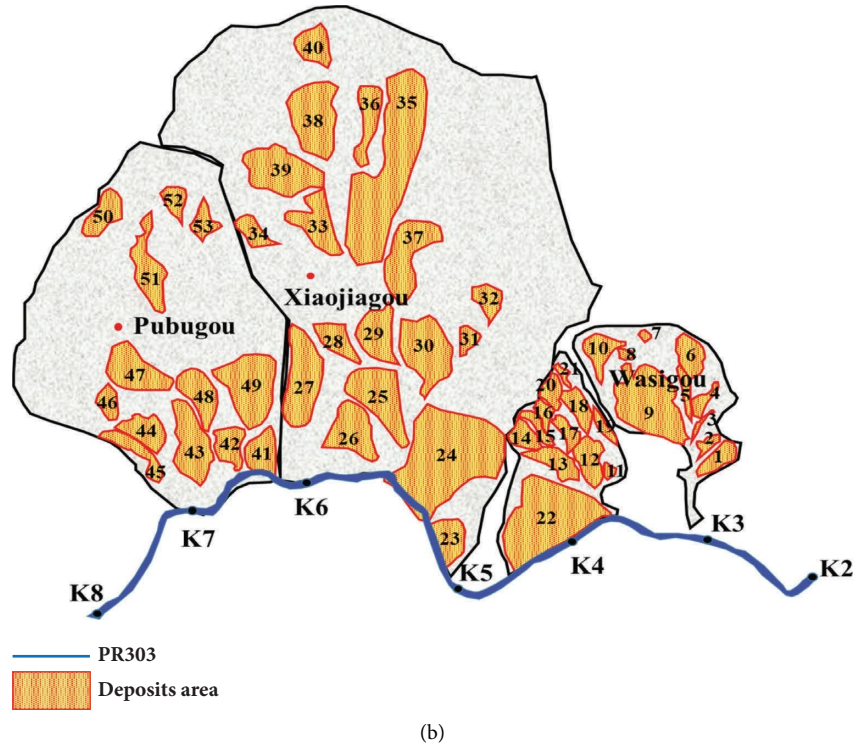


FIGURE 2: Landslides along PR303: (a) landslides between K1 and K18 and (b) loose deposits landslides between K2 and K7 [18].

TABLE 1: Random variables of the loose deposits landslides.

Random variables	Distribution	Probability density function (PDF)	Statistical information	Unit
$c$	Lognormal	$f(x) = (1/qx\sqrt{2\pi})\exp[-((\ln x - p)^2/2q^2)]$	$\mu = 8, \sigma = 2.56$	kPa
$\varphi$			$\mu = 32.7, \sigma = 4.578$	$^\circ$
$\gamma$			$\mu = \exp(p + 0.5q^2),$	$\text{kN/m}^3$
$\gamma_{\text{sat}}$			$\sigma^2 = [\exp(q^2) - 1] \times \exp(2p + q^2)$	$\mu = 17, \sigma = 1.7$
$\xi$	Normal	$f(x) = (1/\sqrt{2\pi}\sigma)\exp(-(x - \mu)^2/2\sigma^2)$	$\mu = 27.4, \sigma = 7.69$	$^\circ$
$H$			$\mu = 374.72, \sigma = 161.11$	$m$
$m$	Uniform	$f(x) = \begin{cases} 1/(b-a), & a < x < b \\ 0, & \text{other} \end{cases}$	$[a, b] = [0, 1]$	—
$k_h$			$[a, b] = [0.1, 0.6]$	—
$k_v$			$[a, b] = [0.05, 0.45]$	—

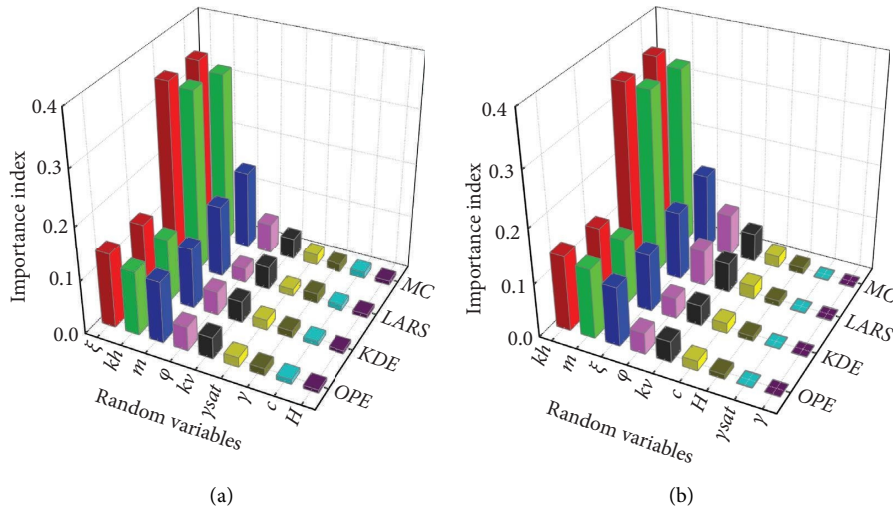


FIGURE 3: Importance indices of random variables for the loose deposits landslides along PR303: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

of  $c$  and  $H$  are small, which means that  $c$  and  $H$  have little impact on the stability of these landslides. The orders of the importance index calculated by MC, LARS, KDE, and OPE are  $\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$ ,  $\xi > k_h > m > k_v > \varphi > \gamma > \gamma_{\text{sat}} > c > H$ ,  $\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > H > c$  and  $\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$ , respectively.

As shown in Figure 3(a), the importance index calculated by MC and LARS are very close, and the importance orders are basically the same, which means the accuracy and validity of LARS have been verified. The values of the importance index obtained by KDE and OPE are different from those obtained by MC and LARS because the calculation principle of the variance-based GSA is different from that of the moment independence-based GSA. However, the importance orders calculated by KDE and OPE are almost exactly identical to that of MC. It is pointed out that if the importance orders calculated by other methods are the same as or similar to that of the variance-based MC method, then the results of these methods are accurate and reliable [25]. Therefore, the accuracy and validity of KDE and OPE have also been verified in this study.

It can be seen from Figure 3(b) that  $k_h$  and  $m$  have a greater impact on the stability of the loose deposit landslides when  $c$  and  $\varphi$  are negatively correlated, then followed by  $\xi$ ,  $\varphi$ ,  $k_v$ , and  $c$ , while  $H$ ,  $\gamma_{\text{sat}}$ , and  $\gamma$  have little impact. The orders of the importance index calculated by MC, LARS, KDE, and OPE are  $k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$ ,  $k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$ ,  $k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > \gamma > H$  and  $k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > \gamma > H$ , respectively. The importance orders of the nine random variables obtained by these four methods are basically the same, which also indicates that the accuracy and validity of the proposed methods are verified.

Comparing Figure 3(a) and 3(b), when  $c$  and  $\varphi$  are independent, the importance orders are significantly different from that of when  $c$  and  $\varphi$  are negatively correlated. For example, the importance order obtained by MC when  $c$  and  $\varphi$  are independent is  $\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$ , while it is  $k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$  when  $c$  and  $\varphi$  are negatively correlated. Similar results were obtained by the other three methods. Therefore, it can be derived from this that the correlation between  $c$  and  $\varphi$  will have an important influence on the importance index, which cannot be ignored in the sensitivity analysis of slope stability.

**3.2. GSA of the Typical Section of Xiaolangdi Dam.** The Xiaolangdi Dam is an earth-rock dam with a loam inclined core wall. The elevation of the dam crest is 281m, and the normal water storage level of the reservoir is 275 m. The dam crest is 1,667 m long, and the dam bottom width is 864 m. The dam site is mainly composed of calcareous siliceous sandstone and calcareous cementitious sandstone. The base layer of the dam is composed of sandy pebble and bedrock from top to bottom, and the deepest part of sandy pebble overburden can reach 80 m. The core wall of the dam is made of clay, and both sides of the core wall are filled with enrockment. The antiseepage material of the inclined core wall is mainly composed of silty clay,

and a high plastic soil zone is set at the top of the antiseepage wall.

As shown in Figure 4, the inclined wall (the clay area) has an important role in Xiaolangdi Dam. Considering that the D0 + 387.50 section is the largest one in the Xiaolangdi Dam, so it is very meaningful to perform the stability analysis in this study. According to Xu et al. [11],  $F_s$  can be obtained by the following equation set:

$$\begin{cases} F_1(\alpha, \beta, F_s, t) = \sum M_x = 0, \\ F_2(\alpha, \beta, F_s, t) = \sum M_y = 0, \\ F_3(\alpha, \beta, F_s, t) = \sum M_z = 0, \end{cases} \quad (17)$$

where  $\alpha$  and  $\beta$  are the inclinations of intercolumn forces;  $M_x$ ,  $M_y$ , and  $M_z$  are, respectively, the moments along the  $x$ ,  $y$ , and  $z$  axes; and  $t$  is any time within the seismic wave period. For more details of the equations and the solution process, please refer to Zhou and Cheng [26] and Xu et al. [11].

For simplifying the calculation,  $c$ ,  $\varphi$ ,  $k_h$ ,  $t$ , and  $f$  are considered as random variables in this case study, where  $f$  is the amplification factor. Other symbols have the same meaning as above. The experimental data of  $c$  and  $\varphi$  are obtained by the consolidated-undrained triaxial compression test, and both  $c$  and  $\varphi$  follow normal distribution [27, 28]. In addition, the correlation coefficient between  $c$  and  $\varphi$  is  $-0.544$ . Other random variables,  $k_h$ ,  $t$ , and  $f$ , are assumed to follow a uniform distribution which is similar to those of case study 1. The information of these five random variables is listed in Table 2.

Figure 5(a) shows that among the 5 random variables, the random variable  $\varphi$  has the greatest impact on the stability of section D0 + 387.50 slope, while  $f$  has the least impact when the correlation between  $c$  and  $\varphi$  is ignored. The importance orders obtained by MC, LARS, KDE, and OPE are consistent, which are  $\varphi > t > c > k_h > f$ . Therefore, the results calculated by LARS, KDE, and OPE are accurate. As shown in Figure 5(b), when  $c$  and  $\varphi$  are negatively correlated, the importance orders obtained by MC, LARS, KDE, and OPE are consistent, which are  $\varphi > t > k_h > c > f$ . It is worth noting that the value of the importance index of the 5 random variables are significantly different when the relationship between  $c$  and  $\varphi$  are different, and the importance orders are also different. Therefore, the correlation of  $c$  and  $\varphi$  takes an important role in stability analysis of the section D0 + 387.50 slope.

**3.3. GSA of the Highway Rock Slope.** According to Chen [29], the highway slope is a homogeneous rock slope whose failure mode is plane shear sliding failure. The slope height and slope angle are, respectively, 150 m and  $45^\circ$ , and the shear strength parameters  $c$  and  $\varphi$  are 20 kPa and  $20^\circ$ . The rock mass density is  $27 \text{ kN/m}^3$ . Then,  $F_s$  is expressed as follows [30]:

$$F_s = \frac{\gamma \tan \varphi H x_0 (x_0 - \cot \xi) + 2c(H^2 + x_0^2)}{\gamma H^2 (x_0 - H \cot \xi)}, \quad (18)$$

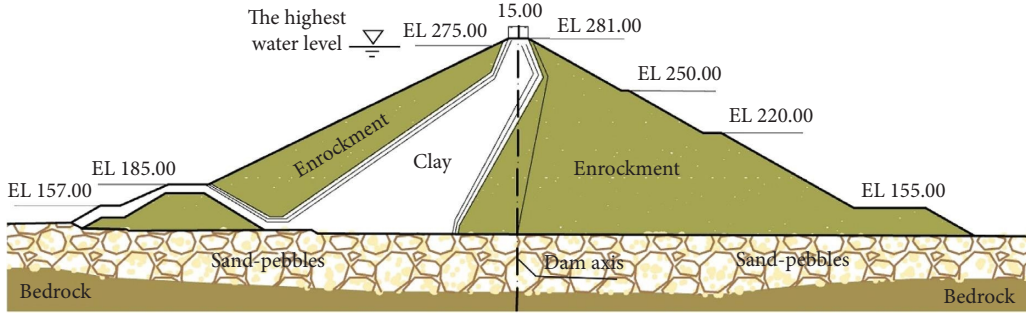


FIGURE 4: D0 + 387.50 section diagram of the Xiaolangdi dam [11] (EL unit: m).

TABLE 2: Random variables of the typical section D0 + 387.50 slope.

Random variables	Distribution	PDF	Parameters	Unit
$c$	Normal	$f(x) = 1/\sqrt{2\pi}\sigma \exp(-(x-\mu)^2/2\sigma^2)$	$\mu = 66.48, \sigma = 28.59$	kPa
$\varphi$			$\mu = 21.99, \sigma = 3.30$	°
$k_h$	Uniform	$f(x) = \begin{cases} 1/(b-a), & a < x < b \\ 0, & \text{other} \end{cases}$	$[a, b] = [0.1, 0.6]$	—
$t$			$[a, b] = [0, 0.2]$	s
$f$			$[a, b] = [1, 2]$	—

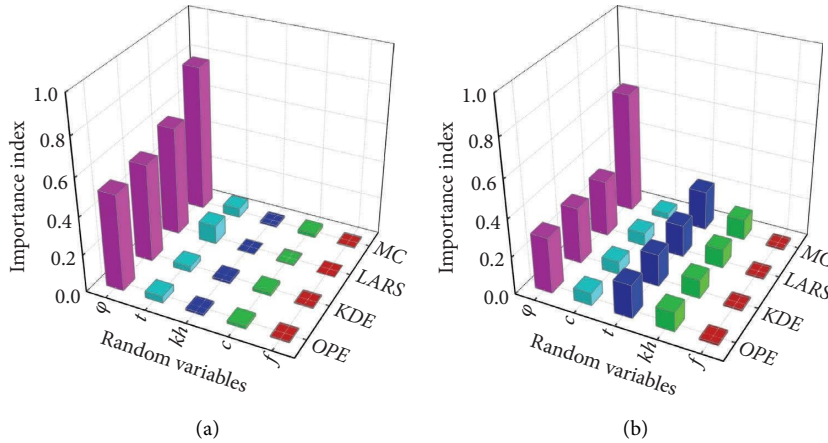


FIGURE 5: Importance indices of random variables for the section D0 + 387.50: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

where  $x_0$  is the projection of the starting point of the slipping surface on the abscissa, and  $H$  is the height of the slope. Other symbols have the same meanings as above.

The parameters  $c$ ,  $\varphi$ ,  $\gamma$ ,  $H$ , and  $\xi$  are taken as the random variables for this case study, but there is no experiment data of them. Only the mean value of  $c$  and  $\varphi$  are known. As abovementioned in case study 1,  $c$  and  $\varphi$  are considered to follow the lognormal distribution, and the correlation coefficient between  $c$  and  $\varphi$  is assumed to be  $-0.5$ . The probability distributions of  $H$  and  $\xi$  are rarely reported, while their influence on slope stability should not be neglected. It is generally assumed that they vary equally within a certain interval; therefore,  $H$  and  $\xi$  are assumed to follow a uniform distribution. Therefore, the statistical information of the five random variables is listed in Table 3. The importance analysis results obtained by MC, LARS, KDE, and OPE are shown in Figure 6.

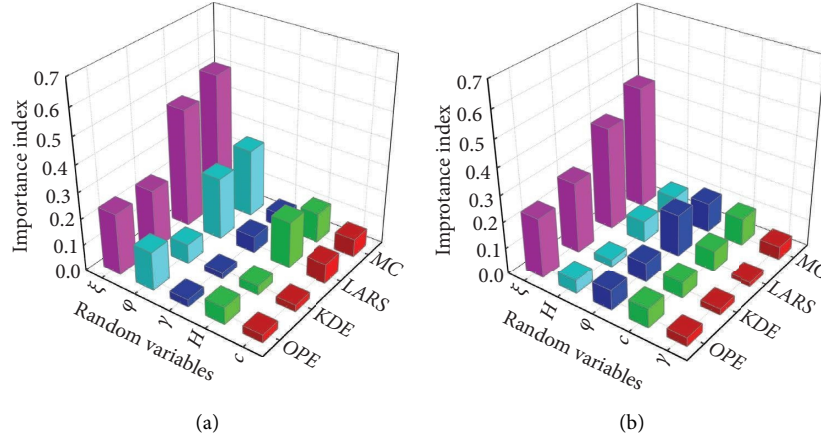
As shown in Figure 6, the importance index of each variable obtained by LARS algorithm is close to that of MC algorithm, which shows that LARS algorithm is effective. The value of the importance index of each variable calculated by KDE and OPE are nearly consistent, while different from those calculated by MC and LARS. The reason has been expressed in the abovementioned case study, so it will not be repeated here. It can be clearly seen from Figure 6(a) that the importance index value of  $\xi$  is obviously the largest and then followed by  $\varphi$ . The importance index of  $c$  and  $H$  is relatively small, and it is the smallest for  $\gamma$ . The importance orders obtained by MC, LARS, KDE, and OPE are the same, which is  $\xi > \varphi > H > c > \gamma$ . Therefore, the accuracy of KDE and OPE have also been verified.

When  $c$  and  $\varphi$  are negatively correlated, as shown in Figure 6(b), the importance orders obtained by MC, LARS, KDE, and OPE are consistent, which are  $\xi > \varphi > c > H > \gamma$ .



TABLE 3: Random variables of the expressway rock slope.

Random variables	Distribution	PDF	Parameters	Unit
$c$	Lognormal	$f(x) = (1/qx\sqrt{2\pi})\exp[-((\ln x - p)^2/2q^2)]$	$\mu = 20, \sigma = 6$	kPa
$\varphi$		$\mu = \exp(p + 0.5q^2),$	$\mu = 20, \sigma = 4$	°
$\gamma$		$\sigma^2 = [\exp(q^2) - 1] \times \exp(2p + q^2)$	$\mu = 27, \sigma = 2.7$	kN/m <sup>3</sup>
$H$	Uniform	$f(x) = \begin{cases} 1/(b-a), & a < x < b \\ 0, & \text{other} \end{cases}$	$[a, b] = [50, 250]$	m
$\xi$			$[a, b] = [15, 75]$	°

FIGURE 6: Importance indices of random variables for the expressway rock slope: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

Compared to Figure 6(a) and 6(b), the importance orders are different when the relationship between  $c$  and  $\varphi$  are different. Therefore, the correlation between  $c$  and  $\varphi$  has important influence on slope stability, which should not be neglected.

#### 4. Global Sensitivity Analysis Based on Failure Probability ( $p_f$ )

Take  $p_f$  as the output response;  $p_f$  is defined as  $p_f = Nu/N$ , where  $Nu$  is the number of  $Fs < F$ ,  $F$  is the critical value of  $Fs$ , and  $N$  is the total number of  $Fs$ . The slope stability analysis model of case study 1 and 2 are relatively simple, so  $Nu$  is set to 1 as usual.  $Nu$  in Case 2 is set to 1.2 according to Yu [27]. Then, the results obtained by MC, LARS, KDE, and OPE are shown in Figures 7–9, respectively.

It can be seen from Figure 7(a) that when  $c$  and  $\varphi$  are independent, the importance orders based on failure probability obtained by MC, LARS, KDE, and OPE are  $\xi > k_h > \varphi > m > k_v > \gamma_{sat} > \gamma > c > H$ ,  $\xi > k_h > m > \varphi > k_v > \gamma_{sat} > c > \gamma > H$ ,  $\xi > k_h > \varphi > m > k_v > \gamma > \gamma_{sat} > c > H$  and  $\xi > k_h > \varphi > m > k_v > \gamma > c > \gamma_{sat} > H$ , respectively. Obviously, the importance orders of failure probability obtained by the four methods are not completely the same. However, only  $c$ ,  $\gamma$ , and  $\gamma_{sat}$  are different, and the orders of the three variables are ranked lower. In addition, the importance index values of  $c$ ,  $\gamma$ , and  $\gamma_{sat}$  are very close. Therefore, the results of GSA based on failure probability obtained by these four methods are still effective and accurate.

When  $c$  and  $\varphi$  are negatively correlated, the importance orders of the random variables based on failure probability

calculated by MC, LARS, KDE, and OPE are  $k_h > m > \xi > \varphi > k_v > c > H > \gamma_{sat} > \gamma$ ,  $k_h > m > \xi > \varphi > k_v > c > \gamma_{sat} > H > \gamma$ ,  $k_h > m > \xi > k_v > \varphi > c > H > \gamma_{sat} > \gamma$  and  $k_h > m > \xi > k_v > \varphi > c > H > \gamma_{sat} > \gamma$ , respectively. It is clear that the importance orders of failure probability obtained by the four methods are not completely consistent. However, only the last three ranking  $\gamma$ ,  $\gamma_{sat}$ , and  $H$  are different, and their importance index values are very close, which are all close to 0. Therefore, the results of GSA based on failure probability calculated by these four methods are still effective and accurate.

Compared with Figure 7(a) and 7(b), when  $c$  and  $\varphi$  are independent, the influence of  $\xi$  on the failure probability is the largest, and  $H$  has the smallest influence on the failure probability; while when  $c$  and  $\varphi$  are negatively correlated,  $k_h$  has the greatest impact on the failure probability and  $\gamma$  or  $H$  has the least effect on the failure probability. The correlation between  $c$  and  $\varphi$  must be given more attention when studying the impact of the uncertainty of random variables on the  $p_f$  for the loose deposits landslides along PR303.

As shown in Figure 8(a), the impact of random variables' uncertainty on  $p_f$  is obviously different. When  $c$  and  $\varphi$  are independent, the importance orders obtained by the four methods are, respectively,  $\varphi > t > k_h > c > f$ ,  $\varphi > k_h > t > c > f$ ,  $\varphi > t > c > k_h > f$  and  $\varphi > t > c > k_h > f$ . Although the importance orders are not exactly the same, the greatest impact on the failure probability is always  $\varphi$ , and the smallest is  $f$ . When  $c$  and  $\varphi$  are negatively correlated, the importance orders obtained by the four methods are, respectively,  $\varphi > c > t > k_h > f$ ,  $\varphi > c > t > k_h > f$ ,  $\varphi > c > t > f > k_h$  and

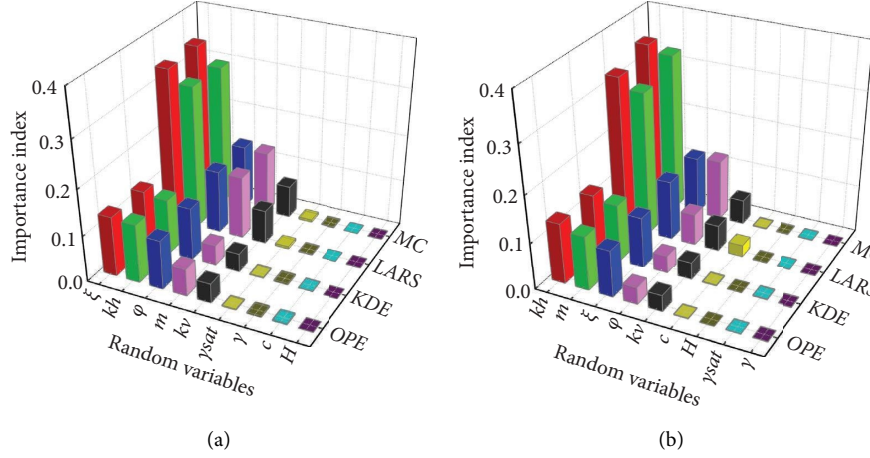


FIGURE 7: Importance indices of the loose deposits landslides along PR303: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

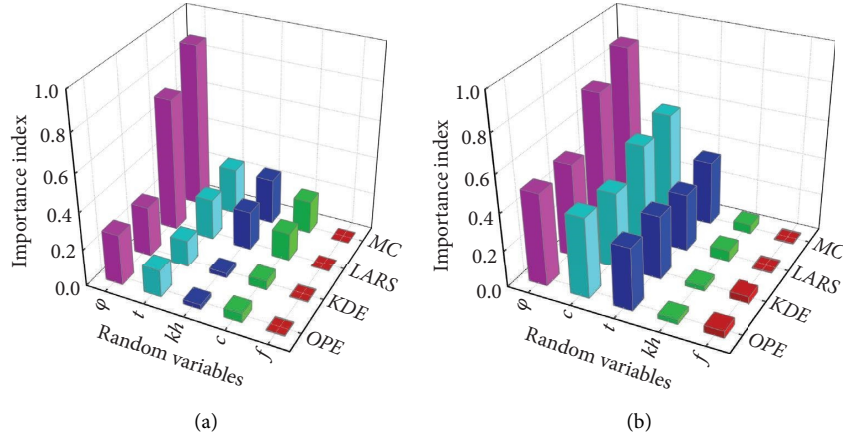


FIGURE 8: Importance indices of the section D0 + 387.50: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

$\varphi > c > t > f > k_h$  (shown in Figure 8(b)). Obviously, the importance orders of the random variables are different when the relationship between  $c$  and  $\varphi$  are different for the slope of the section D0 + 387.50.

The influence of the uncertainty of the random variables on the expressway rock slope is shown in Figure 9. When  $c$  and  $\varphi$  are independent, the importance orders obtained by MC and LARS are consistent and those obtained by KDE and OPE are the same, while there are some differences between MC and KDE, i.e., the importance orders are  $\xi > \varphi > \gamma > H > c$ ,  $\xi > \gamma > \varphi > H > c$ ,  $\xi > \varphi > H > c > \gamma$  and  $\xi > \varphi > H > c > \gamma$ , respectively. In general,  $\xi$  and  $\varphi$  have more impact on  $p_f$ , while  $H$ ,  $c$ , and  $\gamma$  have less impact on  $p_f$ . As shown in Figure 9(b), when  $c$  and  $\varphi$  are negatively correlated, the importance orders are  $\xi > H > \varphi > c > \gamma$ ,  $\xi > \varphi > c > H > \gamma$ ,  $\xi > \varphi > H > c > \gamma$  and  $\xi > \varphi > H > c > \gamma$ , respectively. Compared to Figure 9(a) and 9(b), the importance orders obtained by the four methods still have some differences when the relationship between  $c$  and  $\varphi$  are different for the rock slope of expressway.

## 5. Discussion

In order to compare the differences in the influence of the uncertainty of random variables on  $F_s$  and  $p_f$ , the importance orders of each random variable to  $F_s$  and  $p_f$  are, respectively, listed in Tables 4 and 5.

As shown in Table 4, the importance ranking of the cumulative influence of each variable on  $F_s$  and  $p_f$  is not exactly the same. For the loose accumulation landslides along PR303 (case study 1), when  $c$  and  $\varphi$  are independent, the importance orders based on  $F_s$  and  $p_f$  obtained by MC are, respectively,  $\xi > k_h > m > \varphi > k_v > \gamma_{sat} > \gamma > c > H$  and  $\xi > k_h > \varphi > m > k_v > \gamma_{sat} > \gamma > c > H$ . Where those are, respectively,  $\xi > k_h > m > k_v > \varphi > \gamma > \gamma_{sat} > c > H$  and  $\xi > k_h > m > \varphi > k_v > \gamma_{sat} > c > \gamma > H$  obtained by LARS  $\xi > k_h > m > \varphi > k_v > \gamma_{sat} > \gamma > H > c$  and  $\xi > k_h > \varphi > m > k_v > \gamma > \gamma_{sat} > c > H$  obtained by KDE,  $\xi > k_h > m > \varphi > k_v > \gamma_{sat} > \gamma > c > H$  and  $\xi > k_h > \varphi > m > k_v > \gamma > c > \gamma_{sat} > H$  obtained by OPE. Obviously, the importance ranking of each variable based on  $p_f$  is different from that based on  $F_s$ . Thus,

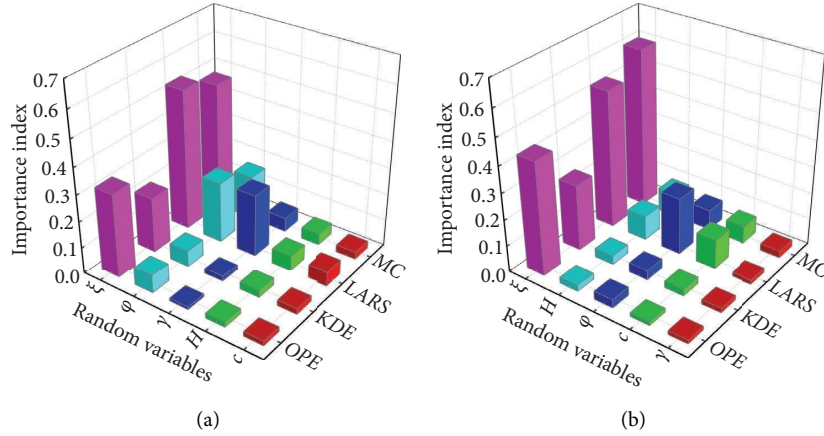


FIGURE 9: Importance indices of the expressway rock slope: (a)  $c$  and  $\varphi$  are independent and (b)  $c$  and  $\varphi$  are negatively correlated.

TABLE 4: Ranking of the influence of random variables on  $F_s$  and  $p_f$  when  $c$  and  $\varphi$  are independent.

Methods	$c$ and $\varphi$ are independent		Case study
	$F_s$	$p_f$	
MC	$\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$	$\xi > k_h > \varphi > m > k_v > \gamma_{\text{sat}} > \gamma > c > H$	Case study 1
LARS	$\xi > k_h > m > k_v > \varphi > \gamma > \gamma_{\text{sat}} > c > H$	$\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > c > \gamma > H$	
KDE	$\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > H > c$	$\xi > k_h > \varphi > m > k_v > \gamma > \gamma_{\text{sat}} > c > H$	
OPE	$\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$	$\xi > k_h > \varphi > m > k_v > \gamma > c > \gamma_{\text{sat}} > H$	
MC	$\varphi > t > c > k_h > f$	$\varphi > t > k_h > c > f$	Case study 2
LARS	$\varphi > t > c > k_h > f$	$\varphi > k_h > t > c > f$	
KDE	$\varphi > t > c > k_h > f$	$\varphi > t > c > k_h > f$	
OPE	$\varphi > t > c > k_h > f$	$\varphi > t > c > k_h > f$	
MC	$\xi > \varphi > H > c > \gamma$	$\xi > \varphi > \gamma > H > c$	Case study 3
LARS	$\xi > \varphi > H > c > \gamma$	$\xi > \gamma > \varphi > H > c$	
KDE	$\xi > \varphi > H > c > \gamma$	$\xi > \varphi > H > c > \gamma$	
OPE	$\xi > \varphi > H > c > \gamma$	$\xi > \varphi > H > c > \gamma$	

TABLE 5: Ranking of the influence of random variables on  $F_s$  and  $p_f$  when  $c$  and  $\varphi$  are negatively correlated.

Methods	$c$ and $\varphi$ are negatively correlated		Case study
	$F_s$	$p_f$	
MC	$k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$	$k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$	Case study 1
LARS	$k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > H > \gamma$	$k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > H > \gamma$	
KDE	$k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > \gamma > H$	$k_h > m > \xi > k_v > \varphi > c > H > \gamma_{\text{sat}} > \gamma$	
OPE	$k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > \gamma > H$	$k_h > m > \xi > k_v > \varphi > c > H > \gamma_{\text{sat}} > \gamma$	
MC	$\varphi > t > k_h > c > f$	$\varphi > c > t > k_h > f$	Case study 2
LARS	$\varphi > t > k_h > c > f$	$\varphi > c > t > k_h > f$	
KDE	$\varphi > t > k_h > c > f$	$\varphi > c > t > f > k_h$	
OPE	$\varphi > t > k_h > c > f$	$\varphi > c > t > f > k_h$	
MC	$\xi > \varphi > c > H > \gamma$	$\xi > H > \varphi > c > \gamma$	Case study 3
LARS	$\xi > \varphi > c > H > \gamma$	$\xi > \varphi > c > H > \gamma$	
KDE	$\xi > \varphi > c > H > \gamma$	$\xi > \varphi > H > c > \gamma$	
OPE	$\xi > \varphi > c > H > \gamma$	$\xi > \varphi > H > c > \gamma$	

the influence of the same variable on the importance of  $F_s$  and  $p_f$  is not consistent.

For the Xiaolangdi Dam slope, when  $c$  and  $\varphi$  are independent, the importance orders based on  $F_s$  obtained by the four methods are consistent, which are  $\varphi > t > c > k_h > f$ , while those are  $\varphi > t > k_h > c > f$  (obtained by MC),

$\varphi > k_h > t > c > f$  (obtained by LARS), and  $\varphi > t > c > k_h > f$  (obtained by KDE and OPE) based on  $p_f$ . For the expressway rock slope, when  $c$  and  $\varphi$  are independent, the importance orders based on  $F_s$  obtained by the four methods are consistent, which are  $\xi > \varphi > H > c > \gamma$ , while those are, respectively,  $\xi > \varphi > \gamma > H > c$ ,  $\xi > \gamma > \varphi > H > c$ ,  $\xi > \varphi > H$

$> c > \gamma$  and  $\xi > \varphi > H > c > \gamma$  based on  $p_f$ . The results of these two case studies indicate that the influence of the random variable on  $F_s$  and  $p_f$  is different.

As shown in Table 5, when  $c$  and  $\varphi$  are negatively correlated, the importance orders based on  $F_s$  and  $p_f$  obtained by MC and LARS are consistent, while those are different obtained by KDE and OPE for the case study 1. Specifically, the orders based on  $F_s$  and  $p_f$  obtained by KDE are, respectively,  $k_h > m > \xi > \varphi > k_v > c > \gamma_{\text{sat}} > \gamma > H$  and  $k_h > m > \xi > k_v > \varphi > c > H > \gamma_{\text{sat}} > \gamma$ . The results of OPE are the same as KDE. It can be seen that the impact of the uncertainty of each random variable on  $F_s$  and  $p_f$  are different for the loose deposits landslides along PR303.

For case study 2, the importance orders for  $F_s$  and  $p_f$  are also different. For example, the importance orders for  $F_s$  obtained by the four methods are consistent, which is  $\varphi > t > k_h > c > f$ , while those are  $\varphi > c > t > k_h > f$  (obtained by MC and LARS),  $\varphi > c > t > f > k_h$  (obtained by KDE and OPE) when  $c$  and  $\varphi$  are negatively correlated. Therefore, it can be drawn that the influence of random variables on  $p_f$  and  $F_s$  is different for the slope of the section D0 + 387.50 slope of Xiaolangdi Dam.

For case study 3, the importance orders for  $F_s$  obtained by the four methods are consistent, which is  $\xi > \varphi > c > H > \gamma$ , while those are  $\xi > H > \varphi > c > \gamma$  (obtained by MC),  $\xi > \varphi > c > H > \gamma$  (obtained by LARS), and  $\xi > \varphi > H > c > \gamma$  (obtained by KDE and OPE) when  $c$  and  $\varphi$  are negatively correlated. Therefore, it indicates that the influence of random variables on  $p_f$  and  $F_s$  is different for the slope of the expressway rock slope.

In summary, the influence of random variables on  $p_f$  and  $F_s$  is different whether the relationship between  $c$  and  $\varphi$  is considered or not. The results obtained by the other three methods have similar characteristics. Therefore,  $F_s$  should not be the only criterion for slope stability.

In addition, while comparing Tables 4 and 5, the importance orders of the random variables are different when the relationship between  $c$  and  $\varphi$  is different. For example, the importance order-based  $F_s$  obtained by MC is  $\xi > k_h > m > \varphi > k_v > \gamma_{\text{sat}} > \gamma > c > H$  when  $c$  and  $\varphi$  are independent in case study 1, while it is  $k_h > m > \xi > \varphi > k_v > c > H > \gamma_{\text{sat}} > \gamma$  when  $c$  and  $\varphi$  are negatively correlated. In case study 2, those are, respectively,  $\varphi > t > c > k_h > f$  and  $\varphi > t > k_h > c > f$  (obtained by MC). In case study 3, those are, respectively,  $\xi > \varphi > H > c > \gamma$  and  $\xi > \varphi > c > H > \gamma$  (obtained by MC). The results obtained by the other three methods are generally consistent, which shows that the relationship between  $c$  and  $\varphi$  will impact the importance of the random variables, and the correlation between  $c$  and  $\varphi$  should not be neglected.

It is pointed out that the probabilistic approaches which can integrate the  $F_s$  with advanced failure probability prediction have seen fast development in recent years. For example, Ji et al. [31] proposed a simplified iterative algorithm for forward/inverse first-order reliability method to perform the geotechnical reliability-based designs of a strip footing and an earth slope. Ji et al. [32] studied the seismic slope failure mechanism of a rotating sliding body to clarify the mechanism of slope movement triggered by earthquake and the

criteria of seismic performance or failure state and proposed a reliability-based design of the allowable displacement method for slope stability analysis. Ji et al. [33] established a modified rotational sliding block model considering depth-dependent shear strength and dynamic yield acceleration, and investigated the influence of slope parameters on the failure probability of seismic slope. In order to improve the efficiency and accuracy of reliability analysis, Ji and Wang [34] developed a modified weighted uniform simulation method for reliability analysis involving nonnormal random variables by adopting Nataf transformation. This paper currently only analyzes the impact of parameter uncertainty on  $F_s$  and  $p_f$ . In the future, further research will be conducted on the impact of other reliability indicators of slope stability.

In addition, more and more computer technologies are used in slope risk assessment, such as machine learning, intelligent optimization algorithms, etc. For example, Ma et al. [35] developed an automated machine learning-based landslide susceptibility mapping (LSM), which provides a high performance solution for machine learning-based LSM. Liu et al. [36] proposed an earthworm optimization algorithm-optimized support vector regression to predict reservoir landslide displacement. Jia et al. [37] developed a multilevel, comprehensive method based on the analytic hierarchy process to evaluate the hazards of ground fissures. Long et al. [38] studied the landslide evolution in the worst-affected area (Mianyuan River Basin) based on supervised classification methods and multitemporal remote sensing images during the decade from 2007 to 2018. These techniques provide more efficient and more convenient methods for slope stability assessment. The follow-up work of this paper will try to introduce machine learning algorithm to analyze the influence of parameter uncertainty on reliability index, in order to provide a more practical method for landslide risk assessment.

## 6. Conclusions

In this paper, the variance-based methods (LARS and MC) and the moment-independent-based methods (KDE and OPE) are, respectively, used to study the impact of random variables on  $F_s$  and  $p_f$ . Three engineering cases have been applied to verify the accuracy and efficacy of those proposed methods. The results obtained by LARS, KDE, and OPE are in good sync with those calculated by the variance-based MC method, which is considered to be an exact solution and is often used to verify other methods. Therefore, the proposed methods are accurate and effective. When  $c$  and  $\varphi$  are independent or correlated, the influence of parameters on  $F_s$  and  $p_f$  are very different, and the importance orders are also obviously different, which indicates that the correlation between  $c$  and  $\varphi$  has a nonnegligible impact on the importance analysis for slope stability. The importance orders based on  $F_s$  and  $p_f$  differ greatly, which indicates that the influence of each random variable on  $F_s$  and  $p_f$  is different. The impact of variables with large value of the importance index should be emphatically considered in the risk assessment of slope stability.  $F_s$  should not be the only criterion in the uncertainty analysis.

## Data Availability

The datasets used and/or analyzed during the current study are available from the corresponding author on reasonable request.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.

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