

# Retraction

# **Retracted: Risk Evaluation Study of Urban Rail Transit Network Based on Entropy-TOPSIS-Coupling Coordination Model**

## **Discrete Dynamics in Nature and Society**

Received 23 January 2024; Accepted 23 January 2024; Published 24 January 2024

Copyright © 2024 Discrete Dynamics in Nature and Society. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

This article has been retracted by Hindawi following an investigation undertaken by the publisher [1]. This investigation has uncovered evidence of one or more of the following indicators of systematic manipulation of the publication process:

- (1) Discrepancies in scope
- (2) Discrepancies in the description of the research reported
- (3) Discrepancies between the availability of data and the research described
- (4) Inappropriate citations
- (5) Incoherent, meaningless and/or irrelevant content included in the article
- (6) Manipulated or compromised peer review

The presence of these indicators undermines our confidence in the integrity of the article's content and we cannot, therefore, vouch for its reliability. Please note that this notice is intended solely to alert readers that the content of this article is unreliable. We have not investigated whether authors were aware of or involved in the systematic manipulation of the publication process.

Wiley and Hindawi regrets that the usual quality checks did not identify these issues before publication and have since put additional measures in place to safeguard research integrity.

We wish to credit our own Research Integrity and Research Publishing teams and anonymous and named external researchers and research integrity experts for contributing to this investigation. The corresponding author, as the representative of all authors, has been given the opportunity to register their agreement or disagreement to this retraction. We have kept a record of any response received.

## References

 F. Gao, Z. Zhang, and M. Shang, "Risk Evaluation Study of Urban Rail Transit Network Based on Entropy-TOPSIS-Coupling Coordination Model," *Discrete Dynamics in Nature and Society*, vol. 2021, Article ID 5124951, 8 pages, 2021.



# Research Article

# **Risk Evaluation Study of Urban Rail Transit Network Based on Entropy-TOPSIS-Coupling Coordination Model**

# Fawen Gao (),<sup>1,2</sup> Zhibin Zhang (),<sup>1</sup> and Mengxing Shang ()<sup>3</sup>

<sup>1</sup>College of Geography and Environmental Science, Northwest Normal University, Lanzhou, China <sup>2</sup>School of Architecture and Urban Planning, Lanzhou Jiaotong University, Lanzhou, China <sup>3</sup>School of Automation and Electrical Engineering, Lanzhou Jiaotong University, Lanzhou 730070, China

Correspondence should be addressed to Fawen Gao; gaofawen@mail.lzjtu.cn and Zhibin Zhang; zbzhang@nwnu.edu.cn

Received 13 November 2021; Revised 29 November 2021; Accepted 7 December 2021; Published 28 December 2021

Academic Editor: Gengxin Sun

Copyright © 2021 Fawen Gao et al. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

As one of the core systems of a city, urban rail transit plays a pivotal role in ensuring the safe, rational, and efficient operation of the city. Therefore, it is of great significance to ensure the safe operation of urban rail transit network to improve the operation efficiency and economic level of the city. The prerequisite to ensure the safety of urban rail transit network is whether the risk situation of urban rail transit network can be reasonably and accurately evaluated. In order to evaluate the risk level of urban rail transit, the risk evaluation system of urban rail transit network was established in this paper based on the three levels of regional economy, social resources, and rail transit. Secondly, based on the entropy-TOPSIS-coupling coordination model, the single-factor influence and multifactor coupling influence in the index system are calculated and analyzed, respectively; thus the coupling coordination degree of urban rail transit system is obtained, so as to quantitatively evaluate and analyze the risk situation in urban rail transit network. Finally, based on the actual data of Shanghai from 2000 to 2016, the case simulation and analysis are carried out. The results show that the two indicators of regional economy and social resources are more likely to affect the safety state of urban rail transit. At the same time, the safety factor of urban rail transit coupling system is increasing year by year and gradually develops from disorder to order. This is more in line with current urban rail transit condition, demonstrating the rationality and accuracy of the entropy-TOPSIS-coupling coordination model proposed in this study.

# 1. Introduction

Urban rail transit is a kind of public transportation that transports a large number of passenger flows in the form of corresponding vehicles through a dedicated track structure, and it occupies a very important position in the urban system. A reasonable and safe urban rail transit network can greatly improve the efficiency and economic level of urban development. The construction of a reasonable and safe urban rail transit network cannot be achieved without an accurate evaluation of the risk of the existing urban rail transit network. Therefore, in order to establish a reasonable risk evaluation system of urban rail transit network, a risk evaluation method of urban rail transit based on the entropy-TOPSIS-coupling coordination model is proposed in this paper, aiming to accurately evaluate the risk situation of urban rail transit network, so as to lay a solid theoretical foundation for optimizing and perfecting urban rail transit network.

Relevant scholars have conducted a series of research on the evaluation of urban rail transit planning and have achieved certain research results. The research content mainly focuses on the exploration, improvement, and optimization of the evaluation model; for example, Yixiu Song [1] used the Analytic Hierarchy Process (AHP) to evaluate the rail transit planning and compared each evaluation index of the transportation planning to obtain its relative importance. Jing Li [2] established a comprehensive evaluation model of traffic network by combining the relative theory of topology and entropy for the shortcomings of the existing urban rail transit network evaluation index system. Chaoxia Su [3] proposed a comprehensive evaluation method of urban traffic network planning and constructed the comprehensive evaluation model of urban rail transit network by fuzzy evaluation method. Yong Jiang [4] believed that the material element analysis model can provide an operable method for VFM evaluation of urban rail transit PPP projects, reduce the subjectivity in the evaluation process, and improve the scientific and reasonable evaluation results. Xin Liu [5] proposed an evaluation model based on the extension cloud theory for the characteristics of urban rail transit safety evaluation, taking advantage of the uncertain reasoning of the cloud model and the quantitative analysis of the extension theory. Xu XD [6] evaluated the potential benefits and limitations of deploying eco-driving strategies on different transit services, service areas, fleet composition, and road terrain. Bin S [7] proposed a quantitative method to evaluate the performance of urban subway network under different damage scenarios. Hy et al. [8] proposed a vague fuzzy matter-element model for the risk assessment of urban rail transit projects by combining vague set and matter-element theory. Hu et al. [9] provided an improved DS/AHP method in this study for the evaluation of hazard source for urban rail transit risk evaluation with incomplete information. Aydin [10] proposed a fuzzy-based multidimensional and multiperiod service quality evaluation outline for rail transit systems. Wang et al. [11] used the grey incidence method for evaluating the hazards of urban rail transit dynamic operating systems and conducting quantitative analysis of risks in the operation process.

At the same time, scholars prefer to use various types of evaluation models in combination, so that the evaluation method is more efficient and reasonable. For example, Ying Wang et al. [12] used AHP method and entropy method to determine index weight and applied TOPSIS method to determine the ideal scheme of line network and selected the optimal scheme by comparing the gap between each scheme and the ideal scheme. Bingyi Qian et al. [13] combined entropy method and expert method to determine the evaluation indexes, combined with TOPSIS method to calculate the pros and cons of each scheme and the optimal solution to determine the optimal scheme, and verified by practical case. Zhifeng Zhou [14] proposed the correlation function as the qualitative index for screening in order to evaluate the service level of transfer stations more reasonably. Ruisong Zhao [15] analyzed the basic form of rail network layout and the suitable form of rail network layout, improved the calculating method of existing rail network scale, and also improved the Analytic Hierarchy Process (AHP) network layout method, established the evaluation index system of line network layout, and constructed the evaluation model. Xie [16] constructed an evaluation model based on ISM-ANP-Fuzzy to evaluate the interface risk in urban rail transit PPP projects. Huang et al. [17] proposed a technique for order preference entropy by similarity to ideal solution (TOPSIS) method to evaluate the operational performance of urban rail transit systems from the perspective of operators, passengers, and government. Wu et al. [18] evaluated the urban rail transit operation safety based

on an improved CRITIC method and cloud model. Bouraima MB [19] used a combined SWOT matrix and Analytic Hierarchy Process (AHP) to evaluate the priority factors and to employ them in developing strategies for the railway transportation system.

Most of the above literature only makes quantitative analysis on the single index factor in the evaluation of urban rail transit; the influence situation and coupling condition between index factors were not calculated and analyzed. Therefore, based on the discussion of the above literature, the entropy-TOPSIS-coupling coordination model evaluation method of urban rail transit is proposed by combining entropy weight method, TOPSIS method, and coupling coordination model. Combined with the relevant traffic system data of Shanghai from 2000 to 2016, the system risk and coordination degree are quantitatively analyzed and comprehensively analyzed, and the development of Shanghai's rail transit system in these ten years is obtained.

#### 2. Identification of Evaluation Index

The evaluation index system of the urban rail transit planning network is the key to measuring the results of the traffic system scheme, as well as an important precondition for picking the most reasonable traffic system scheme. This index system needs to comprehensively reflect the traffic system's economic efficiency, social development, network structure, operation effect, and other rail transit characteristics. Based on an analysis of the related literature's index system, combined with the characteristics of the city and the needs of social development, and in accordance with the principles of strong purpose, hierarchy, science, rationality, ease of operation, and the quantitative and qualitative combination, the evaluation index system of urban rail transit network is constructed in this paper from three aspects of regional economy, social resources, and urban rail transit, as shown in Table 1.

#### 3. Evaluation Modeling

Step 1. Statistical panel data of three potential variables in Shanghai from 2000 to 2016 are defined as *k*th, where *k*th denotes the three subsystems of regional economy (E), social resources (S), and urban rail transit (T), respectively; *k*th is the*k*th second index under the subsystem,  $k = 1, 2, 3, ..., l, l \in N^+$ ; *j*th is the*j*th year to be evaluated,  $j = 1, 2, 3, ..., n, n \in N^+$ . The initial matrix of the subsystem  $X_i = [x_{i,k,i}]_{l \times n}$  is expressed as

$$\mathbf{X}_{i} = \begin{bmatrix} x_{i,k,j} \end{bmatrix}_{l \times n} = \begin{bmatrix} x_{i,1,1} & x_{i,2,1} & x_{i,3,1} & \cdots & x_{i,l,1} \\ x_{i,1,2} & x_{i,2,2} & x_{i,3,2} & \cdots & x_{i,l,2} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ x_{i,1,n} & x_{i,2,n} & x_{i,3,n} & \cdots & x_{i,l,n} \end{bmatrix}.$$
 (1)

Step 2. For each subsystem separately, the entropy weight method is used to calculate the weight of the kth second index in the *j*th time period. The smaller the entropy

Target layer	Criterion layer	Index layer	Description					
	Regional economy	Total GDP (E1) Investment in urban infrastructure (E2) Investment in traffic service (E3)	Annual gross regional product Annual city investment in the engineering and social infrastructure necessary for survival and development Annual investment in necessary tools for transportation, such a machinery and equipment and communication equipment					
		Population density along the rail (E4)	Average number of people per unit area of land along urban rail lines per year					
		Number of hospital beds (S1)	Total number of people using beds in all hospitals within the urban rail system per year					
		Number of park visitors (S2)	Total number of people visiting all parks within the urban rail system per year					
Further of unber wil	Social	Number of mall patrons (S3)	Total number of people patronaging all shopping malls within the urban rail system per year					
Evaluation of urban rail transit systems	resources	Total number of jobs along the rail (S4)	Total number of jobs along urban rail lines that provide money- making opportunities for citizens per year					
		Total number of students enrolled along the rail (S5)	Total number of students enrolled in all schools along the urban rail line per year					
		Building area of houses along the rail (S6)	Total above-ground floor space along urban rail lines per year					
		Urban rail mileage (T1)	Total length of lines in normal operation in the urban rail system					
		Daily average flow of rail transit (T2)	Daily passenger volume of urban rail system					
	Kall transit	Peak hourly cross-sectional flow (T3)	The peak number of passengers passing through each section of the rail line in the same direction per unit time					
		Rail transit share (T4)	The ratio of trips made by urban residents choosing rail transit to total trips					

TABLE 1: System of evaluation indicators for urban rail transit systems.

value, the larger the entropy weight, indicating that the more informative the indicator is, the more important the indicator weight will be. Firstly, the initial matrix is normalized to eliminate the dimension problem, and the normalized matrix  $Y_i = [y_{i,k,j}]_{l \times n}$  of subsystem *i* is formed as follows:

$$y_{i,k,j} = \frac{\left[ \left( x_{i,k,j} \right)_{\max} - x_{i,k,j} \right]}{\left[ \left( x_{i,k,j} \right)_{\max} - \left( x_{i,k,j} \right)_{\min} \right]}, \quad \forall i,k,j,$$
(2)

where  $k^{\text{th}}$  is the value after normalization and  $k^{\text{th}}$  and  $k^{\text{th}}$  are the maximum and minimum values of  $k^{\text{th}}$ , respectively. Calculate the entropy value  $e_{i,k}$  of the  $k^{\text{th}}$  second index under subsystem *i* as follows:

$$e_{i,k} = \frac{1}{\ln n} \sum_{j=1}^{n} f_{i,k,j} \cdot \ln(f_{i,k,j}),$$

$$f_{i,k,j} = \frac{y_{i,k,j}}{\sum_{j=1}^{n} y_{i,k,j}}, \quad \forall i, k, j,$$
(3)

when  $f_{i,j,k} = 0$ ; let  $f_{i,j,k} \times \ln f_{i,j,k} = 0$ . Calculate the entropy weight  $\varpi_{i,k}$  by using the entropy value of the *k*th second index under subsystem *i* as follows:

$$\widehat{\omega}_{i,k} = \frac{\left[1 - e_{i,k}\right]}{\left[l - \sum_{i=1}^{l} e_{i,k}\right]}, \quad \forall i, k,$$
(4)

Step 3. Using the normalization matrix  $Y_i = [y_{i,k,j}]_{l \times n}$  of subsystem *i* and the entropy weights  $\omega_{i,k}$  of the *k*th second index under subsystem *i*, the normalization matrix of the subsystem is weighted as  $U = [u_{i,i}]_{m \times n}$ :

$$u_{i,j} = y_{i,k,j} \times \overline{\mathbb{Q}}_{i,k},$$

$$U = \begin{bmatrix} u_{i,j} \end{bmatrix}_{m \times n} = \begin{bmatrix} u_{1,1} & u_{2,1} & u_{3,1} \\ u_{1,2} & u_{2,2} & u_{3,2} \\ \vdots & \vdots & \vdots \\ u_{1,n} & u_{2,n} & u_{3,n} \end{bmatrix}.$$
(5)

Then the probability of subsystem *i* in the *j*th year is

$$t_{i,j} = \frac{u_{i,j}}{\sum_j u_{i,j}}, \quad \forall i, j.$$
(6)

*Step 4.* Repeat Step 2 and calculate the weight of subsystem *i* for the *j*th time period using the entropy weight method. Form the normalization matrix  $R = [r_{i,j}]_{m \times n}$ 

$$r_{i,j} = \frac{\left[ \left( u_{i,j} \right)_{\max} - u_{i,j} \right]}{\left[ \left( u_{i,j} \right)_{\max} - \left( u_{i,j} \right)_{\min} \right]}, \quad \forall i, j.$$
(7)

Calculate the entropy weight  $\omega_i$  by the entropy value of subsystem *i*:

$$\varpi_i = \frac{\left[1 - e_i\right]}{\left[m - \sum_{i=1}^m e_i\right]}, \quad \forall i.$$
(8)

*Step 5.* Use the TOPSIS method to solve the comprehensive evaluation index  $C_j$  of the urban rail transit system in the *j*th year, first calculating the weighting matrix $O = [o_{i,j}]_{m \times n}$ :

$$o_{i,j} = \varpi_i \times r_{i,j}, \quad \forall i, j.$$
(9)

Determine optimal  $S_i^+$  and inferior solutions  $S_i^-$  for the weighted value of subsystem *i*:

$$S_{i}^{+} = \max(o_{i,1}, o_{i,2}, o_{i,3}, \dots, o_{i,n}), \quad \forall i,$$
  

$$S_{i}^{-} = \min(o_{i,1}, o_{i,2}, o_{i,3}, \dots, o_{i,n}), \quad \forall i.$$
(10)

Calculate the Euclidean distance between the weighted value for the *j*th year and the optimal and inferior solutions:

$$\sup_{j}^{+} = \sqrt{\sum_{i=1}^{m} (S_{i}^{+} - o_{i,j})^{2}}, \quad \forall j,$$

$$\sup_{j}^{-} = \sqrt{\sum_{i=1}^{m} (S_{i}^{-} - o_{i,j})^{2}}, \quad \forall j.$$

$$(11)$$

Calculate the overall evaluation index  $C_j = \text{sep}_j^-/\text{sep}_j^+ + \text{sep}_j^-, \forall j, C_j \in [0, 1]$  of urban rail transit systems for the *j*th year:

$$C_j = \frac{\operatorname{sep}_j^-}{\operatorname{sep}_j^+ + \operatorname{sep}_j^-}, \quad \forall j, C_j \in [0, 1].$$
(12)

Step 6. Calculate coupling  $B_j$  of multiple factors in the *j*th year. The smaller the deviation between the single factors, the greater the coupling among the factors. Calculate deviation  $B_v$  by selecting the formula corresponding to the number of subsystems to be coupled:

$$B_{\nu} = S_i \cdot M \sum t_{i,j} \times \sqrt{2 \left[ 1 - \frac{\sum (t_{i',j} \times t_{i,j})}{M \left( \sum t_{i,j}/M \right)^2} \right]},$$
(13)

where  $S_i$  is the standard deviation of accidents caused by a single factor; M is the number of coupled subsystems to be calculated,  $2 \le M \le 5$ ,  $M \in N^+$ , let  $B' = M \sum (t_{i,j} \times t_{i,j}) / \sum (t_{i,j})^2$ ,  $t_{i,j} \times t_{i,j}$  is the product of the probability of two coupled subsystems, and the larger B', the smaller the deviation. The index is mainly used to evaluate the annual risk coupling strength between the subsystems of urban rail transit coupling model, and at the same time the evaluation results are given to propose decoupling measures. The coupling degree of multifactor risk coupling is calculated by the following formula:

$$B_{j} = \sqrt[M]{\frac{M\sum(t_{i_{j},j} \times t_{i,j})}{\left(\sum t_{i,j}\right)^{2}}}, \quad \forall j.$$
(14)

Step 7. Calculate the comprehensive coordination index  $V_j$  of probability in the *j*th year; this index is mainly used to



FIGURE 1: Entropy-TOPSIS-coupling coordination model flow chart.

evaluate the orderly and disorderly development of urban rail transit system every year. The more orderly the system develops, the more likely it will lead to safety accidents.

$$V_j = \frac{\sum_{i=1}^m \left( t_{i,j} \times \mathfrak{Q}_i \right)}{\sum_{j=1}^n \sum_{i=1}^m \left( t_{i,j} \times \mathfrak{Q}_i \right)}, \quad \forall j.$$
(15)

Step 8. Calculate the coupling coordination degree  $K_j$  of the urban rail transit system in the *j*th year. This indicator comprehensively considers the characteristics of coupling degree and coordination degree and is mainly used to evaluate the annual coupling strength and orderly and disorderly development between subsystems of urban rail transit coupling model. At the same time, the decoupling method is proposed based on the evaluation results.

$$K_j = \left| \sqrt{B_j \times V_j} \right|, \quad \forall j.$$
(16)

The flow chart of the model is shown in Figure 1.

#### 4. Case Study

Using year as the statistical time period, the panel data of three variables of regional economy (E), social resources (S), and urban rail transit (T) in Shanghai from 2000 to 2016 are counted; the results are shown in Table 2 (see Appendix).

The statistical results of Table 2 show that the economic development of the region is rapid and the investment in infrastructure and transport facilities is increasing, and the growth is increasing over time; in addition, the population density is increasing year by year; the number of times or the number of people using social resources is increasing rapidly; the flow of rail

TABLE 2: Initial data on regional economy, social resources, and urban rail transportation in Shanghai,	2000-2016.
TABLE 2: Initial data on regional economy, social resources, and urban rail transportation in	Shanghai,
TABLE 2: Initial data on regional economy, social resources, and urban rail transportation	п.
TABLE 2: Initial data on regional economy, social resources, and urban rail	transportation
TABLE 2: Initial data on regional economy, social resources, and urban	rail
TABLE 2: Initial data on regional economy, social resources, and	urban
TABLE 2: Initial data on regional economy, social resources,	and
TABLE 2: Initial data on regional economy, social	resources,
TABLE 2: Initial data on regional economy	, social
TABLE 2: Initial data on regional e	conomy,
TABLE 2: Initial data on regior	nal e
TABLE 2: Initial data on	region
TABLE 2: Initial data	uo
TABLE 2: Initial	data
TABLE 2: 1	Initial
TABLE .	2:1
	TABLE

	Rail Transit Share (T4)	%	9.6	7	8.8	10	11	22.5	15	18	22.5	32	31.8	34.5	37	38.8	43	46.2	51	
ansit	Peak hourly cross- sectional flow (T3)	Passengers/ h	6232	6912	7580	8080	8392	8861	8948	9026	9745	10268	11056	11274	11910	12501	12842	12956	13041	
Rail tr	Daily average flow of rail transit (T2)	Million passengers/ day	42	80	98	111	131	163	180	223	308.21	361	516	576	622	687	775	841	929	
	Urban rail mileage (T1)	km	62.92	62.92	62.92	108.65	121.23	147.8	169.4	234	264.3	355.05	452.57	454.1	510	528.9	577	588	617	
	Building area of houses along the rail (S6)	hm2	8917	11470	12790	14123	16729	18333	19588	21217	21920	24819	29188	29634	28773	30277	31795	33230	35436	
	Total number of students enrolled along the rail (S5)	Ten thousand	26.01	26.41	27.0125	27.615	28.2175	28.82	29.4225	30.025	30.6275	31.23	32	32.82	33.96	35.45	36.02	36.02	36.38	
esources	Total number of jobs along the rail (S4)	Ten thousand	195.64	202.38	224.1	240.13	244.83	290.53	308.57	355.07	374.57	374	377.81	384.38	390.042	465.74	452.11	438.94	440.19	
Social r	Number of mall patrons (S3)	Person	303690	410220	470640	693240	759972.3	841110	935715	1068480	1210483	1775855	2071563	2121537	2364330	2509020	2690280	2839740	3140250	
	Number of park visitors (S2)	Ten thousand	3.037425	3.378192	3.481151	4.681288	6.586164	6.119151	6.392849	8.024164	10.25247	10.40956	12.08282	10.62455	11.22973	11.05578	11.74501	11.14575	8.887014	Ē
	Number of hospital beds (S1)	Person	1100.933	1141.098	1162.36	1183.371	1292.254	1492.024	1515.009	1557.748	1451.267	1775.846	2015.141	2128.829	2350	2489.731	2566.667	2751.32	3078.676	4-1000399.ht
	Population density along the rail (E4)	Persons/km	1575.13	1594.793	1627.999	1945.152	2262.305	2579.396	2699.295	2793.656	2786.73	2880.225	3606.419	3702.511	3759.09	3817.833	3836.384	3824.635	3830.881	100/20170629/001
economy	Investment in traffic service (E3)	Hundred million	48.83	60.72	63.01	273.77	316.96	385.58	589.52	840.46	838.91	978.24	754.66	595.75	473.43	458.7	422.48	759.23	883.81	://tjj.sh.gov.cn/tj
Regional	Investment in urban infrastructure (E2)	Hundred million	449.9	510.78	583.49	604.62	672.58	885.74	1125.54	1466.33	1733.18	2113.45	1497.46	1157.34	1038.61	1043.31	1057.25	1425.08	1551.87	tij/index.html; httf
	Total GDP (E1)	Hundred million	4771.17	5210.12	5741.03	6694.23	8072.83	9164.1	10366.37	12188.85	14275.8	15285.58	17433.21	19533.84	20553.52	22257.66	24060.87	25643.47	28178.65	w.sh.gov.cn/j
	Year	Year	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	http://ji

TABLE 3: Results of two-factor and three-factor risk coupling calculations.

Year	E-S	E-T	S-T	E-S-T
2000	0.706848266	0.707045225	0.477653744	0.278363504
2001	0.706840272	0.707080423	0.476984636	0.277563834
2002	0.706866093	0.707103581	0.475869973	0.276825274
2003	0.706886642	0.707103555	0.47570298	0.275646204
2004	0.706991312	0.707106312	0.474370109	0.274784144
2005	0.707056031	0.707104543	0.472856308	0.273784565
2006	0.707095162	0.707106271	0.472108388	0.27301559
2007	0.707102599	0.707106736	0.470917514	0.271881172
2008	0.707057535	0.707097484	0.468729786	0.270321168
2009	0.7071	0.707103057	0.471217156	0.268368082
2010	0.707090675	0.707106759	0.470296768	0.26645825
2011	0.707030181	0.70710517	0.468724052	0.265600117
2012	0.707053756	0.707101545	0.46885766	0.264379497
2013	0.706993127	0.707085698	0.467340377	0.263035824
2014	0.706920686	0.707082975	0.466451061	0.261731552
2015	0.706743803	0.707093851	0.465277297	0.260486344
2016	0.706542267	0.707106608	0.464940613	0.25872955

TABLE 4: Integrated coordination of urban rail transit coupled systems, 2000–2016.

Year	Overall coordination value
2000	0.064319499
2001	0.063911727
2002	0.063578293
2003	0.06276528
2004	0.062219223
2005	0.061646665
2006	0.061083937
2007	0.060285252
2008	0.059427307
2009	0.057899301
2010	0.056771151
2011	0.056293734
2012	0.055560615
2013	0.054835764
2014	0.054052972
2015	0.053268746
2016	0.052080534

transport resources, the sharing rate, and other characteristic values are also increasing every year.

Table 3 shows the two-factor and three-factor risk coupling degree; the results show that the coupling degree of E-S and E-T, regional economic and social resources, is larger in the two factors, while the coupling degree of S-T, that is, social resources and rail transit, is small, indicating that regional economic and social resources are easy to cause accidents.

Table 3 shows the two-factor and three-factor risk coupling; its results show that the coupling in E-S as well as E-T, that is, regional economy and social resources, is larger in the twofactor risk, while the coupling in S-T, that is, social resources and rail transportation, is smaller, indicating that both, that is, regional economy and social resources, are prone to accidents.

Using (15) to calculate the integrated coordination of urban rail transit coupled system in Shanghai from 2000

TABLE 5: Results of two-factor and three-factor risk coupling coordination.

Year	E-S	E-T	S-T	E-S-T
2000	0.045464126	0.045476794	0.030722449	0.017904201
2001	0.045175382	0.045190731	0.030484912	0.017739584
2002	0.04494134	0.044956439	0.030255001	0.017600078
2003	0.044367938	0.044381553	0.029857631	0.017301011
2004	0.04398845	0.043995605	0.02951494	0.017096856
2005	0.043587646	0.043590637	0.029150014	0.016877905
2006	0.043192156	0.043192835	0.028838239	0.016676867
2007	0.042627859	0.042628108	0.028389381	0.016390425
2008	0.042018525	0.042020899	0.027855349	0.016064459
2009	0.040940596	0.040940773	0.027283144	0.015538324
2010	0.040142351	0.040143264	0.026699289	0.015127142
2011	0.039801369	0.03980559	0.026386227	0.014951622
2012	0.039284341	0.039286997	0.02605002	0.014689087
2013	0.038768508	0.038773585	0.025626967	0.01442377
2014	0.038211164	0.038219936	0.025213066	0.014147368
2015	0.037647356	0.037666003	0.024784738	0.013875781
2016	0.036797098	0.03682649	0.024214355	0.013474773

to 2016, as shown in Table 4, the integrated system coordination maintains a slowly decreasing trend, indicating that the Shanghai urban rail transit system gradually develops from a disorderly state to an orderly state, and the probability of accidents gradually decreases. This is analyzed because the rapid development of Shanghai brings favorable conditions for the improvement of the safety condition of Shanghai's rail transit system.

The coordination degrees between the two-factor and three-factor risk coupling were measured separately using the evaluation model proposed in Part 2, and the degree of coordination of their evolution toward the common system goal (risk) was further analyzed and evaluated objectively, as shown in Table 5. From Table 5, it can be seen that the two-factor and three-factor risk coupling coordination degrees maintain a steady decreasing trend, which represents a low degree of interaction and synergistic evolution among the factors and a low possibility of risk occurrence in the system. Meanwhile, Table 5 shows that the coupling coordinations of the two-factor E-S as well as E-T, that is regional economy and social resources and regional economy and rail transit, are both larger, while the risk coupling coordination of S-T, that is, social resources and rail transit, is smaller, indicating that both, that is, regional economy and social resources and regional economy and rail transit, are prone to accidents. E-S-T, that is, the smallest risk coupling coordination among the three factors of regional economy, social resources, and rail transportation, indicates that this scenario is the least likely to lead to accidents.

Table 6 shows the annual comprehensive risk index of urban rail transit coupling system based on TOPSIS; the higher the value, the safer the system. The results show that the Shanghai urban rail transit system was the least safe in 2000, and the safety factor of the coupled urban rail transit system is increasing year by year after 2000; that is, the system was gradually safe after 2000.

TABLE 6: Combined risk index and ranking of urban rail transit coupled systems, 2000–2016.

Year	TOPSIS value	Sorted
2000	0	17
2001	0.032291135	16
2002	0.055527455	15
2003	0.122951141	14
2004	0.164184398	13
2005	0.208533961	12
2006	0.255951377	11
2007	0.323101496	10
2008	0.3892544	9
2009	0.521650975	8
2010	0.612688027	7
2011	0.65000222	6
2012	0.709916021	5
2013	0.766845372	4
2014	0.830907081	3
2015	0.896998925	2
2016	1	1

In the end, the range of the evaluation value obtained by the entropy-TOPSIS-coupling coordination model is 1 and the coefficient of variation is 0.718. The larger the range and coefficient of variation, the greater the dispersion and the higher the degree of discrimination of the evaluation value, where the range reaches the maximum. Therefore, the comprehensive evaluation value of the system obtained by the entropy-TOPSIScoupling coordination model evaluation method is more beneficial to visually assess the level of urban rail transit risk evaluation.

#### **5.** Conclusion

- (1) This paper proposes an entropy-TOPSIS-coupling coordination model for urban rail transit by combining the entropy weight method, TOPSIS method, and coupling coordination model. The simulation results show that the risk of urban rail transit system can be reasonably evaluated based on this model, and the conclusions obtained are more in line with the actual situation.
- (2) The following results can be obtained from the relevant data of Shanghai from 2000 to 2016: compared with other factors, regional economic and social resources are more likely to cause accidents, so managers need to focus on these two factors for reasonable control.
- (3) From Table 5, it can be seen that the E-T two-factor coupling coordination degree is the highest in the factor coupling calculation, so managers should try to avoid the coupling condition of regional economic indicators and rail transit indicators.
- (4) From Table 6, it can be seen that the safety factor of urban rail transit coupling system is increasing year by year, gradually developing from disorderly state to orderly state, and the risk is in a gradually increasing situation. Therefore, relevant government

departments should pay attention to the urban rail transit problem and increase the strength of urban rail transit safety construction.

Subsequent improvements to the system can be carried out by decoupling methods, and theoretical approaches and practical implementation schemes to decoupling methods for urban rail transit systems should be studied in depth in the future.

### **Data Availability**

Previously reported data are used to support this study and are cited at relevant places within the text as references.

### **Conflicts of Interest**

The authors declare that there are no conflicts of interest regarding the publication of this paper.

### Acknowledgments

This work was supported by the National Natural Science Foundation of China (Grant no. 41961029) and the Natural Science Foundation of Gansu Province, China (Grant no. 20JR5RA398).

#### References

- Y. Song, "Evaluation of rail transportation planning based on hierarchical analysis," *Modern Transportation Technology*, vol. 8, no. 05, pp. 88–90, 2011.
- [2] Li Jing, H. Mou, and L. Wang, "A comprehensive evaluation of urban rail transit network planning based on physical element entropy weight model," *Journal of Engineering Management*, vol. 27, no. 01, pp. 19–23, 2013.
- [3] C. Su, "Model and method for comprehensive evaluation of urban rail transit line network planning," *Logistics Science and Technology*, vol. 33, no. 06, pp. 143–145, 2010.
- [4] Y. Jiang, Research on VFM Evaluation of Urban Rail Transit PPP Projects Based on Object Element Analysis method, Lanzhou Jiaotong University, Lanzhou, China, 2019.
- [5] X. Liu, "Research on urban rail transit safety evaluation based on game theory," *Science and Technology Innovation*, vol. 23, pp. 138-139, 2017.
- [6] X. D. Xu, H. Y. Li, H. B. Liu, M. O. Rodgers, and R. Guensler, "Evaluation of transit ecodriving in rural suburban, and urban environments," *Transportation Research Record*, vol. 2672, no. 08, pp. 152–164, 2018.
- [7] S. Bin and G. Sun, "Optimal energy resources allocation method of wireless sensor networks for intelligent railway systems," *Sensors*, vol. 20, no. 2, p. 482, 2020.
- [8] A. Hy, B. Cg, and B. He, "Risk assessment for construction of urban rail transit projects," *Safety Science*, vol. 118, pp. 583– 594, 2019.
- [9] X. Hu, X. Li, and Y. Huang, "Urban rail transit risk evaluation with incomplete information," *Procedia Engineering*, vol. 137, pp. 467–477, 2016.
- [10] N. Aydin, "A fuzzy-based multi-dimensional and multi-period service quality evaluation outline for rail transit systems," *Transport Policy*, vol. 55, pp. 87–98, 2017.
- [11] Y. Wang, M. Li, B. Yang, and C. Yang, "An urban rail transit hazard evaluation methodology based on grey system theory,"

*Procedia - Social and Behavioral Sciences*, vol. 43, pp. 764–772, 2012.

- [12] Y. Wang, K. Chen, and Y. Zhou, "Evaluation of rail transit line network based on TOPSIS model," *Highway Transportation Technology*, vol. 32, no. 06, pp. 130–134, 2015.
- [13] B. Qian and L. Zhao, "Evaluation of urban rail transit line network planning scheme based on entropy value method," *Transportation Technology and Economy*, vol. 19, no. 05, pp. 4–8, 2017.
- [14] Z. Zhou, Research on the Evaluation of Service Level of Urban Rail Transit Interchange stations, Shijiazhuang University of Railways, Shaoxing, China, 2020.
- [15] R. Zhao, Research on Urban Rail Transit Line Network Layout and Scheme evaluation, Xi'an University of Architecture and Technology, Xi'an, China, 2018.
- [16] F. Xie, Research on Interface Risk Evaluation of Urban Rail Transit PPP Projects Based on ISM-ANP-Fuzzy, Qingdao University of Technology, Qingdao, China, 2018.
- [17] W. Huang, B. Shuai, Y. Sun, Y. Wang, and E. Antwi, "Using entropy-TOPSIS method to evaluate urban rail transit system operation performance: the China case," *Transportation Research Part A: Policy and Practice*, vol. 111, pp. 292–303, 2018.
- [18] H.-W. Wu, J. Zhen, and J. Zhang, "Urban rail transit operation safety evaluation based on an improved CRITIC method and cloud model," *Journal of Rail Transport Planning & Management*, vol. 16, Article ID 100206, 2020.
- [19] M. B. Bouraima, Y. Qiu, and B. Yusupov, "A study on the development strategy of the railway transportation system in the West African Economic and Monetary Union (WAEMU) based on the SWOT/AHP technique," *Scientific African*, vol. 8, 2020.