Research Article

Operation Control of In Situ Combustion Based on the Material Balance Equation

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The stability of combustion in the process of fire flooding requires not only a reasonable gas injection rate but also a matching exhaust rate. A reasonable injection-production balance system is very important. Based on the material balance of injection-production, the expression of injection-production ratio suitable for normal fire flooding production is established. The air injection rate of fire flooding combustion and oxygen consumption of formation pressurization is analyzed by this formula to calculate the gas production and liquid production in combustion. The reasonable injection and production parameters for the oilfield are calculated by using the oilfield parameters. It can be seen that the calculated value of injection-production ratio is consistent with the actual value, which shows that the injection-production ratio is reasonable and can guide the adjustment of production parameters in the oilfield.

1. Introduction

With the reduction of conventional oil resources, the proportion of low-efficiency reserves and low-grade reserves that are difficult to recover in old oilfields is increasing, and the exploitation of unconventional reservoirs is paid more and more attention in the current situation [1, 2]. Heavy oil reservoir is more difficult to produce than conventional reservoir because of its high viscosity and poor fluidity. Fire flooding is an important development method of heavy oil thermal recovery; how to maintain the stability of combustion is very important for the recovery effect [3, 4]. The design of air injection rate in the fire flooding is usually estimated according to the burning rate, well spacing, and burning scale [5–7]. From the point of view of combustion, a stable combustion needs not only a reasonable gas injection speed but also a matching exhaust speed. Otherwise, the combustion effect will inevitably be affected, and the development effect of fire flooding will be further affected [8–10]. Whether water injection development or air injection development of fire flooding, it is very important to maintain the balance of injection-production in oilfield development [11–14]. A reasonable injection-production balance system can not only meet the need of increasing the formation energy of liquid production but also can not cause the loss of crude oil and reduce the development effect [15–18].

The injection-production balance can be well designed by numerical simulation. As early as 1976, Chien and Shum did the first numerical simulation research in the fire flooding oilfield [19]. In 1979, Grabowski et al. proposed a fully implicit finite-difference thermal recovery model for fire flooding and steam flooding [20]. In 1989, Islam et al. compared and analyzed the previous numerical model of fire flooding and put forward a complete description model [21]. However, the model of numerical simulation technology is difficult to establish and requires many parameters, which is difficult to guide the adjustment of the parameters of the short-term development. In addition to numerical simulation, the design and analysis of the fire flooding mostly adopt empirical formula, with few parameters, easy to use but low accuracy.

The material balance of fire flooding means that under the reasonable injection-production parameters, the injected material and produced material can maintain the dynamic balance state and make the formation pressure rise steadily. Injection-production material is the basis of the system to
maintain the dynamic balance. Considering the role of air in maintaining the combustion of crude oil and increasing formation pressure, the ratio of injected gas to produced gas is obtained in this paper by the principle of material balance, which provides the basis for the operation of fire flooding in the oilfield.

2. Material Transfer in Fire Flooding Process

Taking the gas injection wells, production wells, and reservoir as a unified system, the material transfer of the in situ combustion (ISC) process mainly includes the following parts.

(1) Air injection

The air is injected into reservoirs from the injector. Part of the air is used as an oxidant and combustion improver to participate in the combustion reaction in the underground, and others are used to increase formation pressure.

(2) The flue gas production by the burn of heavy components in crude oil

The composition of heavy component combustion products is very complex, such as hot water, steam, CO₂, a small amount of CO, and unreacted O₂. The combustion reaction exists in the form of a combustion zone in the oil reservoir, which also is called the combustion front.

(3) Production from producer

The heat from combustion, hot water, and hot gas act on the crude oil in front, formed a series of complex oil displacement actions, such as viscosity reduction, expansion, distillation and vaporization, miscible driving, gas drive, and high temperature changing the relative permeability, which causes the fluid substance is produced from the reservoir.

According to the above analysis, the ISC process starts with air injection and ends with the mix produced. The transport process of various materials in the reservoir is as shown in Figure 1.

3. The Balance of Injection-Production Process in Fire Flooding

3.1. Assumption

(1) The reservoirs have been developed by steam stimulation, and there is a large amount of residual oil left in the reservoir. However, the declining of formation pressure is serious, and the formation pressure of the fire flooding process should be gradually recovered

(2) The gas injection wells of fire flooding adopt a row pattern, and the injector-producer ratio is 1 : 1

(3) The formation is in a stable combustion state, regardless of the combustion start-up and breakthrough stage

3.2. The Calculation of the Amount of Air Injection in Stable Combustion

The air injected into the reservoir is used to (1) keep combustion, (2) flooding oil, (3) reservoir pressure build-up, and (4) not participate in the reaction and then be produced.

In the actual production, the amount of air that is not involved in the reaction is very small, so it cannot be considered in the calculation process.

3.3. The Air Required for Oil Combustion

In the actual production of the oilfield, the combustion products are mainly CO₂ and water, and the proportion of CO is very small. In order to simplify the calculation process, the amount of CO is not considered. The high temperature oxidation reaction formula is simplified as formula (1):

\[
\text{CH}_x + (1 + 0.25X)\text{O}_2 \rightarrow \text{CO}_2 + 0.5X \cdot \text{H}_2\text{O}. \tag{1}
\]

Formula (1) shows that \((1 + 0.25X)\)mol oxygen can burn up 1 mol CHx fuel, and the mass of 1 mol CHx is \((12 + X)\)g. When the fuel require \(m_R\) is known, the air requites for completely burning 1 m³ oil sand is as below:

\[
V_R = \frac{112.5m_R}{12 + X} \cdot \frac{\text{Nm}^3(\text{air})}{\text{m}^2(\text{layer})}, \tag{2}
\]

where \(X\) is the apparent atomic H/C ratio, which can be calculated by flue gas.

The air required for combustion is expressed as follows:

\[
V_{\text{air for combustion}} = V_R \cdot S \cdot v \text{ (Nm}^3/\text{d)}, \tag{3}
\]

\(v\) — the velocity of the combustion front (3.8~15.2 cm/d); \(S\) — cross-section area of combustion front, m².

3.4. The Air Required for Oil Displacement

The drop of the formation pressure is mainly caused by the combustion of fuel, the production of oil, and water. The second role of air injection is to supplement formation pressure, and this part of air volume is called the air consumption of the displacement reservoir. In the reservoir conditions, the underground volume of this part of air is equal to the amount of the oil, water, and burned fuel produced every day.

The amount of liquid production is related to the capacity of the liquid supply of the formation. From the theoretical model of “one injector and one producer” and the liquid
production formula, the expression of air consumption of displacement reservoir is shown in formula (4):

\[ V_{\text{driving}} = V_{\text{oil}} + V_{\text{water}} + V_{\text{fuel}}. \]  

(4)

\[ V_{\text{driving}} \]— the air injection rate for displacement oil, m³/day;

\[ V_{\text{oil}} \]— the oil rate, m³/day;

\[ V_{\text{water}} \]— the water rate, m³/day;

\[ V_{\text{fuel}} \]— fuel consumption rate, m³/day.

3.5. The Air Required for Increasing the Reservoir Pressure. The air injected into the formation can make up for the formation pressure loss caused by steam stimulation. In the stable combustion stage, the pressure build-up curve can be approximately simplified to a linear one. The pressure rise rate called \( V_{n} \) (MPa/a) is the slope of that line, and the average reservoir pressure after \( n \) years is:

\[ V_{n} = \frac{p_{r0} + np_{v}}{1 + \frac{p_{v}}{365}} V_{n+1/365}, \]  

(5)

\[ V_{n} \]— gas volume in the reservoir of corresponding years, m³;

\[ V_{n+1/365} \]— gas volume in the reservoir of corresponding years plus one, m³;

\[ \Delta V \]— the amount of air injection for increasing the reservoir pressure, m³/d;

\[ p_{r0} \]— initial average reservoir pressure, MPa;

\[ np_{v} \]— developing years minus one, which is \( n \) years later.

The volume of the air injection has little change after the development period, which can be calculated as follows:

\[ \Delta V = \frac{(p_{r0} + np_{v}) V_{n+1/365}}{p_{r0} + np_{v}} - V_{n}, \]  

(6)

\[ V_{n} \]— the amount of air combustion and oil displacement at \( n \) year, m³/d.

3.6. The Total Air Injection Rate. In the process of combustion, tail gas produced by combustion and most of \( N_{2} \) are used to displace oil and supplement formation energy. Therefore, the total gas injection during fire flooding should be considered comprehensively. In general, the air-oil ratio in the initial stage of the fire flooding is very large, which is more than 3000 Nm³/m³. In the stable period, the air-oil ratio will drop to 500–4000 Nm³/m³. Air injection is sufficient to meet the needs of displacement and pressurization.

\[ G_{\text{air injection}} = V_{\text{air for combustion}}. \]  

(7)

When the reservoir pressure is in serious shortage and more air is needed to supply the pressure of the reservoir, the unreacted \( N_{2} \) and tail gas can continue driving oil and supplying the reservoir energy. The total air injection is as follows:

\[ G_{\text{air injection}} = \frac{0.05X - 0.1m^{3}}{1 + 0.25X - 0.5m^{3}} V_{\text{air for combustion}} + V_{\text{driving}} \]  

(8)

3.7. The Liquid and Gas Production of Fire Flooding

3.7.1. The Liquid Production. Fire flooding development can be regarded as the injection of air from the injector to drive the formation fluid to flow from injector to producer. According to the relationship of reservoirs pressure recovering with time at the underground condition, the liquid-producing capacity in a certain time can be calculated as follows:

\[ N_{\text{liquid}} = \left(1 + \frac{f_{\text{w}}\rho_{\text{o}}}{(1 - f_{\text{w}})\rho_{\text{w}}B_{\text{o}}}\right) V_{\text{oil}}. \]  

(9)

\[ \rho_{\text{w}}, \rho_{\text{o}} \]— density of water and oil, g/cm³;

\[ f_{\text{w}} \]— water cut, %;

\[ B_{\text{o}} \]— volume factor of crude oil;

\[ V_{\text{oil}} \]— the oil production rate, m³/d.

3.7.2. The Gas Production. In the process of fire flooding, the gas produced from the producer mainly consists of steam, \( N_{2}, CO_{2}, CO, \) hydrocarbon gas, and unreacted \( O_{2} \). The main components are \( N_{2} \) and \( CO_{2} \) when the fuel combustion is complete, accounting for more than 95% of the total. In the case of complete combustion, only the output of \( N_{2} \) and \( CO_{2} \) should be considered in the calculation of gas composition.

The consumption of fuel by combustion reaction is 1 m³ per day, so the volume of the gas production underground can be calculated as follows:

\[ G_{\text{gas production}} = \frac{34.822ZRTV_{\text{g}}vS}{p} + \frac{9.375ZRTV_{\text{g}}vS}{(1 + 0.25X)p}, \]  

(10)

\[ S \]— cross-section area of combustion front, m²;

\[ v \]— the velocity of the combustion front, m/d;

\[ Z \]— gas compressibility factor, decimal number;

\[ R \]— universal gas constant;

\[ T \]— reservoir temperature, K;

\[ P \]— average reservoir pressure, MPa;

\[ N \]— developing years minus one, which is \( n \) years later.

3.8. The Injection-Production Ratio. The injection-production ratio (IPR) usually represents the material balance of injection-production in water flooding and reflects the relationship between water injection and fluid production.
IPR is an extremely important parameter in the oilfield development process and is closely related to other parameters such as production rate and water cut. The reasonable control of IPR is an important task in the oilfield. According to the material balance, the reasonable IPR value is close to 1.

The conventional water flooding IPR can be expressed as follows:

$$\text{IPR} = \frac{W_f}{N_p B_o + N_p WOR}.$$  \hspace{1cm} (11)

In the fire flooding, the main injection gas is air, and the productions include oil, gas, and water. Therefore, IPR can be expressed as follows:

$$\text{IPR}_{fl} = \frac{G_{\text{air injection}}}{(G_{\text{gas production})}} = \left(\frac{p_o + n p_w + \left(p_f/365\right) p_o + n p_w}{(1 + f_w p_o/(1 - f_w)p_o B_o)}\right) \left(2 \pi k h \left[p_o + p_w\left(n + 1/365\right) - p_{wfr}\right] PR/\mu_o \ln (R_f/R_w)\right) \times 86.4 \times \left(-1.898V_R S/(1 + 0.25X) V_M p_o \right) \times 10^{-3} + \left(m_{rfl} S/\rho_{cok}\right) + \left(44.643ZRT V_R S/(p_{wfr} + p_t\left(n + 1/365\right))\right) \times 10^6 \right) + \left(34.822 ZRT V_R S(p_o - p_w\left(n\right) \times 10^6) + (9.375 ZRT V_R S(1 + 0.25X)/(p_{wfr} + p_w\left(n\right) \times 10^6)\right),\hspace{1cm} (13)

IPR<sub>fl</sub>—gas injection-production ratio in fire flooding;

- \(p_o\)—the rate of formation pressure recovery MPa/y;
- \(m\)—production-injection rate in fire flooding;
- \(S\)—the cross-section area of combustion surface;
- \(V_M\)—molar volume of gases, \(22.4 \times 10^{-3}\) m<sup>3</sup>/mol;
- \(P_{wfr}\)—bottom-hole pressure;
- \(k\)—permeability, \(\mu m^2\);
- \(h\)—thickness of oil layer, m;
- \(p_w\) and \(p_o\)—water density and oil density, g/cm<sup>3</sup>;
- \(\rho_{cok}\)—fuel density, kg/m<sup>3</sup>;
- \(PR\)—productivity ratio;
- \(\mu\)—viscosity of underground crude oil, mPa·s;
- \(R_f, R_w\)—well diameter, supply radius, m.

Formula (13) is suitable for a stable combustion period in the development of conventional dry combustion, and the oxygen content is less than 1% in flue gas, which is high-temperature oxidation (HTO) mode in the reservoir.

The reasonable ranges of injection-production ratio, air injection, and gas production can be reached through the above formula (13). And different parameters in oilfield production can be modified by means of the theoretical data to make the combustion process work stable and effective.

4. The Application of Material Balance Equation in an Oilfield

4.1. The Introduction of Reservoir G3. The reservoir G3, which is located in Bohai Bay Basin in China, is a heavy oil reservoir. The producer-injector ratio is 21:8 in fire flooding pilot G3. The G3 block was put into development in 1987. After two stages of conventional exploitation and steam stimulation, the recovery percent of the block reached 16.45% at the end of 2007, and the formation pressure is only 2 MPa. The water sensitivity of the reservoir is changed from medium to strong, and the underground water storage is large. The heat loss is large, and the heat utilization rate is low, when hot water flooding and steam flooding are used. Therefore, fire flooding is adopted to replace development.

The wellhead gas injection pressure is 1.7~5.2 MPa at the beginning of fire flooding and decreases to 1.5~3.2 MPa after half a year. With the extension of gas injection time and the increase of cumulative gas injection volume, the injection pressure began to rise slowly. At present, the injection pressure is 3.4~4.7 MPa and shows an upward trend. In the gas produced from production wells and observation wells, the content of O<sub>2</sub> is very low, which is 0% when the combustion is good. The highest content of CO<sub>2</sub> is 25%, generally 10% to 20%, and the CO content is generally 1% to 2%. At present, 13 ignition well groups have been formed in the fire flooding development of the block, with a daily oil increase of 51.9 t and an annual oil increase of 1.89 × 10<sup>4</sup> t. The basic data is shown in Table 1.

Taking \(n = 5\) as an example, in the sixth year of the development, the gas IPR is 1.12 when the velocity of the combustion front is 8 cm/d.

4.2. Sensitivity Analysis of ISC Parameters

4.2.1. The Effects of Vertical Sweep Efficiency and the Combustion Front Width. The average combustion front
Table 1: Basic data of reservoir G3.

<table>
<thead>
<tr>
<th>Reservoir parameters</th>
<th>Fluid parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Permeability, ×10(^{-3}) (\mu)m(^2)</td>
<td>6113</td>
</tr>
<tr>
<td>Water cut, %</td>
<td>60</td>
</tr>
<tr>
<td>Initial average reservoir pressure, MPa</td>
<td>3.5</td>
</tr>
<tr>
<td>Approximate bottom hole flowing pressure, MPa</td>
<td>2.5</td>
</tr>
<tr>
<td>Effective thickness, m</td>
<td>62.7</td>
</tr>
<tr>
<td>Rate of pressure recovery, MPa/a</td>
<td>0.12</td>
</tr>
<tr>
<td>Supply radius, m</td>
<td>105</td>
</tr>
<tr>
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<td>62.7</td>
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<td>105</td>
</tr>
</tbody>
</table>

The consumption of fuel \(M_r = 22.07 \text{ kg/m}^3\) is calculated by oil density in reservoir G3. So when the fuel is \(M_r\), the air consumption for complete combustion \(1 \text{ m}^3\) (every cubic meter fuel) oil sand is as \(V_R = 266.02 \text{ Nm}^3/\text{m}^3\).

4.2.2. The Effects of the Build-Up of the Reservoir Pressure.

The liquid production rate, gas injection, and production are affected by reservoir pressure. While the first, sixth, and eleventh year in the fire flooding process, the relationship between the gas IPR and velocity of combustion front is shown in Figure 3.

In general, with the increase of development time, formation pressure will be build-up and the liquid production rate will increase. Figure 3 shows that with the increase of development time, the gas IPR increases, and the numerical range of gas IPR increases gradually.

4.2.3. The Effects of Oxygen Utilization.

If the flue gas contains a higher proportion of oxygen, the combustion reaction will change to low-temperature oxidation (LTO) mode, and some of the air mixtures flow through the formation without participating in any chemical reaction. Therefore, this partial
gas can be added to the numerator and denominator of the IPR formula for the analysis. When the oxygen content is 0%, 2%, and 5% in flue gas, the effect of oxygen utilization on gas IPR is as shown in Figure 4.

As shown in Figure 4, incomplete combustion will cause IPR decline, but the range of theoretical value is less affected. Actually, the change of IPR is the result of the multiple parameters in oilfield production. In order to make the IPR fluctuate within a larger range, it is necessary to analyze the geological parameters, the perforation, and the fluid properties in that reservoir, and use the IPR formula to optimize the fire flooding process.

5. Conclusions

(1) With the increase of the cross-section area of the combustion surface, the gas IPR becomes steady. Increasing the length of the perforation and optimizing the well section position of perforation can improve vertical sweep efficiency in the injection well, thus keeping the cross-section area of combustion surface in high level, and decrease the diversity of the combustion front.

(2) Since the IPR formula created on the water cut is known, the water cut is a variable during the fire flooding process. In addition, the oxygen utilization has a great influence on IPR; both parameters must be monitored in real-time.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there is no conflict of interest regarding the publication of this paper.

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