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Research Article

Cascaded Fractional-Order Controller-Based Load Frequency Regulation for Diverse Multigeneration Sources Incorporated with Nuclear Power Plant

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To sustain a system frequency within acceptable limits, it is widely conceded that retaining a power balance between generation and demand is necessary. In order to regulate the frequency of power systems (PSs) this article proposes a novel cascaded based fractional-order controller termed as fractional-order integer- (FOI-) fractional-order proportional integral with double derivative (FOPIDD2). In addition to redox flow batteries and capacitive energy storage, the recommended control strategy has been validated with gas, thermal reheat, hydro, and nuclear power systems. Additionally, a newly designed algorithm known as squid game optimizer (SGO) optimizes the gains of the new FOI-FOPIDD2 controller. The squid game optimizer technique is inspired by the fundamental principles of a conventional Korean sport. It employs a population of candidate solutions and iteratively adjusts the control parameters to discover the optimal set that reduces frequency abnormalities and improves system stability. A comparison is also made between the controller's performance and benchmarks, including the jellyfish search algorithm, the firefly algorithm, the grey wolf optimizer, and the particle swarm algorithm. The proposed algorithms reduced peak overshoot as compared to grey wolf optimizer algorithm by 35.34%, 46.78%, and 76.89%; jellyfish search optimization algorithm by 34.76%, 77.22%, and 82.56%; and firefly algorithm by 82.67%, 89.23%, and 29.67% for frequency variations in area 1, area 2 and tie line power, respectively. Furthermore, SGO-FOI-FOPIDD2 controllers under different loading circumstances and conditions were evaluated and endorsed for their ability to withstand uncertainties in power system parameters.

1. Introduction

The modern interconnected power system (IPS) is designed with several control regions linked by tie lines. The daily energy demand is increasing as the world's population grows. Inconsistencies in load demand cause irregularities in both frequency and tie line power flow within the IPS's control zones. In order to overcome this challenge within the existing power system framework, load frequency regu-

lators play an important role in balancing power consumption and generation [1, 2]. Both primary and secondary mechanisms play an important role in controlling frequency fluctuations. A governor uses a control method to alter the speed and frequency of basic control processes [3]. However, after considerable deviations, supplementary control is required to stabilize frequency. The secondary controller, therefore, is of greater importance to the overall performance of the system [4].

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1.1. Literature Survey. The principal aim of load frequency control (LFC)/automatic generation control (AGC) is to regulate the power deviation between adjacent regions linked by tie lines within defined boundaries and maintain the system frequency within predetermined limits [5]. In the early stages of control scheme development for AGC, conventional controllers such as integral (I), proportional integral (PI), and PI derivative (D) were utilized. Researchers preferred these controllers due to their adaptability and simplicity; nevertheless, the outcomes frequently failed to meet expectations in terms of performance [6, 7]. For instance, in [8] proposed PID controller optimized with ant colony optimization (ACO) for single-area nuclear power system. The authors in reference [9] proposed PI controller to address the LFC problem in a single-area scenario incorporated with renewable energy resources. Researchers extended their investigations to tackle the LFC challenges arising in interconnected PSs. The researchers in [10] introduced an ACO algorithm for the purpose of optimizing the PID controller of a two-area interconnected nonreheat thermal power system with nonlinearity caused by governor dead band (GDB). Jagatheesan et al. in [11] proposed PI-based fuzzy logic controller for the frequency regulation of interconnected hydropower system incorporated with GDB as well as GRC nonlinearities. Apart from the conventional power systems, various researchers have worked in a deregulated power system by designing various types of controllers to regulate the frequency [12, 13].

Various control mechanisms have been introduced in PSs to address the issue of load frequency management. A few examples include model predictive control [14], robust sliding mode controllers [15], artificial intelligence-based LFC approach [16], linear matrix inequality [17], resilient control methodologies [18], data-driven controllers [19], fuzzy logic control (FLC) [20, 21], and robust virtual inertia control [22]. To control the frequency of connected PSs, the classic PID controller has been the principal focus of academic research because of its ease of use and low cost. Even yet, the PID controller has a difficult time adapting to nonlinear properties and interruptions in the system by trial and error. To determine the best PID values, a considerable amount of effort has been expended. Due to advances in computing power that enable simulation and accurate implementation of the fractional-order controller, the use of fractional-based controllers has recently drawn more attention in power engineering issues, specifically for power optimization control. The FOPID and their modification have been utilized in [23-25] as a secondary LFC to improve the frequency stability of the interconnected two region power systems. Numerous cascaded controller forms [26-28] have been used to improve frequency persistence in PSs. Recent research [29, 30] has investigated a second method for studying LFC that emphasizes the integration of two controllers. The frequency variations of a two-area coupled PS can be diminished using a PIDD2 controller framework, which was also proposed by authors in [31]. Moreover, references [32, 33] recommended the integral-(I-) tilt derivative (TD) and fractional-order (FO) I-TD controller for system frequency adaptation, respectively. The frequency effectiveness of the ID-T controller is superior to that of the TID controller [34].

There is numerous research in the literature that use fractional calculus to solve classical PID controller [35, 36]. According to previous research, FOPID and PIDD2 controllers can surpass PID controllers in numerous engineering applications in addition to the LFC system. To improve the control performance of LFC systems, an upgraded controller must be developed. As a result, for the first time, we proposed a cascaded based FOI-FOPIDD2 controller to enhance LFC transient and dynamic performance. The suggested controller can be viewed as a hybrid of fractional calculus and PIDD2.

Research has shown that selecting the controller type is just as important as choosing the controller settings. By utilizing evolutionary optimization to optimize controller parameters, the frequency stability problem has been greatly improved. New sophisticated methods are employed to adjust the controller coefficients to overcome the complexity of the control methods. For example, the researchers used the self-tuned algorithm (STA) [37], marine predator optimization algorithm (MPA) [38], chaos game optimization (CGO) [39], modified multiverse optimizer [40], improved based fitness-dependent optimizer [41], equilibrium optimizer hybridized with slime mould optimization algorithm [42], artificial ecosystem optimization (AEO) [43], sunflower optimization [44], butterfly optimization algorithm (BOA) [45], smell agent optimization (SAO) [46], pathfinder optimizer algorithm (PFA) [47], mine blast algorithm (MBA) [48], Fox optimizer algorithm (FOA) [49], and socialspider optimizer [50]. According to research [51], the TID with filter (TIDF) configured with DE outperformed the I/ PI/PID controller. Similarly, in reference [52], the water cycle algorithm- (WCA-) tuned modified TID controller functioned more efficiently than PID/TID controllers.

This study is aimed at obtaining the right knobs for the recommended controller by developing a new metaheuristic algorithm called the squid game optimizer (SGO) technique, which is inspired by the fundamentals of a traditional Korean sport. During the squid game, attackers strive to reach their target, whereas players attempt to eradicate one another. It is typically acted on broad, open grounds with no predetermined extent and dimension limitations. Based on historical records, the playing area for this sport is commonly devised in a design resembling a squid and appears to be approximately half the dimensions of a standard basketball court. First, the numerical model of this approach is built by selecting the best nominee solutions and selecting an initialization method at random. In two groups, solution candidates move among defensive players, initiating a fight that is replicated by random movement towards defensive players. The position update procedure is completed, and the current position vectors are formed by judging the winner declarations of the players on opposite sides. These states are estimated based on the cost function. Twenty-five (25) unrestricted mathematical assessment functions are applied to examine the performance of the presented SGO algorithm, along with six others that regularly used metaheuristics for assessment

TABLE 1: List of nomenclature and notations.

| Acronym | Definition |
|------------------|--|
| IPS | Interconnected power system |
| SGO | Squid game optimizer |
| AVR | Automatic voltage regulator |
| FA | Firefly algorithm |
| JSO | Jellyfish swarm optimization |
| SLP | Step load perturbation |
| PSO | Particle swarm optimization |
| ΔF | Frequency variation |
| PID | Proportional integral derivative |
| WCA | Water cycle algorithm |
| PIDD2 | Proportional integral with double derivative |
| PIDF | Proportional-integral-derivative filter |
| ITAE | Integral time absolute error |
| CES | Capacitive energy storage |
| TIDN | Tilt integral derivative with filter |
| TF | Transfer function |
| FO | Fractional order |
| FLC | Fuzzy logic controller |
| PSO | Particle swarm optimization |
| TD | Time delay |
| RFB | Redox flow battery |
| $T_{\rm re}$ | Time constant for reheat turbine |
| $K_{ m g}$ | Participation factor for gas |
| BDG | Biodiesel generator |
| K_{b} | Participation factor for hydro |
| CF | Cost function |
| β | Frequency bias factor |
| AGC | Automatic generation control |
| BES | Battery energy storage |
| ESS | Energy storage system |
| ITSE | Integral time square error |
| ΔPD | Load deviation |
| R | Speed regulation |
| ΔPG | Output deviation of a generator |
| FA | Firefly algorithm |
| Тр | Time constant of power system |
| $O_{ m sh}$ | Overshoot |
| $U_{ m sh}$ | Undershoot |
| Kp | |
| - | Gain of power system |
| M | Inertia constant |
| ST | Settling time |
| JSO | Jellyfish search optimization |
| H | Power system gain |
| HMG | Hybrid microgrid |
| MG | Microgrid |
| U_{b} | Upper boundary |
| ΔXG | Valve position of governor |

TABLE 1: Continued.

| Acronym | Definition |
|-------------------|---|
| ITSE | Integral time square error |
| $L_{\rm b}$ | Lower boundary |
| $T_{ m w}$ | Wind time constant |
| $T_{\rm cr}$ | Combustion reaction time delay |
| X | Speed governor lead time constant |
| a, b, c | Constants of valve positioner |
| $G_{ m N}$ | Participation factor for nuclear plant |
| K_{re} | Gain of reheat steam turbine |
| PS | Power system |
| Tw | Time constant for water |
| TCD | Compressor discharge volume time constant |
| a_{12} | Area size ratio |
| Y | Speed governor lag time constant |
| LFC | Load frequency control |
| BD | Boiler dynamics |

[53]. Furthermore, the suggested SGO's capability is evaluated using advanced real-real-life challenges on the latest CEC, such as CEC 2020, with the SGO demonstrating remarkable results in haggling with these inspiring optimization challenges [53].

In addition, the primary conclusion drawn from the available literature is that LFC methods, such as FLC, Hinfinite approaches, and model predictive control, which rely on the controller designer's imagination to achieve the desired performance, accomplish that despite numerous design flaws and a lengthy setup process. In addition, conventional PD/PI/PID controllers struggle with responding to uncertainty in the system. The impact of system nonlinearities and boundary fluctuations on robustness evaluations has been underexplored in several earlier works. Most previous evaluations also ignored the significant integration of energy storage devices (ESD) without adjusting system parameters due to the included system nonlinearities/uncertainties and immediate demand variations. The list of nomenclature and notations is shown in Table 1.

- 1.2. Contribution of the Paper. This research proposes a novel FOI-FOPIDD2 controller that improves system frequency steadiness as accounting for perturbations affected by diverse power sources. In accord with the SGO, the settings for the suggested FOI-FOPIDD2 controller have also been established to guarantee frequency and system constancy under atypical conditions. The main contribution of the paper is summarized as follows, in contrast to earlier studies on related subjects:
 - (i) Employing a reliable FOI-FOPIDD2 controller to enhance frequency reliability for dual zone coupled

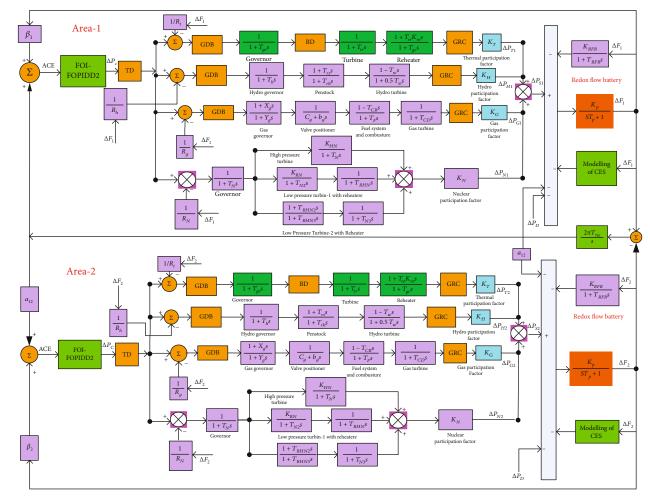


FIGURE 1: Dynamic modelling of the proposed PS.

power systems amalgamated with capacitor energy storage, hydro, nuclear, reheat thermal, gas, and redox flow battery

- (ii) In order to refine the knobs of the presented FOI-FOPIDD2 controller, a novel strong algorithm termed as squid game optimizer (SGO) algorithm is presented for the diverse interconnected hybrid power systems
- (iii) To validate the dominance of the proposed FOI-FOPIDD2 controller over the existing FOPID/PID/PIDD2 controller
- (iv) The diverse hybrid power systems have been analyzed with the inclusion of various nonlinearities including time delay (TD), generation rate constraints (GRC), boiler dynamics (BD), and governor dead zone (GDB) to make the system realistic
- (v) Exhibiting the supremacy of the SGO over other existing algorithms, such as the particle swarm optimization (PSO) algorithm, grey wolf optimizer

- (GWO), jellyfish swarm optimization (JSO), and firefly algorithm (FA)
- (vi) Examine the robustness and stability of the proposed controller under extensive variation of the power system parameters and loads

2. Modelling of Hybrid Power System

In this portion, a dual area PS that is combined with reheat thermal, nuclear, gas, hydro, capacitor energy storage, and redox flow battery is mathematically modeled which is shown in Figure 1. The schematic diagram is shown in Figure 2. The distribution of all the included power generations between the two regions is assumed to be equal. The PS material from [24, 41, 54] is used to construct the system in Simulink/MATLAB and is available in Table 2. For the thermal system, the GRC of 10%/min is considered for both rising and dropping rates. Growing generation is utilized into consideration for the hydro portion at a typical GRC of 270%/min, while decreasing generation is considered into action at a regular GRC of

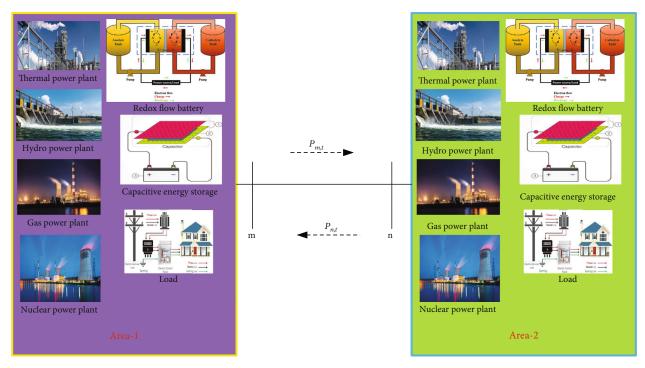


FIGURE 2: Schematic diagram of the proposed PS.

360%/min [12]. The mathematical formulation for GDB is described below [55].

$$GDB = \frac{N_1 + sN_2}{sT_{sq} + 1},\tag{1}$$

where $N_1 = 0.8$ and

$$N_2 = \frac{-0.2}{\pi} \,. \tag{2}$$

Furthermore, a time delay (TD) of 2 seconds is inserted after the controller design to make the arrangement more realistic, which is given in equation (3). Similarly, a boiler dynamic is added as a nonlinearity into the thermal reheat system, and their schematic type is shown in Figure 3. The mathematical representation for the proposed boiler dynamics is also given in equation (4) [12, 55]. The area control error (ACE) for multigeneration unit is given in equation (5).

$$T_f(s) = \frac{e^{-t_d(s)}}{sT+1},$$
 (3)

$$T_{\text{cpu}}(s) = \frac{K_{1b}(I + sT_{1b})(1 + sT_{rb})}{(1 + 0.1T_{rb}s)s},$$
(4)

$$ACE = \beta_i \Delta F_i + \Delta P tie_{ij}, \quad i \neq j.$$
 (5)

2.1. Modelling of Reheat Thermal, Hydro, Nuclear, and Gas Power Plants. Conventional power systems comprised of reheat thermal (with submodel of governor/turbine/reheater) and hydropower generation (with submodel of governor/pen-

stock/droop compensation). The mathematical descriptions for reheating thermal structure with their subsequent submodel including (governor/turbine/reheater) are shown in the below equations, respectively [24, 28].

$$G_{G}(s) = \frac{1}{sT_{gr} + 1},$$

$$G_{T}(s) = \frac{1}{sT_{tr} + 1},$$

$$G_{R}(s) = \frac{1 + T_{re}K_{re}s}{sT_{re} + 1},$$

$$G_{RT}(s) = \frac{1 + T_{re}K_{re}s}{(sT_{re} + 1)(sT_{gr} + 1)(sT_{tr} + 1)}.$$
(6)

The mathematical representations for hydroelectric power with their subsequent submodel including governor/penstock/droop compensation are shown in the below equations, respectively [45, 55].

$$\begin{split} G_{\rm HG}(s) &= \frac{1}{sT_{\rm h}+1}, \\ G_{\rm HT}(s) &= \frac{1+T_{\rm rs}s}{sT_{\rm rh}+1}, \\ G_{\rm HD}(s) &= \frac{1-T_{\rm w}s}{0.5T_{\rm w}s+1}, \\ G_{\rm H}(s) &= \frac{(1-T_{\rm w}s)(1+T_{\rm rs}s)}{(sT_{\rm h}+1)(1+0.5T_{\rm w}s)(sT_{\rm rh}+1)} \,. \end{split} \tag{7}$$

 K_{1b}

Table 2: [25, 41, 55, 57, 58].

| LFC model | | | |
|---|------------------------|--------------------|----------------------|
| T_{ps1} | 11.49 | K_{ps1} | 68.97 Hz/p.u. MW |
| $R_{\rm h}=R_{\rm t}=R_{\rm g}=R_{\rm N}$ | 2.4 Hz/p.u. MW | K_{ps2} | 68.97 Hz/p.u. MW |
| $T_{\rm ps2}$ | 11.49 | $oldsymbol{eta}_1$ | 0.4312 Hz/p.u. MW |
| R_{T} | 2.4 | eta_2 | 0.4312 Hz/p.u. MW |
| $T_{ m tie}$ | 0.0866 p.u. MW/ rad | | |

Parameters and their values for hydropower system, reheat thermal, hydro nuclear, CES, and RFB

| $T_{ m gr}$ | 0.08 sec | $T_{ m tr}$ | 0.3 sec |
|---------------------------------------|------------|--------------------|------------|
| $T_{\rm re}$ | 10 sec | $K_{\rm re}$ | 0.3 |
| $T_{ m h}$ | 0.3 sec | $T_{\rm rs}$ | 5 sec |
| $T_{ m rh}$ | 28.75 sec | $T_{ m w}$ | 0.0235 sec |
| K_{T} | 0.5 | T_{CR} | 0.01 sec |
| $C_{\rm g},c_{\rm g2}$ | 1 | $T_{ m F}$ | 5 |
| b_{g1} , b_{g2} | 0.05 | T_{CD} | 0.2 sec |
| $X_{ m g}$ | 0.6 | Y_{g} | 1 |
| $T_{ m N}$ | 0.05 | K_{G} | 0.25 |
| $K_{ m RN}$ | 0.2 | a_{12} | -1 |
| $T_{ m N2}$ | 0.25 | K_{H} | 0.25 |
| $T_{ m RHN}$ | 10 sec | T_{T} | 0.3 sec |
| $T_{ m RHN2}$ | 10 sec | $K_{ m RFB}$ | 0.6 |
| $T_{ m RHN3}$ | 0.25 | $K_{ m N}$ | 0.25 |
| $T_{ m N3}$ | 0.05 sec | T_{CES} | 0.046 sec |
| K_{CES} | 0.3 | T_2 | 0.029 sec |
| T_1 | 0.280 sec | T_4 | 0.39 sec |
| T_3 | 0.0411 sec | | |
| Boiler dynamic | | | |
| K_3 | 0.92 | $C_{\rm b}$ | 200 |
| $T_{ m f}$ | 0.23 | $T_{ m rb}$ | 0.545 |
| $T_{ m rh}$ | 28.75 | $T_{\rm r}$ | 1.4 |
| K_2 | 0.095 | K_1 | 0.85 |
| | | | |

The nuclear power plant model consists of a governor, two low-pressure turbines (LPT), and a high-pressure turbine (HPT) shown in Figure 4. Equations (8)–(11) represent the transfer functions (TFs) of the governor, HPT turbine with reheater, LPT-1 with reheater, and LPT-2 with reheater, respectively [56, 57].

0.950

$$G_{\rm N}(s) = \frac{1}{sT_{\rm N} + 1},$$
 (8)

 T_{1b}

0.545

$$G_{\rm HP}(s) = \frac{K_{\rm HN}}{sT_{\rm N1} + 1},$$
 (9)

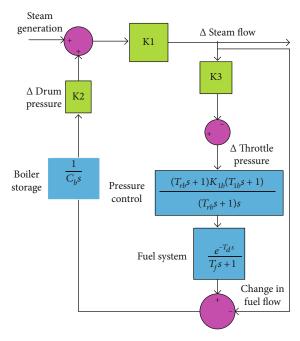


FIGURE 3: Schematic pattern of boiler dynamics.

$$G_{\text{LP1}}(s) = \frac{K_{\text{RN}}}{(sT_{\text{N2}} + 1)(sT_{\text{RHN1}} + 1)},$$
 (10)

$$G_{\rm LP1}(s) = \frac{(sT_{\rm RHN2} + 1)}{(sT_{\rm N3} + 1)(sT_{\rm RHN3} + 1)}. \tag{11}$$

The transfer functions (TFs) of the gas generation system, which includes the fuel system with combustor ($G_{\rm GC}(s)$), gas turbine ($G_{\rm GT}(s)$), (GFC), gas governor ($G_{\rm GG}(s)$), and valve positioner ($G_{\rm GV}(s)$) are expressed by [49, 57]

$$G_{GC}(s) = \frac{(1 - sT_{CR})}{(sT_F + 1)},$$

$$G_{GT}(s) = \frac{1}{(sT_{CD} + 1)},$$

$$G_{GG}(s) = \frac{(1 + sX_g)}{(sY_g + 1)},$$

$$G_{GV}(s) = \frac{1}{(sb_g + C_g)}.$$
(12)

2.2. Capacitive Energy Storage (CES) Modeling. Due to its ability to rapidly charge and discharge with a substantial amount of power, capacitive energy storage devices are growing in favor of modern power systems [58]. The benefit of CES is that it responds to a boost in demand by producing an abundance of electricity. It is affordable and easy to use. It has a long service life and does not perform worse for it. A supercapacitor [59] serves as the CES system's main energy storage factor. Capacitor plates are utilized for retaining energy in the form of static charge. CES emits energy back into the grid when demand is at

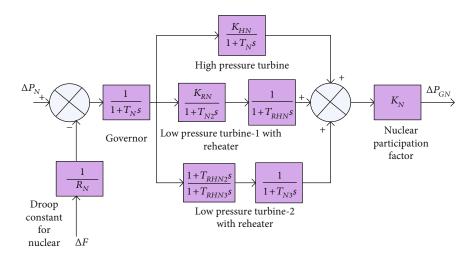


FIGURE 4: Transfer function model of nuclear power plant.

its highest. The modification in CES's incremental power is represented by [59]

$$\Delta P_{\text{CES}} = \left[\frac{K_{\text{CES}}}{(sT_{\text{CES}} + 1)} \right] \left[\frac{1 + sT_1}{(sT_2 + 1)} \right] \left[\frac{1 + sT_3}{(sT_4 + 1)} \right] \Delta F, \quad (13)$$

where T_1 – T_4 stand for the two-stage phase compensation blocks' time constants. Both analyzed PSs have incorporated CES scoring into their repertoires. The input control signal for each CES unit is the phase shift in frequency between two areas of the PS. The TF model of CES is shown in Figure 5.

2.3. Modelling of Redox Flow Battery (RFB). RFB has become prevalent as a quick-rechargeable battery in recent times. An electrochemical transformation process is utilized in the redox progression, and a dual converter manages the rectifier and inverter functions. The benefit of the RFB is its rapid storage operation, which minimizes the impact on the environment by addressing the governor response delay and eliminating oscillations. RFB is made up of electrolyte, pumps, pipes, tanks, flow cells, and other modules that store energy during charging and release it under load demand [60, 61]. RFB can function at room temperature and is suitable for power ratings between kW and MW with storage durations of 2 to 10 hours [62]. Its control response time to frequency variations is particularly quick [63]. The key features that set RFB apart as an excellent ESD are its flexible power capability, low environmental effect, high efficiency, and versatility. Equation (14) shows the RBF transfer function [60, 61].

$$G_{\text{RFB}}(s) = \frac{K_{\text{RFB}}}{(sT_{\text{RFB}} + 1)}.$$
 (14)

3. Squid Game Optimize

The proposed SGO algorithm is offered as a unique metaheuristic approach prompted by the basic rules of a tradi-

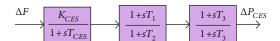


FIGURE 5: TF model of CES.

tional Korean sport. During the squid game, attackers strive to reach their target, whereas players attempt to eradicate one another. It is typically acted on broad, open grounds with no predetermined extent and dimension limitations. Based on historical records, the playing area for this sport is commonly devised in a design resembling a squid and appears to be approximately half the dimensions of a standard basketball court. First, the numerical model of this approach is built by selecting the best nominee solutions and selecting an initialization method at random. In two groups, solution candidates move among defensive players, initiating a fight that is replicated by random movement towards defensive players. The position update procedure is completed, and the current position vectors are formed by judging the winner declarations of the players on opposite sides. These states are estimated based on the cost function. Twenty-five (25) unrestricted mathematical assessment functions are applied to examine the performance of the presented SGO algorithm, along with six others that regularly used metaheuristics for assessment [53]. Furthermore, the suggested SGO's capability is evaluated using advanced real-real-life challenges on the latest CEC, such as CEC 2020, with the SGO demonstrating remarkable results in haggling with these inspiring optimization challenges [53]. SGO algorithms consist of the following steps [53].

3.1. Mathematical Formulation. In this section, the numerical description of the SGO method is considered employing the squid game strategy. The initialization technique is executed as follows in the initial step, with the search space treated as a specific area of the playing field and

the prospective contenders (X_i) supposed to be players [53]:

$$X = \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_i \\ \vdots \\ X_n \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j \cdots x_1^d \\ x_2^1 x_2^2 \cdots x_2^j \cdots x_2^d \\ \cdots \ddots \vdots \\ x_i^1 x_i^2 \cdots x_i^j \cdots x_i^d \\ \vdots \\ x_n^1 x_n^2 \cdots x_n^j \cdots x_n^d \end{bmatrix}, \begin{cases} i = 1, 2, \dots m, \\ j = 1, 2, \dots m, \\ j = 1, 2, \dots m, \end{cases}$$
(15)

$$x_i^j = x_{i,\text{Min}}^j + \text{rand.}\left(x_{i,\text{Max}}^j - x_{i,\text{Min}}^j\right), \quad \begin{cases} i = 1, 2, \dots, n, \\ j = 1, 2, \dots, d. \end{cases}$$

$$(16)$$

Here, "n" signifies the overall count of players within the field, which corresponds to the search space. "d" denotes the dimensionality of the problem at hand. The initial position of the ith candidate is influenced by the i th decision variable, represented as x_i^j . The upper and lower bounds of the jth variable are termed as $x_{i,\mathrm{Max}}^j$ and $x_{i,\text{Min}}^{j}$, respectively. The random number, denoted as "rand," follows a uniform distribution between 0 and 1. In the second phase of the algorithm, players are categorized into two equal-sized groups known as defensives (Def) and offensives (Off). Below is an algebraic depiction of these elements [53].

$$X^{\text{off}} = \begin{bmatrix} X_{1}^{\text{off}} \\ X_{2}^{\text{off}} \\ \vdots \\ X_{i}^{\text{off}} \\ \vdots \\ X_{m}^{\text{off}} \end{bmatrix} = \begin{bmatrix} x_{1}^{1}x_{1}^{2} \cdots x_{1}^{j} \cdots x_{1}^{d} \\ x_{2}^{1}x_{2}^{2} \cdots x_{2}^{j} \cdots x_{2}^{d} \\ \vdots \\ x_{i}^{1}x_{i}^{2} \cdots x_{i}^{j} \cdots x_{i}^{d} \\ \vdots \\ x_{m}^{1}x_{m}^{2} \cdots x_{m}^{j} \cdots x_{m}^{d} \end{bmatrix}, \begin{cases} i = 1, 2, \dots \dots m, \\ j = 1, 2, \dots \dots d, \end{cases}$$

$$X^{\text{Def}} = \begin{bmatrix} X_{1}^{\text{Def}} \\ X_{2}^{\text{Def}} \\ \vdots \\ X_{i}^{\text{Def}} \end{bmatrix} = \begin{bmatrix} x_{1}^{1}x_{1}^{2} \cdots x_{1}^{j} \cdots x_{m}^{d} \\ x_{2}^{1}x_{2}^{2} \cdots x_{2}^{j} \cdots x_{2}^{d} \\ \vdots \\ x_{i}^{1}x_{i}^{2} \cdots x_{i}^{j} \cdots x_{i}^{d} \\ \vdots \\ x_{m}^{1}x_{m}^{2} \cdots x_{m}^{j} \cdots x_{m}^{d} \end{bmatrix}, \begin{cases} i = 1, 2, \dots \dots m, \\ j = 1, 2, \dots \dots d. \end{cases}$$

$$\begin{cases} i = 1, 2, \dots \dots m, \\ j = 1, 2, \dots \dots d. \end{cases}$$

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Here, "m" represents the total count of players within each game group. The ith offensive player is denoted as X_i^{off} , and the kth defensive player is represented as X_i^{Def} . Once the game starts, an offensive player maneuvers among the defensive players to initiate a confrontation. It is important to highlight that each attacking player is constrained to move and engage in battle using a single foot, whereas defensive players have the liberty to use both feet. In mathematical terms, these elements are represented as follows [53]:

$$DG = \frac{\sum_{i=1}^{m} X_i^{\text{Def}}}{m}, \quad i = 1, 2, \dots m,$$

$$X_i^{\text{offNew1}} = \frac{X_i^{\text{off}} + r_1 \times DG - r_2 \times X_{r3}^{\text{Def}}}{2}, \quad i = 1, 2, \dots m.$$

$$(18)$$

Here, " r_1 " and " r_2 " denote two random numbers within the range of [0, 1], signifying the ability of the offensive players. " X_{r3}^{Def} " is a random integer ranging from 1 to "m". X_i^{offNew1} represents the position vector of the upcoming ith offensive player in the field, while "DG" stands for the defensive group. The subsequent step involves the evaluation of the objective function for each player, following a confrontation between the ith offensive player and a specific defensive player. The winning state (WS) of the players is then determined. If the offensive player emerges as the winner, based on the squid game's fundamental rules, they join the successful offensive group (SOG). The offensive player can use both feet for this purpose if the defensive player's winning state is lower than the offensive player's winning state. The mathematical representation of these aspects is articulated as [53]

$$X^{\text{off}} = \begin{bmatrix} X_1^{\text{off}} \\ X_2^{\text{off}} \\ \vdots \\ X_i^{\text{off}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j & \cdots x_1^d \\ x_2^1 x_2^2 \cdots x_2^j & \cdots & x_2^d \\ \vdots \\ x_i^1 x_i^2 \cdots x_i^j & \cdots & x_i^d \\ \vdots \\ x_m^{\text{off}} \end{bmatrix}, \quad \begin{cases} i = 1, 2, \dots & m, \\ j = 1, 2, \dots & d, \end{cases}$$

$$X^{\text{Sccoff}} = \begin{bmatrix} X_1^{\text{Sccoff}} \\ X_2^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j & \cdots & x_1^d \\ x_2^1 x_2^2 \cdots & x_2^j & \cdots & x_2^d \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ x_n^1 x_n^2 \cdots & x_n^j & \cdots & x_n^d \end{bmatrix}, \quad \begin{cases} i = 1, 2, \dots & m, \\ j = 1, 2, \dots & \cdots & d, \end{cases}$$

$$X^{\text{Sccoff}} = \begin{bmatrix} X_1^{\text{Sccoff}} \\ \vdots \\ X_n^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j & \cdots & x_n^d \\ \vdots \\ x_n^1 x_n^2 \cdots & x_n^j & \cdots & x_n^d \end{bmatrix}, \quad \begin{cases} i = 1, 2, \dots & \cdots & m, \\ j = 1, 2, \dots & \cdots & d, \end{cases}$$

$$X^{\text{Def}} = \begin{bmatrix} X_1^{\text{Def}} \\ X_2^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j & \cdots & x_n^d \\ x_1^2 x_2^2 \cdots & x_2^j & \cdots & x_n^d \\ \vdots \\ x_n^1 x_n^2 \cdots & x_n^j & \cdots & x_n^d \end{bmatrix}$$

$$X^{\text{Def}} = \begin{bmatrix} X_1^{\text{Def}} \\ X_2^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots & x_1^j & \cdots & x_n^d \\ x_1^2 x_2^2 \cdots & x_2^j & \cdots & x_n^d \\ \vdots \\ x_n^2 x_n^2 \cdots & x_n^j & \cdots & x_n^d \end{bmatrix}$$

$$X^{\text{Def}} = \begin{bmatrix} X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Sccoff}} \\ \vdots \\ X_n^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots & x_n^d \\ \vdots \\ x_n^1 x_n^2 \cdots & x_n^d \end{bmatrix}$$

$$X^{\text{Def}} = \begin{bmatrix} X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Sccoff}} \\ \vdots \\ X_n^{\text{Sccoff}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}} \end{bmatrix} = \begin{bmatrix} X_1^{\text{Def}} \\ X_1^{\text{Def}} \\ \vdots \\ X_n^{\text{Def}}$$

Defensive players are deemed the game's champions and are asked to join the SDG if their winning states are better than those of the offensive players. It is anticipated that the defensive players in this group will defend the bridge, the playground's pivotal feature. In preparation for starting a fresh fight, the thriving defensive players move among the attacking performers in the group. The mathematical appearance of these parts is given below [53].

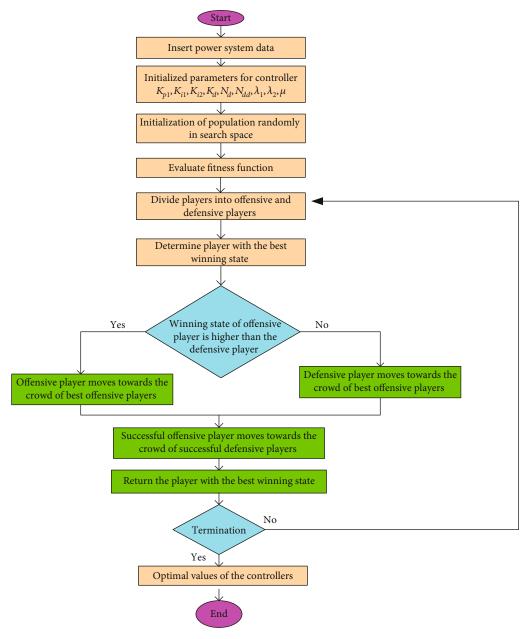


FIGURE 6: Flow diagram of SGO techniques.

$$SDG = \begin{bmatrix} X_1^{Sccoff} \\ X_2^{Sccoff} \\ \vdots \\ X_i^{Sccoff} \\ \vdots \\ X_p^{Sccoff} \end{bmatrix} = \begin{bmatrix} x_1^1 x_1^2 \cdots x_1^j \cdots x_1^d \\ x_2^1 x_2^2 \cdots x_2^j \cdots x_2^d \\ \cdots & \ddots & \vdots \\ x_i^1 x_i^2 \cdots x_i^j \cdots x_i^d \\ \cdots & \ddots & \vdots \\ x_p^1 x_p^2 \cdots x_p^j \cdots x_p^d \end{bmatrix}, \quad \begin{cases} i = 1, 2, \dots \dots p, \\ j = 1, 2, \dots \dots d, \end{cases}$$

$$OG = \frac{\sum_{i=1}^m X_i^{\text{off}}}{m}, \quad i = 1, 2, \dots \dots m,$$

$$X_i^{\text{DefNew1}} = \frac{X_i^{\text{Def}} + r_1 \times \text{OG} - r_2 \times X_{r3}^{\text{off}}}{2}, \quad i = 1, 2, \dots \dots m.$$

$$(20)$$

The algorithm introduces an additional search loop, where offensive players within the successful offensive group (SOG) endeavor to navigate a bridge guarded by defensive players in the successful defensive group (SDG). This inclusion is aimed at intelligently adapting the exploration and exploitation phases of the proposed algorithm. To achieve this, a position-updating operation is executed for all offensive players in SOG, involving advancement towards the best-known solution candidate and a specific defensive player in SDG. This simulates the reward for an offensive player attempting to cross the bridge. The mathematical expression of these components is detailed as follows [53]:

$$X_{i}^{\text{offNew1}} = \frac{X_{i}^{\text{Scoff}} + r_{1} \times \text{BS} - r_{2} \times X_{k}^{\text{ScDef}}}{2}, \quad \begin{cases} i = 1, 2, \dots o, \\ k = 1, 2, \dots o. \end{cases}$$
(21)

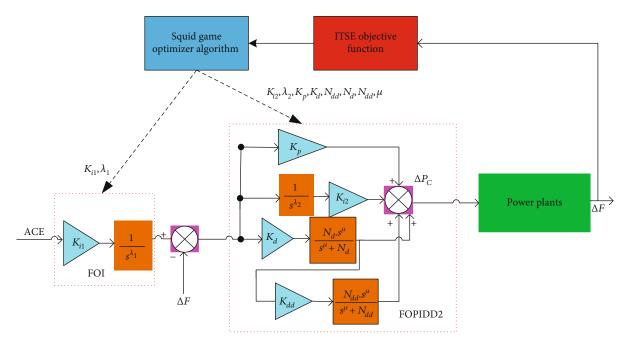


FIGURE 7: Structure of suggested FOI-FOPIDD2.

In SOG and SDG, *p* and *o* are the number of effective defensive and offensive players and "BS" represents the best solution candidate. The flow diagram for the proposed SGO method is depicted in Figure 6.

4. Design of Cascaded Based Controllers and Expression of Fitness Function

4.1. Concept of Fractional Order. Fractional calculus is a field of mathematical analysis that expands traditional calculus to include integrators and differentiators with noninteger orders. These orders are represented as ${}_aD_t^{\gamma}$, where "a" and "t" indicate the operation boundaries and γ is a real number (R). The formulas for fractional-order integrator and differentiator can be expressed as follows [64, 65]:

$${}_{a}D_{t}^{\gamma} = \begin{cases} \frac{d^{\gamma}}{dt^{\gamma}}, & \gamma > 0, \\ 1, & \gamma = 0, \\ \int_{0}^{t} (d\tau)^{\gamma}, & \gamma < 0. \end{cases}$$
 (22)

The field of fractional calculus is guided by three essential principles: the Riemann-Liouville (RL) principle, the Caputo principle, and the Grunwald-Letnikov (GL) principle. These principles are represented by equations (14)–(16) correspondingly [64, 65].

$${}_{a}D_{t}^{\gamma}f(f) = \frac{1}{\Gamma(n-r)} \frac{d^{n}}{dt^{n}} \int_{a}^{t} \frac{f(\tau)d(\tau)}{(t-\tau)^{\gamma-n+1}} ; n-1 < \gamma < n,$$

$${}_{a}D_{t}^{\gamma}f(f) = \frac{1}{\Gamma(n-r)} \int_{a}^{t} \frac{f^{n}(\tau)d(\tau)}{(t-\tau)^{\gamma-n+1}} ; n-1 < \gamma < n,$$

$${}_{a}D^{a}t^{\gamma}f(t) = \lim_{b \longrightarrow 0} \frac{1}{b^{\gamma}} \sum_{i=0}^{[(t-a)/b]} (-1)^{i} \binom{\gamma}{i} f(t-jb).$$
(23)

Mathematically, the α th fractional-order (FO) derivative, denoted as S^{α} , can be represented as follows [25]:

$$S^{\alpha} = \omega_h^{\alpha} \prod_{K=-N}^{N} \frac{s + \omega_k^z}{s + \omega_p^p}.$$
 (24)

In this study, oustaloup-based recursive approximations are applied with a filter order of 5 and within the range of $[10^{-3}, 10^{3}]$ rad/s. The primary objective of the new design of the cascaded controller is to regulate and enhance the frequency response of a diverse power system coping with immediate load variations and variations. The controller has been recommended in both regions to reduce fluctuations in frequency and interconnected tie line power discrepancies between both regions. Conventional PID controllers are commonly utilized in manufacturing due to their straightforward design and efficient functioning. Like the standard PID structure, the PIDD2 assembly also incorporates a second-order derivative gain [66]. The FOI-FOPIDD2 controller has not yet been utilized in a study, despite numerous approaches being tested to improve the control performance of LFC systems. Researchers have shown that PIDD2 and FOPIDD controllers outperform traditional PID controllers. Figure 7 displays the cascaded based FOI-FOPIDD2 controller that was established by fusing FOPIDD2 controller and fractionalorder integral controller.

Equations (25) and (26) describe the transfer function of the FOI and FOPIDD2 controllers. Similarly, equation (27) illustrates the connection between the system's output and the error signal.

$$FOI = C_1(s) = \frac{K_{i1}}{s^{\lambda 1}}, \tag{25}$$

| | Approach | Кр | K_i | K_{i1} | K_{i2} | K_d | K_{dd} | N_d | N_{dd} | μ | λ_1 | λ_2 |
|--------|------------------|-------|-------|----------|----------|-------|----------|-------|----------|-------|-------------|-------------|
| | SGO: FOI-FOPIDD2 | 3.875 | | 4.566 | 3.565 | 3.980 | 5.322 | 7.234 | 5.405 | 0.122 | 0.054 | 0.032 |
| | JSO: FOI-FOPIDD2 | 1.090 | _ | 3.783 | 2.989 | 1.678 | 7.778 | 9.772 | 7.012 | 0.378 | 0.252 | 0.098 |
| | PSO: FOI-FOPIDD2 | 1.120 | _ | 2.109 | 3.120 | 1.989 | 3.345 | 3.300 | 4.890 | 0.045 | 0.458 | 0.212 |
| | GWO: FOI-FOPIDD2 | 3.456 | _ | 1.900 | 1.123 | 1.110 | 2.657 | 6.090 | 5.780 | 0.157 | 0.234 | 0.114 |
| Area 1 | FA: FOI-FOPIDD2 | 5.101 | _ | 2.546 | 2.787 | 2.079 | 8.456 | 8.567 | 4.781 | 0.056 | 0.767 | 0.098 |
| | FOI-FOPIDD2: SGO | 4.101 | _ | 1.989 | 3.897 | 4.671 | 5.322 | 9.566 | 8.456 | 0.452 | 0.286 | 0.097 |
| | FOPID: SGO | 1.234 | 0.53 | _ | _ | 3.980 | _ | _ | _ | 0.042 | 0.223 | _ |
| | PIDD2: SGO | 4.760 | 3.45 | _ | _ | 2.974 | 6.897 | 4.678 | 9.898 | _ | _ | _ |
| | PID: SGO | 3.12 | 2.89 | _ | _ | 7.789 | _ | _ | | _ | _ | _ |
| | SGO: FOI-FOPIDD2 | 8.908 | _ | 0.345 | 1.232 | 5.780 | 9.678 | 1.090 | 7.898 | 1.223 | 1.009 | 0.011 |
| | JSO: FOI-FOPIDD2 | 5.776 | _ | 7.879 | 3.345 | 4.445 | 3.390 | 9.878 | 4.454 | 1.909 | 2.000 | 1.019 |
| | PSO: FOI-FOPIDD2 | 8.902 | _ | 3.452 | 5.776 | 3.389 | 5.990 | 9.999 | 3.334 | 0.345 | 1.209 | 0.345 |
| | GWO: FOI-FOPIDD2 | 5.346 | _ | 3.786 | 7.090 | 3.786 | 1.298 | 7.897 | 1.909 | 1.123 | 0.009 | 0.465 |
| Area 2 | FA: FOI-FOPIDD2 | 5.090 | _ | 2.786 | 4.570 | 8.019 | 3.678 | 3.435 | 5.009 | 1.543 | 0675 | 1.010 |
| | FOI-FOPIDD2: SGO | 8.111 | _ | 4.567 | 9.890 | 2.991 | 5.900 | 2.567 | 9.090 | 1.902 | 1.223 | 1.070 |
| | FOPID: SGO | 2.134 | 4.67 | _ | _ | 1.980 | _ | _ | _ | 1.090 | 0.903 | _ |
| | PIDD2: SGO | 1.340 | 9.34 | _ | _ | 5.909 | 9.009 | 1.903 | 8.000 | _ | _ | _ |
| | PID: SGO | 4.12 | 9.87 | _ | _ | 2.009 | _ | _ | _ | _ | _ | _ |

Table 3: Optimal values for the recommended methods.

TABLE 4: Value of SGO parameters.

| Parameters | Values | Parameters | Values | Parameters | Values | Parameters | Values |
|-------------------|--------|------------------|--------|-----------------------------|--------|-------------|--------|
| Population number | 30 | No. of iteration | 80 | Lower limit | -10 | Upper limit | 10 |
| No. of dimension | 10 | Random numbers | [0, 1] | Execution of each iteration | 25 | | |

Table 5: Statistical parametric analysis for various techniques.

| T. d | Statistical parameters | | | | | | |
|------------------|------------------------|-----------------------|-----------------------|-----------------------|--|--|--|
| Techniques | Best | Worst | Mean | Standard deviation | | | |
| SGO: FOI-FOPIDD2 | 4.57×10^{-5} | 4.58×10^{-5} | 4.58×10^{-5} | 4.57×10^{-7} | | | |
| JSO: FOI-FOPIDD2 | 7.23×10^{-4} | 7.28×10^{-4} | 7.25×10^{-4} | 0.96×10^{-6} | | | |
| GWO: FOI-FOPIDD2 | 8.01×10^{-4} | 8.11×10^{-4} | 8.08×10^{-4} | 9.23×10^{-6} | | | |
| FA: FOI-FOPIDD2 | 3.45×10^{-3} | 3.52×10^{-3} | 3.49×10^{-3} | 2.43×10^{-5} | | | |
| PSO: FOI-FOPIDD2 | 3.02×10^{-3} | 3.34×10^{-3} | 3.28×10^{-3} | 6.89×10^{-5} | | | |

$$\begin{split} \text{FOPIDD2} &= C_2(s) = \text{Kp} + \frac{K_{i2}}{s^{\lambda 2}} + K_d \left[\frac{N_d s^{\mu}}{s^{\mu} + N_d} \right] \\ &+ K_d \left[\frac{N_d s^{\mu}}{s^{\mu} + N_d} \right] . K_{dd} \left[\frac{N_{dd} s^{\mu}}{s^{\mu} + N_{dd}} \right], \end{split} \tag{26}$$

$$\begin{split} U(s) &= \left[\mathrm{Kp} + \frac{K_{i1}}{s^{\lambda 1}} + \frac{K_{i2}}{s^{\lambda 2}} + K_d \left[\frac{N_d s^\mu}{s^\mu + N_d} \right] \right. \\ &+ K_d \left[\frac{N_d s^\mu}{s^\mu + N_d} \right] . K_{dd} \left[\frac{N_{dd} s^\mu}{s^\mu + N_{dd}} \right] E(s), \end{split} \tag{27}$$

where λ_1 , λ_2 , and μ are the integral-differentiator operators; N_d and N_{dd} denote the filter constants; and Kp, K_d , K_{i1} , and K_{i2} indicate the proportional, derivative, and integral coefficients of the proposed controller. The FOI-FOPIDD2 controller gains have been established by reducing the cost function through the utilization of the SGO. The settling period is shortened, and high oscillations are swiftly suppressed using an ITSE-based cost function [25, 33, 37]:

ITSE =
$$j = \int_{o}^{t} t \left[\Delta F_1^2 + \Delta F_2^2 + \Delta P_{\text{tie}}^2 \right] dt$$
. (28)

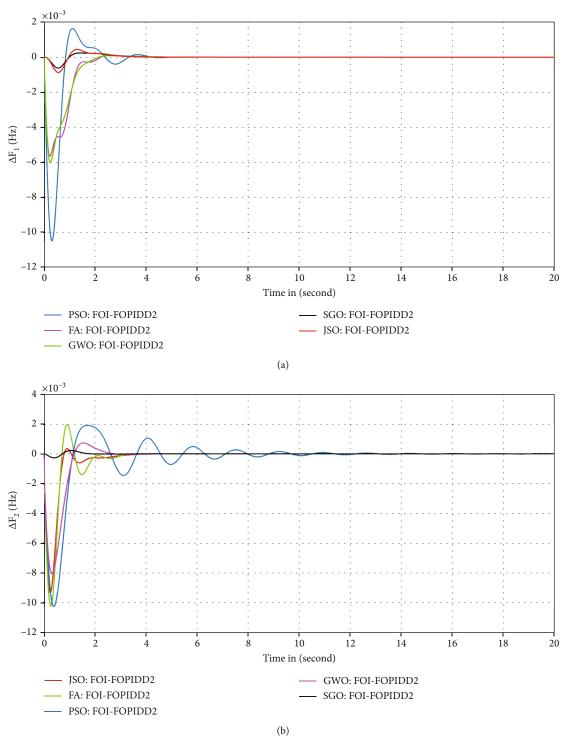


Figure 8: Continued.

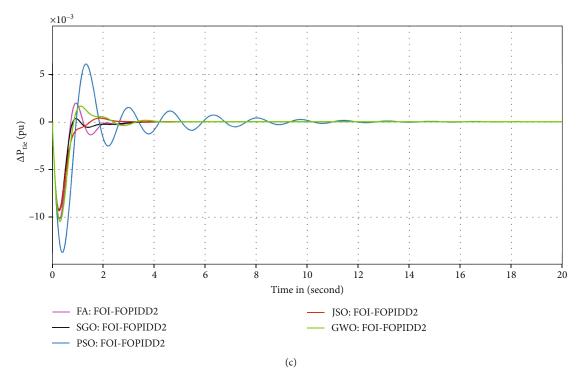


Figure 8: Transient response of PS considering case 1 for (a) ΔF_1 , (b) ΔF_2 , and (c) $\Delta P_{\rm tie}$.

Table 6: Comparison performance for case 1.

| Transient parameters | Variation in areas | PSO | FA | GWO | ISO | SGO | WCA [52] |
|----------------------|---------------------|-----------|----------|----------|------------|-----------|----------|
| | ΔF_1 | 4.01 | 3.29 | 2.83 | 2.34 | 2.22 | 12.27 |
| Time settling | ΔF_2 | 11.93 | 3.23 | 2.64 | 2.90 | 1.52 | 29.46 |
| Ü | $\Delta P_{ m tie}$ | 12.11 | 3.66 | 3.83 | 3.07 | 2.81 | 30.50 |
| | ΔF_1 | 0.001632 | 0.000076 | 0.000123 | 0.0004376 | 0.0002347 | 0.00280 |
| Overshoot | ΔF_2 | 0.001890 | 0.001949 | 0.000725 | 0.0003407 | 0.0002201 | 0.00110 |
| | $\Delta P_{ m tie}$ | 0.006044 | 0.001949 | 0.001710 | 0.0003834 | 0.0003508 | 0.0007 |
| | ΔF_1 | -0.010480 | -0.00601 | -0.00654 | -0.0008692 | -0.000615 | -0.0109 |
| Undershoot | ΔF_2 | -0.010240 | -0.01022 | -0.00803 | -0.0093020 | -0.000268 | -0.0035 |
| | $\Delta P_{ m tie}$ | -0.013700 | -0.01022 | -0.01049 | -0.009516 | -0.009405 | -0.0022 |

Table 7: Comparison performance for case 2.

| Transient parameters | Variation in areas | PID | PIDD2 | FOPID | FOI-FOPIDD2 | FOPI-PD [25] | FOTID [47] | I-TD [52] |
|------------------------------|---------------------|---------|----------|----------|-------------|--------------|------------|-----------|
| | ΔF_1 | 3.80 | 3.66 | 2.86 | 2.69 | 8.434 | 25.5 | 12.27 |
| Time settling (Ts) | ΔF_2 | 4.85 | 4.09 | 3.93 | 3.21 | 10.90 | 23.2 | 29.46 |
| | $\Delta P_{ m tie}$ | 3.83 | 3.71 | 3.66 | 3.20 | 5.98 | 18.77 | 30.50 |
| | ΔF_1 | 0.00194 | 0.00007 | 0.00043 | 0.00024 | 0.00004 | 0.00680 | 0.00280 |
| Overshoot (O _{sh}) | ΔF_2 | 0.00044 | 0.00024 | 0.00028 | 0.00023 | 0.00027 | 0.01170 | 0.00110 |
| | $\Delta P_{ m tie}$ | 0.00241 | 0.00072 | 0.00012 | 0.00007 | 0.00000 | 0.00260 | 0.0007 |
| Undershoot ($U_{\rm sh}$) | ΔF_1 | -0.0102 | -0.00600 | -0.00086 | -0.00061 | -0.00059 | -0.0245 | -0.0109 |
| | ΔF_2 | -0.0008 | -0.00062 | -0.00035 | -0.00026 | -0.00178 | -0.0228 | -0.0035 |
| | $\Delta P_{ m tie}$ | -0.0087 | -0.00803 | -0.00564 | -0.00601 | -0.00084 | -0.0044 | -0.0022 |

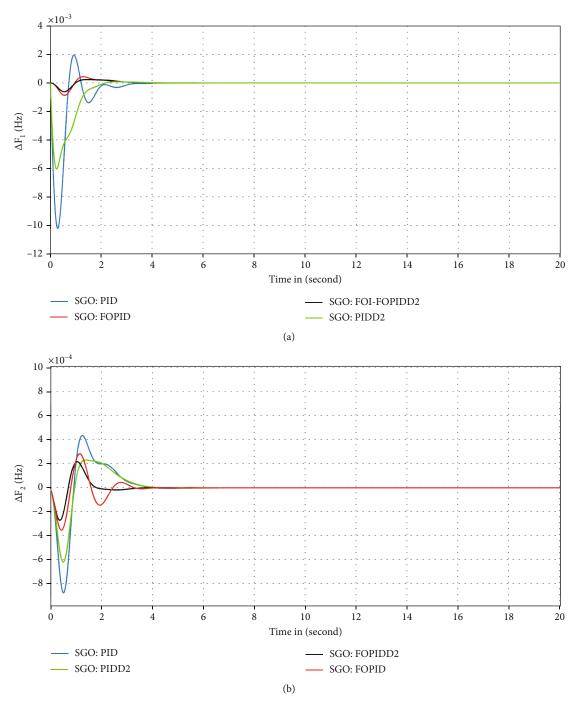


Figure 9: Continued.

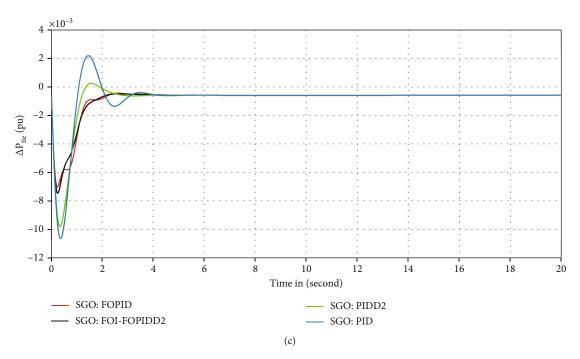


FIGURE 9: Transient response of PS considering case 2 for (a) ΔF_1 , (b) ΔF_2 , and (c) ΔP_{tie} .

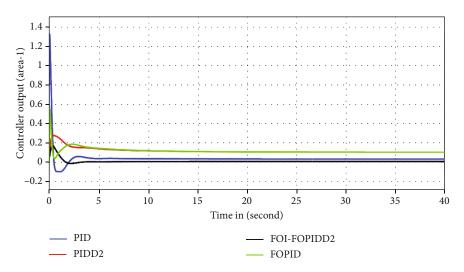


FIGURE 10: Controller efforts for various controllers in area 1.

The FOI-FOPIDD2 controller gains are subject to the following restrictions.

$$\begin{split} K_{p}^{\text{Min}} &\leq K_{p} \leq K_{p}^{\text{Max}} \; ; K_{d}^{\text{Min}} \leq K_{d} \leq K_{d}^{\text{Max}} \; ; K_{dd}^{\text{Min}} \leq K_{dd} \\ &\leq K_{dd}^{\text{Max}} \; ; K_{i1}^{\text{Min}} \leq K_{i1} \leq K_{i1}^{\text{Max}} \; ; K_{i2}^{\text{Min}} \leq K_{i2} \\ &\leq K_{i2}^{\text{Max}} \; ; N_{dd}^{\text{Min}} \leq N_{dd} \leq N_{dd}^{\text{Max}} \; , N_{d}^{\text{Min}} \leq N_{d} \\ &\leq N_{d}^{\text{Max}} \; ; \lambda_{1}^{\text{Min}} \leq \lambda_{1} \leq \lambda_{1}^{\text{Max}} \; ; \lambda_{2}^{\text{Min}} \leq \lambda_{2} \\ &\leq \lambda_{2}^{\text{Max}} \; ; N_{d}^{\text{Min}} \leq N_{d} \leq N_{d}^{\text{Max}} \; ; \mu^{\text{Min}} \leq \mu \leq \mu^{\text{Max}} \; . \end{split} \tag{29}$$

The range of values for the parameters Kp, K_{i1} , K_{i2} , K_d , N_d , and N_{dd} is from 0 to 10, while the values for λ_1 , λ_2 , and μ are from 0 to 2.

5. Results, Execution, and Discussion

This study uses a combination of several hybrid power sources coupled with redox flow battery (RBF) and capacitor energy storage to test the effectiveness and validity of a novel FOI-FOPIDD2 controller. To meet the LFC goal function, the proposed controller coefficients are tweaked with the squid game optimizer utilizing the MATLAB programming language and connected with the Simulink tool. The SGO-based controller knobs for the specified case study are indicated in Table 3 following 80 iterations of the optimization techniques using the materials from Table 4. The statistical values foe various techniques are shown in Table 5. While employing the same alignment with the RFB system that uses the SGO technique, the suggested FOI-FOPIDD2

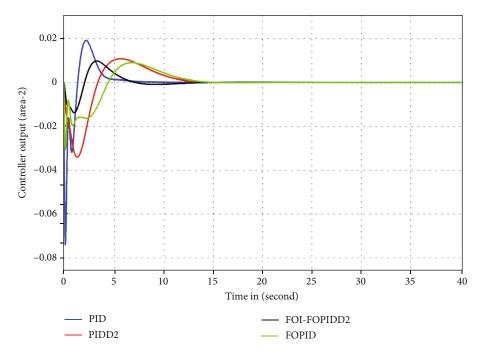


FIGURE 11: Controller efforts for FOI-FOPIDD2 in area 2.

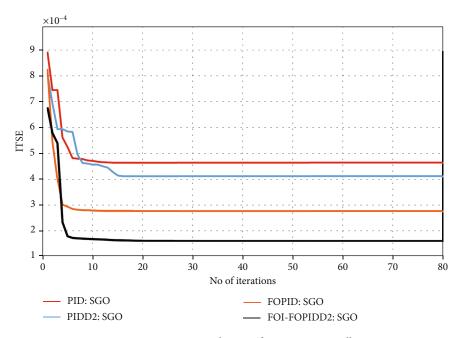


FIGURE 12: Convergence diagram for various controllers.

controller's robustness is compared to other regulators like PIDD2, PID, and FOPID. The load changes are fixed at 5% = 0.05 per unit, in all cases. Results from the examined multiarea IPS are rigorously examined in the subsequent case studies.

5.1. Case 1 (Analyses of Algorithm Performance). The squid game algorithm was compared with various recent algorithms including JSO, PSO, GWO, and firefly algorithm to

determine its efficacy in this scenario. Each algorithm response was measured in terms of area 2 (ΔF_2), tie line ($\Delta P_{\rm tie}$), and area 1 (ΔF_1) as shown in Figures 8(a)–8(c). In Table 6, the overall performance is contrasted for various approaches in respect of transient parameters like $U_{\rm sh}$ (undershoot), $O_{\rm sh}$ (overshoot), and Ts (settling time) for $\Delta P_{\rm tie}$, ΔF_2 , and ΔF_1 . The SGO strategy offered quicker settling times than JSO, GWO, PSO, and FA-based optimization approaches in regions 1 and 2 and the linked tie line. The

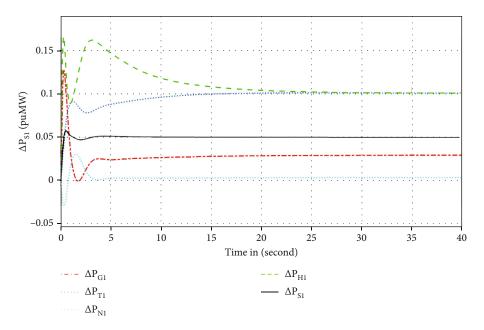


FIGURE 13: Power output for various generation units in area 1.

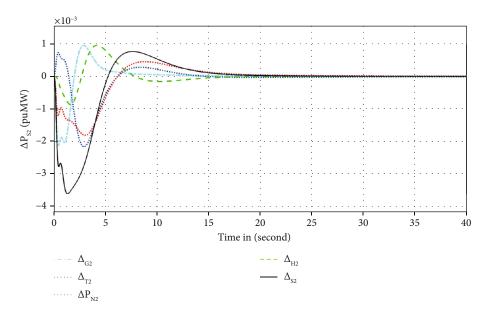


Figure 14: Power output for various generation units in area 2.

SGO approach decreased overshoot for ΔF_1 , ΔF_2 , and $\Delta P_{\rm tie}$ by 81.23%, 45.76%, and 35.22%, respectively, as compared to PSO algorithm. Additionally, our intended method improved the settling time by 14.54%, 20.12%, and 15.34% as compared to PSO algorithms. The SGO algorithms also improve Ts by 22.34%, 09.87%, and 34.89% when compared to GWO algorithm, while also significantly lowering maximum $O_{\rm sh}$ by 71.12%, 72.99%, and 84.17% and undershoot by 80.09%, 36.87%, and 87.76% for ΔF_1 , ΔF_2 , and $\Delta P_{\rm tie}$. When comparing the GSO algorithm with the FA optimizer algorithm, improvements of 12.23% for $\Delta P_{\rm tie}$, 31.98% for ΔF_2 , and 29.76% for ΔF_1 are observed in terms of Ts.

5.2. Case 2 (Analyses of Controller's Performance). This study compared the performance of the FOI-FOPIDD2 controller to that of other control approaches, such as FOPID, PIDD2, PID, and FOTID [47], I-TD [52], and FOPI-PDF [25], in terms of overshoot $(O_{\rm sh})$, minimum undershoot $(U_{\rm sh})$, and time settling (Ts), taking into account changes in area 2 (ΔF_2) , tie line $(\Delta P_{\rm tie})$, and area 1 (ΔF_2) . Overall, Table 7 compares the performance of each optimization procedure using transient metrics. Based on the data shown in Figures 9(a)–9(c) and Table 7, it appears that the FOI-FOPIDD2 control approach performed better than the other control techniques. When compared to the FOPID, PIDD2,

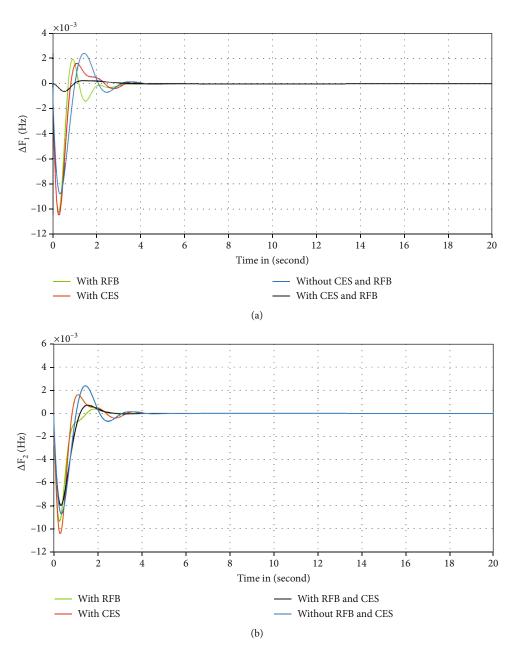


Figure 15: Continued.

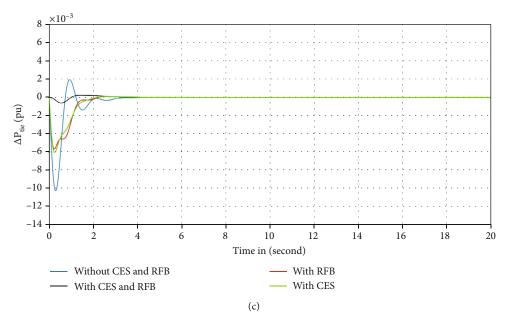


FIGURE 15: Transient response of PS considering case 3 for (a) ΔF_1 , (b) ΔF_2 , and (c) ΔP_{tie} .

| Transient parameters | System consideration | With CES and RFB | Without CES and RFB | With RFB | With CES |
|-----------------------------|----------------------|------------------|---------------------|------------|-----------|
| | ΔF_1 | 2.88 | 4.00 | 3.96 | 3.65 |
| Time settling (Ts) | ΔF_2 | 2.60 | 4.33 | 2.93 | 4.05 |
| | $\Delta P_{ m tie}$ | 2.48 | 3.65 | 2.51 | 2.49 |
| | ΔF_1 | 0.0002347 | 0.0024142 | 0.0019490 | 0.0016320 |
| Overshoot (O_{sh}) | ΔF_2 | 0.0007254 | 0.0024140 | 0.0003912 | 0.0017320 |
| | $\Delta P_{ m tie}$ | 0.000211 | 0.0019389 | 0.0001220 | 0.0000768 |
| | ΔF_1 | -0.0006158 | -0.008772 | -0.0102200 | -0.010480 |
| Undershoot ($U_{\rm sh}$) | ΔF_2 | -0.008038 | -0.008771 | -0.0094160 | -0.010490 |
| | $\Delta P_{ m tie}$ | -0.000612 | -0.0102192 | -0.0056199 | -0.006016 |

Table 8: Comparison performance for case 3.

and PID controllers, the FOI-FOPIDD2 controller tuned using the SGO technique improved settling time for ΔP_{tie} , ΔF_2 , and ΔF_1 by 19.11%, 17.34%, and 15.10%; 16.87%, 31.22%, and 25.07%; and 35.88%, 26.24%, and 23.89%. According to Table 7, the FOI-FOPIDD2 controller beat PIDD2 in terms of $U_{\rm sh}$ (69.44%, 71.23%, and 78.56%) and $O_{\rm sh}$ (56.21%, 67.90%, and 81.19%) for ΔF_1 , ΔF_2 , and $\Delta P_{\rm tie}$. Furthermore, as compared to a FOPID controller, the FOPIDD2 controller reduced overshoot by 57.89%, 67.98%, and 26.12%, respectively, for ΔF_1 , ΔF_2 , and ΔP_{tie} . Similarly, as compared to a PID controller, the FOI-FOPIDD2 controller considerably reduced undershoot by 31.78%, 68.46%, and 73.55%, respectively, for ΔF_1 , ΔF_2 , and ΔP_{tie} . Furthermore, Table 7 shows that the proposed FOPIDD2 controller outperforms PIDD2, PID, FOPID, and FOPI-PDF [25] and I-TD [52] approaches for change in area 2 (ΔF_2), variation in interconnected tie line (ΔP_{tie}), and change in area 1 (ΔF_1). As a result, the proposed FOI-

FOPIDD2 controller appears to be a potential solution for increasing the load frequency performance in a variety of power systems. The controller efforts for area 1 and area 2 have been given in Figures 10 and 11, respectively, which show that our proposed controller performs well as compared to other controllers in respect of quicker settling, reduced overshoot, and undershoot. The convergence diagram for various controllers optimized with SGO is shown in Figure 12. From Figure 12, it can be observed that our proposed control strategies with SGO algorithm converge quickly as compared to other controllers.

Figures 13 and 14 present power output plots of nuclear (ΔP_N) , thermal (ΔP_T) , gas (ΔP_G) , hydro (ΔP_H) , and total power generation (ΔP_S) control regions in response to a 0.05 p.u. MW instantaneous demand disturbance in area 1. The graphs demonstrate the ultimate variations in power generation in area 1; ΔP_{G1} , ΔP_{H1} , ΔP_{N1} , ΔP_{T1} , and ΔP_{S1} are settled to 0.016 p.u. MW, 0.0135 p.u. MW, 0.006 p.u. MW,

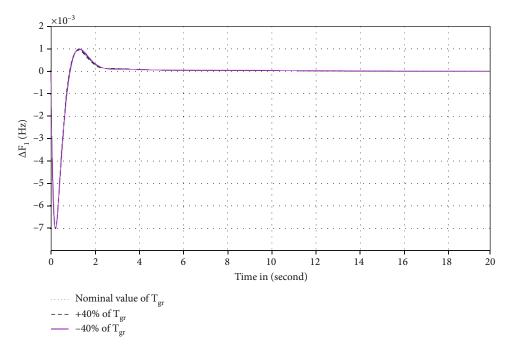


Figure 16: Variation of $T_{\rm gr}$ power system parameters for ΔF_1 .

| Transient response | Parameters of PS | % variation | ΔF_1 | ΔF_2 | $\Delta P_{ m tie}$ |
|--------------------|-------------------|-------------|--------------|--------------|---------------------|
| | $T_{ m gr}$ | +40% | 0.00023470 | 0.0004376 | 0.0001233 |
| | ¹ gr | -40% | 0.0002360 | 0.0004398 | 0.0001298 |
| Overshoot | T | +40% | 0.0002201 | 0.0003407 | 0.0007254 |
| Overshoot | $T{_\mathrm{rh}}$ | -40% | 0.0002226 | 0.0003467 | 0.0007294 |
| | T | +40% | 0.0003508 | 0.0003834 | 0.0017100 |
| | $T_{ m re}$ | -40% | 0.0003569 | 0.0003785 | 0.0017600 |
| | T | +40% | -0.0006158 | -0.0008692 | -0.006016 |
| | $T_{ m gr}$ | -40% | -0.000662 | -0.000884 | -0.006001 |
| Undershoot | T | +40% | -0.000268 | -0.000351 | -0.000622 |
| Undershoot | $T{_\mathrm{rh}}$ | -40% | -0.000220 | -0.000392 | -0.000583 |
| | $T_{ m re}$ | +40% | -0.006016 | -0.005648 | -0.008030 |
| | 1 re | -40% | -0.006080 | -0.005690 | -0.008090 |
| | T | +40% | 2.69 | 2.86 | 3.29 |
| Time settling | $T_{ m gr}$ | -40% | 2.61 | 2.93 | 3.23 |
| | T | +40% | 3.20 | 3.66 | 3.66 |
| | $T_{ m rh}$ | -40% | 3 22 | 3.83 | 3.68 |

+40%

-40%

Table 9: Variations in PS parameters.

0.0135 p.u. MW, and 0.05 p.u. MW, respectively. In area 2, these variations were eventually reduced to 0.00 p.u. MW.

 $T_{\rm re}$

5.3. Case 3 (Analysis of Redox Flow Battery and Capacitive Energy Storage). In case 3, the proposed SGO-FOI-FOPIDD2 has been tested with and without the presence of redox flow battery and capacitive energy storage. The

results for ΔF_1 , ΔF_2 , and $\Delta P_{\rm tie}$ are shown in Figures 15(a)–15(c) and Table 8. Figures 15(a)–15(c) demonstrate that our proposed SGO-FOI-FOPIDD2-based CES and RFB perform superiorly in respect of less overshoot, undershoot, and quicker settling time for area 1 ($O_{\rm sh}=0.00211$, $U_{\rm sh}=-0.00062$, Ts = 2.48), area 2 ($O_{\rm sh}=0.00072454$, $U_{\rm sh}=-0.00080$, Ts = 2.60), and tie line ($O_{\rm sh}=0.0002347$,

2.64

2.63

2.78

2.80

2.52

2.81

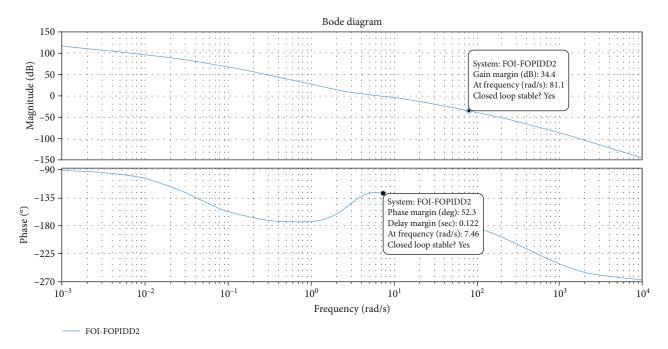


FIGURE 17: Bode diagram for the proposed system.

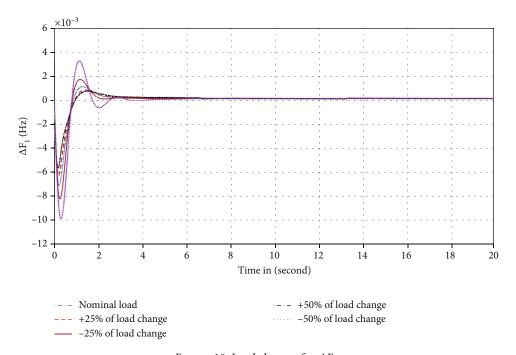


Figure 18: Load changes for ΔF_1 .

 $U_{\rm sh}=-0.000615,~{\rm Ts}=2.88)$ as compared to SGO-FOI-FOPIDD2 based without CES and RFB for area 1 $(O_{\rm sh}=0.0019389,~U_{\rm sh}=-0.0102192,~{\rm Ts}=3.65),~{\rm area}~2$ $(O_{\rm sh}=0.0024140,~U_{\rm sh}=-0.008771,~{\rm Ts}=4.33),~{\rm and}$ tie line $(O_{\rm sh}=0.0024142,~U_{\rm sh}=-0.008772,~{\rm Ts}=4.00);~{\rm SGO-FOPIDD2-based}$ CES for area 1 $(O_{\rm sh}=0.000768,~U_{\rm sh}=-0.01049,~{\rm Ts}=4.05),~{\rm and}$ tie line $(O_{\rm sh}=0.0017320,~U_{\rm sh}=-0.010480,~{\rm Ts}=3.65);~{\rm and}$ SGO-FOI-FOPIDD2-based RFB for area 1

 $(O_{\rm sh}=0.0001220,~U_{\rm sh}=-0.0056199,~{\rm Ts}=2.51),~{\rm area}~2~(O_{\rm sh}=0.0003912,~U_{\rm sh}=-0.009416,~{\rm Ts}=2.93),~{\rm and}~{\rm tie}$ line $(O_{\rm sh}=0.0019490,~U_{\rm sh}=-0.01022,~{\rm Ts}=3.96).~{\rm Using}$ Figures 15(a)–15(c), we can see that the system's response to RFB and CES unit effects is better than its response without RFB and CES component effects in respect of $O_{\rm sh},~U_{\rm sh},~{\rm and}~{\rm Ts}.~{\rm Additionally},~{\rm Table}~8~{\rm highlights}~{\rm the}~{\rm phenomenal}~{\rm results}~{\rm obtained}~{\rm by}~{\rm combining}~{\rm RFB}~{\rm and}~{\rm CES}~{\rm in}~{\rm our}~{\rm proposed}~{\rm method}.$

5.4. Case 4 (Sensitivity and Stability Analysis). Sensitivity analysis has been employed to examine the sturdiness of the recommended SGO-FOI-FOPIDD2 controller. The system's stability may occasionally be negotiated if the proposed control scheme is incapable of accommodating system parameter fluctuations. Various metrics for parameters like T_{gr} , T_{re} , and T_{rh} have been adjusted by approximately ±40% and then contrasted with their nominal parameter response to validate the robustness of the proposed controller. Figures 16 and Table 9 illustrate the dependability of the suggested controller when constraint uncertainty manifests, based on the results obtained when system parameter variations were employed. Figure 17 represents the bode diagram for the proposed FOI-FOPIDD2 controller which confirms the stability of the system due to their positive gain margins and phase margin values. In order to pretend real-time conditions, the performance of the SGO-FOI-FOPIDD2 controller is validated under varied load disturbances up to ±25% and ±50%, as depicted in Figure 18. Numerous parameters respond near to their supposed values, as shown in Table 9, indicating that the suggested SGO-FOI-FOPIDD2 controller provides reliable performance over a spectrum of approximately ±40% of the system's characteristics. Furthermore, the optimal values of the proposed controller have no need to reset controller for a wide range of parameters if employed with the real values at stated value.

6. Conclusion

In this paper, the squid game optimizer-based FOI-FOPIDD2 approach is recommended for the frequency stabilization of diverse two-area power systems containing reheat thermal, gas, hydro, nuclear, redox flow battery, and capacitive energy storage. The superiority of the proposed approach is established by comparing the results with some recent approaches. In terms of settling times and peak under-/overshoots, the squid game optimizer-based FOI-FOPIDD2 approach provides substantially better results than firefly algorithm, grey wolf optimizer, jellyfish search optimization, and particle swarm optimization-tuned FOI-FOPIDD2 controllers. In terms of enhanced settling time, the squid game optimizer-based FOPIDD2 controller outperforms the squid game optimizer-based FOPID, PIDD2, and PID controllers by 19.11%, 17.34%, and 15.10%; 16.87%, 31.22%, and 25.07%; and 35.88%, 26.24%, and 23.89% for ΔF_1 , ΔF_2 , and ΔP_{tie} , respectively. Similarly, the proposed squid game optimizer algorithms also reduced peak overshoot as compared to grey wolf optimizer algorithm by 35.34%, 46.78%, and 76.89%; jellyfish search optimization algorithm by 34.76%, 77.22%, and 82.56%; and firefly algorithm by 82.67%, 89.23%, and 29.67% for ΔF_1 , ΔF_2 , and ΔP_{tie} , respectively. The proposed squid game optimizer algorithms also reduced peak undershoot as compared to jellyfish search optimization algorithm by 62.34%, 22.90%, and 45.76%; grey wolf optimizer algorithm by 56.23%, 84.90%, and 32.16%; particle swarm optimization algorithm by 67.98%, 29.30%, and 34.56%; and firefly algorithm by 78.39%, 59.13%, and 38.55% for ΔF_1 , ΔF_2 , and Δ $P_{\rm tie},$ respectively. It is observed that the recommended squid game optimizer-based FOI-FOPIDD2 is robust and yields higher performance when the size of the load disturbance and system components are changed. In the future, the proposed control scheme and other advanced controllers will be designed and implemented for conventional as well as renewable energy resources.

Data Availability

The data used to support the findings of this study is included within the article.

Conflicts of Interest

The authors declare no conflict of interest.

Authors' Contributions

Conceptualization was carried out by Yidie Ye, Amil Daraz, and Salman AlQahtani. Data curation was performed by Irfan Khan. Formal analysis was participated by Amil Daraz, Abdul Basit, and Irfan Khan. Funding acquisition was provided by Salman AlQahtani. Investigation was carried out by Irfan Khan. Methodology was assisted by Yidie Ye and Irfan Khan. Software was provided by Amil Daraz. Supervision was contributed by Yidie Ye. Validation was performed by Yidie Ye, Abdul Basit, and Irfan Khan. Visualization was participated by Amil Daraz and Abdul Basit. Writing of the original draft was performed by Yidie Ye and Amil Daraz. Writing, reviewing, and editing were carried out by Yidie Ye, Amil Daraz, Abdul Basit, Irfan Khan, and Salman AlQahtani.

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