Research Article

Probabilistic Evaluation of Hydraulic Fracture Performance Using Ensemble Machine Learning

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Evaluation of hydraulic fracture (HF) performances is critical to develop unconventional resources such as tight oil and gas. We present a probabilistic evaluation approach that integrates ensemble machine learning with Monte Carlo simulation. In the method, we employ the ensemble learning to develop a predictive model between well productivity and its influential factors including both geological properties and HF treatment parameters. Next, coupling the built prediction model with Monte Carlo simulation, an empirical cumulative probability distribution of the well productivity is generated. The well HF performance is assessed by estimating its cumulative probability value. The proposed method is applied to evaluate the HF performances in a developed block of the eastern Sulige region. The study shows that 19% of the wells were fractured with good quality and 55% of the wells were fractured with average quality, while the rest were stimulated with poor quality. The evaluations provide a guideline for optimization of HF designs of wells that have not been hydraulically stimulated in the region.

1. Introduction

Tight sand gas has become a new exploration target and important source of natural gas supply in China [1–6]. Sulige gas field, located in the central part of the Ordos Basin, is the largest tight gas field with estimated gas reserves of 18.85 Tcf in China [7–9]. The eastern Sulige is one of the main regions of natural gas exploration and development in the gas field [10, 11]. Due to the low quality of rock properties such as permeability and porosity in the gas-bearing formations, hydraulic fracturing stimulations were carried out so that natural gas can be produced economically from the tight formation.

The hydraulic fracturing is a process which injects large amounts of water, proppants (sand), and additives via a wellbore at high pressure into the low permeable formations to break rock and create cracks (hydraulic fractures). The injected proppants keep fractures open [12–14]. These fractures could extend several hundred feet away the wellbore and form high permeable flow paths, which ease the natural gas flow from the tight formation toward the wellbore and enhance the gas recovery. In the past several years, hundreds of wells were hydraulically stimulated and put on production in the eastern Sulige region. However, the significant differences in the gas production have exhibited in the fractured wells [15]. To further develop the gas field, it is necessary to evaluate the hydraulic fracture performances and to identify the best hydraulic fracturing practices to maximize the well gas production in the field.

Upon completing of a HF job, well production performance such as absolute open flow potential (AOFP) or cumulative gas production is employed as an indicator for the hydraulic fracture performance of the well. The well production performance is controlled by multiple variables. In this work, we consider geological properties and fracturing treatment parameters. The geological properties include gas saturation, pay thickness, porosity, matrix permeability, and presence of nature fractures. The treatment parameters mainly contain fluid injection volumes, injection rates and pressure, and proppant volumes, which influence fracture geometries. To conduct the performance evaluation, it is essential to build a predictive model to quantify the well
production performance with these influential factors. A numerical reservoir simulator is usually employed to build such model by simulating natural gas flow in both tight matrix and the fractures [16–19]. However, the accuracy of the hydrocarbon production predictions highly relies on the characterization of the tight gas reservoirs and representation of induced fracture geometry. Due to limited formation data and subsurface complexities, it is impossible to quantify the properties precisely. Meanwhile, the underlying flow mechanism is so complex in the tight formations that multiple simplified assumptions have been made in the mechanistic modelling [20]. These challenges have made that the estimated hydrocarbon production from the reservoir simulations often differs from actual production data [21]. In addition, the numerical simulation runs are computationally intensive by solving large partial deferential equations and make them unfeasible for the probabilistic evaluation of the HF performance, where hundreds of simulations are often required. Numerous data have been collected from various sources and available in the eastern Sulige region. A machine learning method could provide potential solutions to overcome the drawbacks.

In recent years, the machine learning method has become a powerful tool for predicting the production performance. For instance, Nejad et al. [22] developed a neural network model to examine the effect of the completion and fracture treatment designs on gas production in the Eagle Ford Shale. Mohaghegh [23] proposed the concept of shale analytics to describe the applications of artificial intelligence to shale gas development. The shale analytics was applied to investigate how different reservoir and completion parameters affect gas production in several shale plays of the United States. Montgomery and O’Sullivan [24] developed a spatial error model and regression-Kriging to forecast tight oil production using a large well dataset from the Williston Basin in North Dakota. Wang and Chen [25] investigated the performances of four machine-learning algorithms in forecasting first-year oil production of Montney tight reservoirs and concluded that random forest outperformed other algorithms. Porras et al. [26] developed a random forest model to predict first-year oil production using geological and completion design parameters. The developed model was used to evaluate hydraulic fracture performance of the horizontal wells in the Viking Formation, Canada. Although the machine learning techniques have shown promising results in the production prediction in the above studies, these studies did not consider the uncertainties related to the complexities of the HF process. The quantification of these uncertainties can provide valuable information to assess the HF performances.

In this study, we develop a probabilistic approach to evaluate the HF performance. Our approach integrates ensemble learning with Monte Carlo simulations to consider the uncertainties caused by the HF treatment complexities. The approach was inspired by Mohaghegh’s combination of neural networks and the Monte Carlo simulations [23]. We applied the developed approach to obtain an empirical cumulative probability distribution of the well productivity. The well HF performance is assessed by estimating its probability value.

2. Methodology

The probabilistic evaluation workflow of the HF performance consists of four main steps, as shown in Figure 1.

(Step 1) Data collection: collect raw data from a database. The independent variables include geological properties and hydraulic fracturing treatment parameters. The target variable represents post-treatment well production performance.

(Step 2) Data preprocessing: make raw data ready for building a predictive model. The data preprocessing is composed of two parts: data cleaning and feature selection.

(Step 3) Ensemble learning: build a model to predict the well production performance using ensemble machine learning.

(Step 4) Probabilistic evaluation: combine the predictive model with the Monte Carlo simulation to assess the HF performance.

2.1. Data Collection and Preprocessing. We extracted 743 vertical fractured wells from a private database. These wells were chosen without missing values and from the same developed block in the eastern Sulige. As one of China’s natural gas development key areas, the eastern Sulige gas field stretches from the Ordos district in the Inner Mongolia Autonomous Region to the Yulin district of Shaanxi province in China. The reservoir rocks of the gas field mainly consist of the Upper Paleozoic fluvial and deltaic sands [27]. The main gas-producing layers are Permian-age Shihezi formation, Shanxi formation, Benxi formation, and
Majiagou formation. The 8th member of Shihezi formation (He8) is one of the most gas productive zones with formation thickness between 45 m and 60 m. The average depth of the tight formations in the study area ranges from 2300 m to 3800 m. The reservoir porosity ranges from 5% to 15%, and the matrix permeability varies from 0.5 to 20 mD [28]. The multistage hydraulic fractured wells have been applied recently in the field. However, the fractured wells could only keep stable gas production for 1 to 1.5 years; then the production declined rapidly. Therefore, the gas flow rates were allocated properly to maintain a relatively long stable production [30].

For each vertical well, there are twelve variables listed in Table 1. The target variable is absolute open flow potential (AOFP) to quantify the hydraulic fracture performance. The number of independent variables is eleven. Two kinds of independent variables are identified the most important to the production performance of hydraulically fractured wells: geological properties and HF treatment parameters. The geological properties include formation thickness, true vertical depth (TVD), porosity, matrix permeability, and gas saturation. The HF treatment parameters such as fluid volumes, injection rates, and pressure determine a fracture geometry and conductivity, which play an important role in natural gas flow.

<table>
<thead>
<tr>
<th>Type</th>
<th>Parameters</th>
<th>Unit</th>
<th>Abbreviation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Geological properties</td>
<td>Formation thickness</td>
<td>m</td>
<td>TH</td>
</tr>
<tr>
<td></td>
<td>Well true vertical depth</td>
<td>m</td>
<td>TVD</td>
</tr>
<tr>
<td></td>
<td>Formation porosity</td>
<td>%</td>
<td>PO</td>
</tr>
<tr>
<td></td>
<td>Matrix permeability</td>
<td>mD</td>
<td>PERM</td>
</tr>
<tr>
<td></td>
<td>Gas saturation</td>
<td>%</td>
<td>SG</td>
</tr>
<tr>
<td></td>
<td>Pad fluid volume</td>
<td>m³</td>
<td>PFV</td>
</tr>
<tr>
<td></td>
<td>Slurry fluid volume</td>
<td>m³</td>
<td>SFV</td>
</tr>
<tr>
<td></td>
<td>Proppant fluid ratio</td>
<td>%</td>
<td>PFR</td>
</tr>
<tr>
<td>Fracture treatment</td>
<td>Total fluid volume</td>
<td>m³</td>
<td>TFV</td>
</tr>
<tr>
<td></td>
<td>Average injection rate</td>
<td>m³/min</td>
<td>AIR</td>
</tr>
<tr>
<td></td>
<td>Average injection pressure</td>
<td>MPa</td>
<td>AIP</td>
</tr>
<tr>
<td>Production</td>
<td>Absolute open flow potential</td>
<td>10⁴m³/day</td>
<td>AOFP</td>
</tr>
</tbody>
</table>

**Table 1: Lists of modelling variables.**

**Figure 2: Probabilistic evaluation of a fractured well through obtaining cumulative probability distribution of AOFP (modified from [23])**
The collected raw data usually include missing data, incorrect formats, and abnormal data, and the direct usage of the raw data affects later predictive modelling. Data preprocessing is employed to solve the issues, which mainly includes data cleaning, data transformation, and feature selection, which are described in Section 3.

2.2. Ensemble Learning. The ensemble learning method is an advancement in machine learning technique by building multiple learners and combining the outputs of these learners to obtain robust predictions [31]. It has been confirmed that the ensemble learner has better performances than a single learner and has already been applied in many regression and classification problems [32]. Boosting is one of effective ensemble learning methods. Friedman [33, 34] regarded the boosting as the optimization of a loss function and introduced the concept of gradient boosting.

Gradient boosting decision trees (GBDT) is an ensemble algorithm to combine many decision tree models, where each tree is built to minimize the residual error of the previous tree iteratively. The final prediction is integrated from the outputs of all trees. The GBDT algorithm is described briefly as follows.

Assuming that $x$ is a set of features (geological properties and HF treatment parameters) and $F_M(x)$ is a predicted function of the target variable $y$ (absolute open flow potential). Given training data set $T = \{(x_1, y_1), (x_2, y_2), \ldots, (x_N, y_N)\}$, a GBDT model $F_M(x)$ is built as the summation of $M$ additive functions $f_m(x)$ based on decision trees $t(x; \mu_m)$ [35, 36]:

$$F_M(x) = \sum_{m=1}^{M} f_m(x) = \sum_{m=1}^{M} \theta_m t(x; \mu_m), \quad (1)$$

The histograms of the main variables are shown in Figure 3.}

**Figure 3: Histograms of the main variables.**
where $\mu_m$ is the mean of split locations and the terminal nodes of a tree $t(x; \mu_m)$ and $\theta_m$ is estimated by minimizing a specified loss function $L(y, F(x)) = (y - F(x))^2$:

$$f_0(x) = y = \arg\min_y \sum_{i=1}^{N} L(y, y). \quad (2)$$

The number of iteration $m$ starts from 1 to $M$, and negative gradient $g_{im}$ in the current prediction model is calculated by

$$g_{im} = -\frac{\partial L(y, F(x))}{\partial f(x)}|_{f(x) = f_{m-1}(x)} \quad (3)$$

The tree $t(x; \mu_m)$ is used to approximate the negative gradient, and a descent step size $\theta_m$ is computed by

$$\theta_m = \arg\min \sum_{i=1}^{N} L(y, F_{m-1}(x_i) + \theta t(x; \mu_m)). \quad (4)$$
The model is updated based on Equations (2)–(4):

\[ F(x) = F_{m-1}(x) + \Theta_m I(x; \mu_m). \]

The GBDT has a few advantages, including the ability to cope with skewed variables, computational robustness, and high scalability [37]. More details of the algorithm can be found from Zhu et al. [27].

2.3. Probabilistic Evaluation. Due to the complexity of hydraulic fracturing process, the production prediction has some uncertainty, which strongly affects the HF performance evaluation.

Monte Carlo simulations can be used to quantify the prediction uncertainty by estimating an empirical cumulative probability distribution of the well productivity instead of a determined value. As shown in Figure 2, we fixed the values of the geological properties of a selected well and assumed the fracture treatment parameters as random variables to follow a certain probability distribution such as triangular or Gaussian or uniform. The ranges, means, and variances of these distributions are estimated from the dataset. We run the predictive model thousands of times by randomly sampling from the given distributions. At the end of the runs, an empirical cumulative probability distribution of the selected well AOPF is generated. Through the probability distribution, the HF performance of the well could be evaluated by estimating its probability value. The details are described in the next section.

### Table 3: Optimal hyperparameter values of the GBDT.

<table>
<thead>
<tr>
<th>Hyperparameter</th>
<th>Name</th>
<th>Ranges</th>
<th>Optimal values</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of trees</td>
<td>N_estimators</td>
<td>1–200</td>
<td>110</td>
</tr>
<tr>
<td>Max. depth</td>
<td>max_depth</td>
<td>2–8</td>
<td>3</td>
</tr>
<tr>
<td>No. of features to split</td>
<td>max_features</td>
<td>sqrt; auto</td>
<td>sqrt</td>
</tr>
<tr>
<td>Min. number of samples</td>
<td>min_samples_split</td>
<td>2–12</td>
<td>4</td>
</tr>
<tr>
<td>Learning rate</td>
<td>learning_rate</td>
<td>0.08–0.13</td>
<td>0.11</td>
</tr>
</tbody>
</table>

### Table 4: Properties of well Sudong42-48.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Formation thickness (m)</td>
<td>17.2</td>
</tr>
<tr>
<td>True vertical depth (m)</td>
<td>3138.9</td>
</tr>
<tr>
<td>Formation porosity (%)</td>
<td>7.2</td>
</tr>
<tr>
<td>Matrix permeability (mD)</td>
<td>0.4</td>
</tr>
<tr>
<td>Gas saturation (%)</td>
<td>54.3</td>
</tr>
<tr>
<td>Pad fluid volume (m³)</td>
<td>425</td>
</tr>
<tr>
<td>Slurry fluid volume (m³)</td>
<td>380</td>
</tr>
<tr>
<td>Proppant fluid ratio (%)</td>
<td>9.7</td>
</tr>
<tr>
<td>Injection rate (m³/min)</td>
<td>3.5</td>
</tr>
<tr>
<td>Injection pressure (MPa)</td>
<td>67.5</td>
</tr>
<tr>
<td>Absolute open flow (10⁴ m³/day)</td>
<td>8.5</td>
</tr>
</tbody>
</table>

![Figure 5: Relative variable importance.](image)

![Figure 6: Comparison of actual and predicted AOPF for training and test data.](image)
3. Results

3.1. Outlier Removal. Figure 3 displays the presence of outliers through histograms of the main input variables. The outliers in the data are circled in black for the variables. We also applied Rosner’s test to verify the outliers identified in the histograms [38]. A total of 39 wells with the outliers were detected from the dataset and removed. 704 wells were kept to the following predictive modelling.

Table 2 summarizes the range and statistical properties of the independent and dependent variables. The absolute open flow potential per well ranges from 0.4 to 21.5 \(10^4 \text{ m}^3/\text{day}\), averaging \(5.5 \times 10^4 \text{ m}^3/\text{day}\). The total injection fluid volume and proppant fluid ratio per well are averaged to be 589.7 \(\text{m}^3\) (27.4\%), respectively.

3.2. Correlation Analysis. Figure 4 shows the Pearson covariance matrix to quantify the degree of linear correlation among the variables. It is noted that all treatment parameters have a positive correlation with the well productivity (AOFP). The increasing in the fracturing fluid volumes enlarges the reservoir stimulated zones, which creates more contact area between the wellbore and reservoir. As expected, there is the multicollinearity among the pad fluid volume (PFV), slurry fluid volume (SFV), and total fluid volume (TFV) since total fluid volume consists of the pad fluid volume and slurry fluid volume. Therefore, the total fluid volume will be dropped in the following predictive modelling. In addition, the geological properties also have a positive correlation with the AOFP. The formation thickness has the largest value of the Pearson coefficient. More sophisticated feature selection methods including stepwise regression and recursive feature elimination are being investigated.

3.3. Production Forecasting. The 704 wells in the dataset were split into training and test data sets in the ratio of 80:20. The main hyperparameters for a GBDT model include learning rate, number of trees, minimum number of samples required at a leaf node, maximum depth, and number of features for the best split. The hyperparameter tuning were performed on the training data using grid searching combined with five-fold cross-validation (CV). The optimal hyperparameter values are listed in Table 3.

Figure 5 shows the results of the relative importance of 10 input variables on the AOFP. The formation thickness and proppant fluid ratio are two most important variables, followed by the pad fluid volume and matrix permeability. The variable importance indicts that the formation thickness has a significant impact on the well productivity. Therefore, when fracturing a gas well, we need to evaluate its formation thickness and matrix permeability. In terms of the fracturing operation, we may add more proppant to enhance the fracture conductivity and increase the pad fluid volume to improve the fracturing effectiveness.

Figure 6 compares the actual and predicted AOFP for the training and test data sets using the built GBDT model. In the figure, the data points are grouped along the 45-degree straight line, and the values of coefficient of determination \(R^2\) for the training and test data set are calculated to be 0.91 and 0.74, respectively. The results show that the predicted AOFP have a good match with the actual AOFP values for both the training and test data sets, which indicates the developed AOFP forecasting model is robust for the evaluation of the hydraulic fracture performance.

3.4. Well Hydraulic Performance Evaluation. We choose well Sudong42-48 to assess its hydraulic fracturing performance as an example. Table 4 shows the input variable and AOFP values of this well.

We fixed the values of the geological properties of this well and assumed the fracture treatment parameters as random variables to follow a certain probability distribution such as triangular or Gaussian or uniform. We run the predictive model thousands of times by sampling the treatment
Table 5: Evaluation criteria.

<table>
<thead>
<tr>
<th>Hydraulic fracture performance</th>
<th>Cumulative probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>Good</td>
<td>&gt;0.6</td>
</tr>
<tr>
<td>Fair</td>
<td>[0.3, 0.6]</td>
</tr>
<tr>
<td>Poor</td>
<td>&lt;0.3</td>
</tr>
</tbody>
</table>

Figure 8: Evaluation results of hydraulic fracture performance in the block of the eastern Sulige region.

parameters from the given distributions. An estimated AOFP was obtained from each run. At the end of the runs, a histogram and empirical cumulative probability distribution of the selected well were generated as shown in Figure 7. The well hydraulic performance is assessed by estimating its cumulative probability based on its AOFP, as shown in Figure 7. The well AOFP is $8.5 \times 10^9$ m$^3$/day, which is marked as a filling circle in the x-axis. The corresponding cumulative probability is 0.18 to determine the hydraulic fracturing performance. The hydraulic fracturing quality of this well was classified as “poor” according to the evaluation criteria given in Table 5 because its cumulative probability value is less than 0.3. Taking the same evaluation process, we have assessed the hydraulic fracturing performances of other vertical wells in the developed block of the eastern Sulige region.

From the variable importance analysis, the proppant fluid ratio (FPR) is the most influential factor among the fracture treatment parameters. If we increased FPR value from 9.7% (original) to 23%, the well productivity was increased by 29%, and the hydraulic fracturing quality of this well could be classified as “Fair.” Therefore, the evaluation is useful to optimize the HF treatment.

We performed the assessments for all 704 fractured wells. The evaluation results of the block are shown in Figure 8. 54.6% of the wells in the block have been fractured with “Fair” quality, 26.4% wells with “Poor” quality, and only 19% wells with “Good” quality. The results indicate that the better HF designs are required to improve the HF performances in the gas field.

4. Conclusions

In the paper, we have developed a probabilistic workflow to assess the hydraulic fracture performance by integrating the ensemble learning with the Monte Carlo simulation. Using the data from a developed block in the eastern Sulige region, we have applied the workflow to evaluate the hydraulic fracture performance of the wells.

(1) The absolute open flow potential is regarded as the response variable, while ten geological and fracture treatment parameters are chosen as the input variables.

(2) An ensemble learning model is built to quantify complex relationship between the geological properties, treatment parameters, and the absolute open flow potential. Results indicate that the formation thickness has the most important effect on the well productivity, followed by the proppant fluid ratio.

(3) Among 704 fractured vertical wells, 19% of the wells have been stimulated with “Good” quality, 54.6% of the wells with “Fair” quality, and 26.4% wells with “Poor” quality.

(4) The proposed workflow could be applied to evaluate other well stimulation performances such as multi-stage hydraulic fracturing in horizontal wells or acid fracturing.

Data Availability

Data is available upon request.

Conflicts of Interest

The authors declare no conflict of interest.

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