

ON LOCALLY s -CLOSED SPACES

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(Received October 12, 1992 and in revised form July 23, 1993)

ABSTRACT. In the present paper, the concepts of s -closed sub-spaces, locally s -closed spaces have been introduced and characterized. We have seen that local s -closedness is a semi-regular property; the concept of s - θ -closed mapping has been introduced here and the following important properties are established :-

Let $f : X \rightarrow Y$ be an s - θ -closed surjection with s -set (Maio and Noiri [8]) point inverses. Then :

- (a) If f is completely continuous (Arya and Gupta [1]) and Y is a locally compact T_2 -space, then, X is locally s -closed.
- (b) If f is γ -continuous (Ganguly and Basu [5]) and X is a locally compact T_2 -space, then, Y is locally s -closed.

KEY WORDS AND PHRASES. s -closed subspace, s -set, locally s -closed, s - θ -closed mapping, γ -continuous and completely continuous mapping, regular open set, s - θ -open set, local compactness.

1991 AMS SUBJECT CLASSIFICATION CODES. 54D99, 54C99.

1. INTRODUCTION. S -closed spaces (Thompson [14]) and s -closed (Maio and Noiri [8]) spaces originated from almost compact spaces by the use of semi-open sets as introduced by Levine [7]. Ganster and Reilly [6] had shown, towards the distinction between these concepts, that every infinite topological space can be embedded as a closed connected subspace of an S -closed space which is not an s -closed space. Noiri [13] further generalized S -closed spaces to locally S -closed spaces. In this paper we generalize s -closed spaces to locally s -closed spaces and study s -closed subspaces. Certain important characterizations and properties of locally s -closed spaces have also been established. s - θ -closed mapping is introduced and characterized and we have seen, under certain conditions on the domain and co-domain spaces, that an s - θ -closed mapping would be a continuous mapping. Completely continuous and γ -continuous mappings were introduced respectively by Arya and Gupta [1] and Ganguly and Basu [5]; by the help of these mappings we have been able to establish certain properties which correlate locally compact T_2 -spaces with locally s -closed spaces.

Throughout the present paper, by (X, T) or simply by X we shall mean a topological space. A subset A of a topological space is said to be regular open (resp. regular closed) if $\text{int}(\text{cl}(A))=A$ (resp. $\text{cl}(\text{int}(A))=A$), where $\text{cl}(A)$ (resp. $\text{int}(A)$) denotes the closure (resp. interior) of A . A subset A of a space X is said to be semi-open [7] if there exists an open set O such that $O \subset A \subset \text{cl}(O)$. The complement of a semi-open set is called semi-closed (Crossley and Hildebrand [3]). The semi-closure of a subset A of a space, denoted by $\text{scl}A$, is the intersection of all semi-closed sets containing A (Crossley and Hildebrand [3]). A set A which is both semi-open as well as semi-closed is called a semi-regular set (Maio and Noiri [8]). The collection of all semi-open (resp. semi-regular, regular open) sets containing a point x of X will be denoted by $\text{SO}(x)$ (resp. $\text{SR}(x)$, $\text{RO}(x)$) and for the whole space X these will be denoted by $\text{SO}(X)$ (resp. $\text{SR}(X)$, $\text{RO}(X)$). A point x of X is said to be s- θ -cluster [8] point of a subset A of X if for every $U \in \text{SO}(x)$, $\text{scl}U \cap A \neq \emptyset$. Since, for a semi-open set U , $\text{scl}U$ is a semi-regular set [8], a point x of X is said to be an s- θ -cluster point of A iff $R \cap A \neq \emptyset$, for all $R \in \text{SR}(x)$. The collection of all s- θ -cluster points of A will be denoted by s- θ -cl A ($[A]_{\text{s-}\theta}$, for short). A set A is s- θ -closed if $A = [A]_{\text{s-}\theta}$. A complement of an s- θ -closed set is called an s- θ -open set. For a space (X, T) , $\text{RO}(X, T)$ is a base for a topology T_S on X coarser than T and (X, T_S) is called the semi-regularization space of (X, T) . A topological property P is said to be semi-regular property if whenever a space (X, T) possesses that property P so does its semi-regularization space (X, T_S) . A subset A of X is s-closed [8] (resp. S-closed (Noiri [11])) relative to X or simply an s-set (resp. S-set) if every cover \mathcal{U} of A by sets of $\text{SO}(X)$ admits a finite subfamily \mathcal{U}_0 such that $A \subset \bigcup_{U \in \mathcal{U}_0} \text{scl}U$ (resp. $A \subset \bigcup_{U \in \mathcal{U}_0} \text{cl}U$). In case $A = X$ and A is an s-set (resp. S-set), then X is called s-closed [8] (resp. S-closed [14]). A subset A is called Nearly compact (NC-set (Carnahan [2]), for short) if every cover \mathcal{U} of A by means of open sets of X has a finite subfamily U_1, \dots, U_n (say) such that $A \subset \bigcup_{i=1}^n \text{intcl}U_i$. Clearly every s-set (resp. compact) set, is an NC-set, but not conversely. A subset A of a space X is said to be an α -set (Noiri [10]) if $A \subset \text{int}(\text{cl}(\text{int}(A)))$.

2. s-CLOSED SUBSPACES. At the very outset, an example is given to assert that, every set, s-closed relative to X , is not necessarily an s-closed subspace of X .

EXAMPLE 1. Every countable set in an uncountable set X with co-countable topology T is s-closed relative to (X, T) , but is not even an S-closed subspace.

DEFINITION 1. A subset A of X is said to be pre-open (Mashour et al. [9]) if $A \subset \text{intcl}A$. This collection includes all open sets and, even more, all α -open sets.

LEMMA 1. (See Dorsett [4]) Let (X, T) be a topological space and let A be pre-open set in (X, T) , then $\text{SR}(A, T_A) = \text{SR}(X, T) \cap A$, where T_A is the subspace topology on A .

THEOREM 1. A pre-open set A of X is s-closed as a subspace iff it is s-closed relative to X .

PROOF. Let A be s-closed relative to X and also let $\{V_\alpha : \alpha \in I\}$ be a cover of A by semi-regular sets of the subspace A . Then by Lemma 1, there exists a semi-regular set U_α in X , for each $\alpha \in I$, such that $V_\alpha = U_\alpha \cap A$. Therefore, $A \subset \bigcup_{\alpha \in I} U_\alpha$. Since A is s-closed relative to X , there exists a finite subset I_0 of I such that $A \subset \bigcup_{\alpha \in I_0} U_\alpha$, which shows that $A \subset \bigcup_{\alpha \in I_0} (U_\alpha \cap A)$ i.e., $A \subset \bigcup_{\alpha \in I_0} V_\alpha$. Therefore, A is s-closed as a subspace.

Conversely, let A be s -closed as a subspace. Let $\{V_\alpha : \alpha \in I\}$ be a cover of A by semi-regular sets of X . Then $A = \bigcup_{\alpha \in I} (V_\alpha \cap A)$. Since A is s -closed as a subspace, there exists a finite subset I_0 of I such that $A = \bigcup_{\alpha \in I_0} (V_\alpha \cap A)$, which shows that $A \subset \bigcup_{\alpha \in I_0} V_\alpha$. Therefore A is s -closed relative to X .

THEOREM 2. Let B be a pre-open set in (X, T) . Then a subset A of B is s -closed relative to the subspace B iff A is s -closed relative to X .

PROOF. The proof follows by Lemma 1.

COROLLARY 1. Let A and B be open sets of a space X such that $A \subset B$. Then A is an s -closed subspace of B iff A is an s -closed subspace of X .

PROOF. Applying Theorem 1 and Theorem 2, we get the result.

DEFINITION 2. Let (X, T) be a topological space, then $SR(X, T)$ forms a sub-base for a topology called T_{SR} -topology on X .

LEMMA 2. A subset A of a space (X, T) is s -closed relative to (X, T) iff A is compact in (X, T_{SR}) .

PROOF. Let A be s -closed relative to (X, T) . Then every cover of A by sets of $SR(X, T)$ has a finite subcover. But $SR(X, T)$ forms a sub-base for (X, T_{SR}) . So every sub-basic open cover of (X, T_{SR}) has a finite subcover. Therefore by Alexander sub-base theorem A is compact in (X, T_{SR}) .

Conversely, if A is compact in (X, T_{SR}) then every sub-basic open cover has a finite subcover. So every cover by sets of $SR(X, T)$ has a finite subcover. Therefore A is s -closed relative to (X, T) .

THEOREM 3. Let B be a T_{SR} -closed set in X and let A be any subset of X which is s -closed relative to (X, T) . Then $A \cap B$ is s -closed relative to (X, T) .

PROOF. Let $\{U_\alpha : \alpha \in I\}$ be a T_{SR} -open cover of $A \cap B$. Then clearly $\{U_\alpha : \alpha \in I\} \cup (X - B)$ is a T_{SR} -open cover of A . By Lemma 2, A is compact relative to (X, T_{SR}) ; and so, there exists a finite subset I_0 of I such that $A \subset \{ \bigcup_{\alpha \in I_0} U_\alpha \} \cup (X - B)$, which implies that $A \cap B \subset \bigcup_{\alpha \in I_0} U_\alpha$. Therefore $A \cap B$ is compact in (X, T_{SR}) . Then by Lemma 2, $A \cap B$ is s -closed relative to (X, T) .

COROLLARY 2. If B is regular open or regular closed and A is any subset of X which is s -closed relative to X , then $A \cap B$ is s -closed relative to X .

PROOF. Since every regular closed or regular open set is semi-regular, the corollary follows from Theorem 2.

COROLLARY 3. If X is an s -closed space and A is a regular open set of X , then A is an s -closed subspace of X .

PROOF. The proof follows from Theorem 1 and Theorem 3.

COROLLARY 4. If A is s -closed open subspace of X and B is a regular open set of X , then $A \cap B$ is an s -closed subspace of X and (hence of A and B).

PROOF. The proof follows from Corollary 2 and Theorem 1 and second part follows from Corollary 1.

THEOREM 4. If $A_i, i = 1, 2, \dots, n$ are s -sets i.e., s -closed relative to X . then $\bigcup_{i=1}^n A_i$ is s -closed relative to X .

PROOF. Straightforward.

THEOREM 5. Let X be an s -closed space and let A be a closed set of X and let frontier of A , denoted by $Fr(A)$, be s -closed relative to X . Then A is s -closed relative to X .

PROOF. Since X is s -closed, by Corollary 3 and Theorem 1, $\text{int}A$ is s -closed relative to X whenever A is a closed set. Since $A = \text{int}A \cup \text{Fr}(A)$, by Theorem 4, A is s -closed relative to X .

3. LOCALLY s -CLOSED SPACES

DEFINITION 3. A space X is said to be locally s -closed iff each point belongs to a regular open neighbourhood (nbd. for short) which is an s -closed subspace of X .

REMARK 1. Clearly every s -closed space is a locally s -closed space. However, the converse is not true, in general, because any uncountable set with discrete topology is locally s -closed but not s -closed.

THEOREM 6. A topological space (S, T) is locally s -closed iff for each point $x \in X$, there exists a regular open set U containing x such that U is locally s -closed.

PROOF. Sufficiency : At first we prove that if A is a regular-open set in (X, T) then every regular-open set in the subspace (A, T_A) is also regular-open in (X, T) . Let $V \subset A$ be regular-open in the subspace (A, T_A) . Then $V = \text{int}_A \text{cl}_A V = \text{int}_A (A \cap \text{cl}_X V) = \text{int}_X (A \cap \text{cl}_X V) = \text{int}_X A \cap \text{int}_X \text{cl}_X V = A \cap \text{int}_X \text{cl}_X V = \text{int}_X \text{cl}_X V$ (as $V \subset A$ implies $\text{int}_X \text{cl}_X V \subset \text{int}_X \text{cl}_X A = A$). Therefore V is regular open in (X, T) . Now let x be any point of X . Then, by hypothesis, there exists a regular-open set U of (X, T) containing x such that U is locally s -closed. Then there exists a regular open set V in U such that $x \in V$ and V is an s -closed subspace of U . Therefore V is a regular-open set in (X, T) and by Corollary 1, V is s -closed subspace of X . Therefore (X, T) is locally s -closed.

Necessity : The proof is straightforward.

THEOREM 7. Let (X, T) be a topological space. The following are equivalent :

- (i) X is locally s -closed;
- (ii) every point has a regular-open set which is s -closed relative to X ;
- (iii) every point x of X has an open nbd U such that $\text{int}_X \text{cl}_X U$ is s -closed relative to X ;
- (iv) every point x of X has an open nbd U such that $\text{scl}U$ is s -closed relative to X ;
- (v) for every point x of X , there exists an α -open set V containing x such that $\text{scl}V$ is s -closed relative to X ;
- (vi) for every point x of X , there exists an α -open set V containing x such that $\text{int}_X \text{cl}_X V$ is s -closed relative to X ;
- (vii) for each $x \in X$, there exists a pre-open set V containing x such that $\text{scl}V$ is s -closed relative to X ;
- (viii) for every x of X , there exists a pre-open set V containing x such that $\text{int}_X \text{cl}_X V$ is s -closed relative to X ;
- (ix) for every $x \in X$, there exists a pre-open set V containing x such that $\text{int}_X \text{cl}_X V$ is an s -closed subspace of X .

PROOF. (i) \rightarrow (ii) : Follows from Theorem 1 and from the fact that every regular-open set is pre-open set. (ii) \rightarrow (iii) is obvious.

(iii) \rightarrow (iv) : Follows from the fact that for an open set U , $\text{scl}U = \text{intcl}U$ (Maio and Noiri [8]). (iv) \rightarrow (v) is evident, since every open set is α -open.

(v) \rightarrow (vi), (vi) \rightarrow (vii), (vii) \rightarrow (viii) and (viii) \rightarrow (ix) are straightforward because of the facts that every α -open set is pre-open and a set V is pre-open iff $\text{scl}V = \text{intcl}V$ (Dorsett [4]). (ix) \rightarrow (i) follows from Theorem 1.

THEOREM 8. A topological space (X, T) is locally s-closed iff, its semi-regularization space (X, T_S) is locally s-closed.

PROOF. Let (X, T) be locally s-closed. Dorsett [4] proved that $SR(X, T) = SR(X, T_S)$ and hence a subset A of X is s-closed relative to (X, T) iff A is s-closed relative to (X, T_S) . We know that if U is an open and V a closed subset of (X, T) , then $cl_T U = cl_{T_S} U$ and $int_T V = int_{T_S} V$. Using these results we can easily prove that for a regular-open set U of (X, T) , $int_T cl_T U = int_{T_S} cl_{T_S} U$. Therefore every regular-open set in (X, T) is regular open in (X, T_S) and vice-versa. So (X, T) and (X, T_S) have the same collection of regular-open sets. Therefore, by definition, (X, T) is locally s-closed iff (X, T_S) is locally s-closed.

REMARK 2. Local s-closedness is a semi-regular property.

DEFINITION 4. A function $f : X \rightarrow Y$ is said to be s- θ -closed if image of each s- θ -closed set in X is closed in Y .

THEOREM 9. A function $f : X \rightarrow Y$ is s- θ -closed iff $cl(f(A)) \subset f([A]_{s-\theta})$ for any subset A of X .

PROOF. Let f be s- θ -closed and A be any subset of X . Then $f([A]_{s-\theta})$ is closed in Y (since $[A]_{s-\theta}$ is s- θ -closed set). Clearly $f(A) \subset f([A]_{s-\theta})$ and hence $cl(f(A)) \subset f([A]_{s-\theta})$.

Conversely, let A be an arbitrary s- θ -closed set in X . By hypothesis $f(A) \subset cl(f(A)) \subset f([A]_{s-\theta}) = f(A)$. Therefore $f(A) = cl(f(A))$ and hence $f(A)$ is closed in Y .

THEOREM 10. A surjective function $f : X \rightarrow Y$ is s- θ -closed iff for each subset A in Y and each s- θ -open set U in X containing $f^{-1}(A)$, there exists an open set V in Y containing A such that $f^{-1}(V) \subset U$.

PROOF. Sufficiency : Suppose that the given hypothesis holds. Let A be any s- θ -closed set in X . Let y be an arbitrary point in $Y - f(A)$; then $X - A$ is an s- θ -open set containing $f^{-1}(y)$; by hypothesis, there exists an open set V_y containing y such that $f^{-1}(V_y) \subset X - A$. This shows that $y \in V_y \subset Y - f(A)$. Therefore $Y - f(A) = \bigcup \{ V_y : y \in Y - f(A) \}$. Hence $Y - f(A)$ is an open set i.e., $f(A)$ is closed in Y .

Necessity : Let $V = Y - f(X - U)$. Since $f^{-1}(A) \subset U$, it shows that $A \subset V$. As f is s- θ -closed, $f(X - U)$ is closed and hence V is open in Y . Therefore, $f^{-1}(V) \subset X - f^{-1}\{f(X - U)\} \subset U$.

LEMMA 3. A subset A of a space X is an s-set iff every cover of A by s- θ -open sets has a finite subfamily which covers A .

PROOF. Sufficiency part is straightforward.

Necessity : Let A be an s-set. Let $\mathcal{U} = \{ U_\alpha : \alpha \in I \}$ be an s- θ -open cover of A and also let $x \in A$. Then there exists $U_\alpha \in \mathcal{U}$ such that $x \in U_\alpha$. But U_α being an s- θ -open set, there exists a semi-open set V_x such that $x \in V_x \subset scl V_x \subset U_\alpha$. Therefore the family $\{ V_x : x \in A \}$ is a cover of A by semi-open sets of X . Hence there exist points say x_1, \dots, x_n such that $A \subset \bigcup_{i=1}^n scl V_{x_i}$. Hence $A \subset \bigcup_{i=1}^n U_{\alpha_i}$. Therefore \mathcal{U} has a finite subfamily which covers A .

THEOREM 11. Let $f : X \rightarrow Y$ be an s- θ -closed surjection with s-set point inverses; if A is any compact set in Y then $f^{-1}(A)$ is an s-set in X .

PROOF. Let $\mathcal{U} = \{ U_\alpha : \alpha \in I \}$ be any cover of $f^{-1}(A)$ by s- θ -open sets of X . For each point $y \in A$, $f^{-1}(y) \subset \bigcup_{\alpha \in I} U_\alpha$. By hypothesis $f^{-1}(y)$ is an s-set, by Lemma 3,

there exists a finite subfamily I_0 of I such that $f^{-1}(y) \subset \bigcup_{\alpha \in I_0} U_\alpha$. Since we know that Union of any collection s - θ -open sets is s - θ -open and since f is an s - θ -closed function, by Theorem 10, there exists an open set V_y of Y containing y such that $f^{-1}(V_y) \subset \bigcup_{\alpha \in I_0} U_\alpha$. $\{V_y : y \in A\}$ is a cover of a compact set A and hence there exist points y_1, \dots, y_n of A such that $A \subset \bigcup_{i=1}^n V_{y_i}$ which shows that $f^{-1}(A)$ is covered

by a finite number of s - θ -open sets from \mathcal{U} and hence $f^{-1}(A)$ is an s -set.

COROLLARY 5. Let $f : X \rightarrow Y$ be an s - θ -closed surjection with s -set point inverses; if X is T_2 and Y is compact then f is continuous.

PROOF. Let A be a closed set in Y . Therefore A is also compact; by Theorem 11, $f^{-1}(A)$ is an s -set in X . Since every s -set is an NC-set and X is T_2 , by Theorem 2.1 of T. Noiri [12], $f^{-1}(A)$ is closed and hence f is continuous.

DEFINITION 5. A function $f : X \rightarrow Y$ is said to be completely continuous (Arya and Gupta [1]) if inverse image of each open set in Y is regular-open in X .

THEOREM 12. Let $f : X \rightarrow Y$ be a completely-continuous s - θ -closed surjection with s -set point inverses. If Y is locally compact T_2 , X is locally s -closed.

PROOF. Since Y is locally compact T_2 , for each point $x \in X$, there exists a closed compact nbd. U of $f(x)$. Since f is completely continuous, $f^{-1}(\text{int } U)$ is a regular open set containing x . But it is easy to see that every regular-open set is semi-regular and hence an s - θ -closed set (see Maio and Noiri [8]). Since U is compact and f is an s - θ -closed function, by Theorem 11, $f^{-1}(U)$ is an s -set in X and $x \in f^{-1}(\text{int } U) \subset f^{-1}(U)$. Hence, by Corollary 2, $f^{-1}(\text{int } U)$ is an s -set in X . Therefore X is locally s -closed.

DEFINITION 6. A function $f : X \rightarrow Y$ is said to be \mathcal{V} -continuous (Ganguly and Basu [5]) if for each $x \in X$ and each $W \in \text{SO}(f(x))$, there is an open set V containing x such that $f(V) \subset \text{scl } W$. Equivalently f is \mathcal{V} -continuous iff the inverse image of each semi-regular set is clopen.

LEMMA 4. If $f : X \rightarrow Y$ is \mathcal{V} -continuous and $K \subset X$ is compact; then $f(K)$ is an s -set in Y .

PROOF. Let $\{U_\alpha : \alpha \in I\}$ be a cover of $f(K)$ by semi-regular sets of Y . Then $\{f^{-1}(U_\alpha) : \alpha \in I\}$ is a cover of K by open sets of X . Since K is compact, there exists a finite subset I_0 of I such that $K \subset \bigcup_{\alpha \in I_0} f^{-1}(U_\alpha)$ i.e., $f(K) \subset \bigcup_{\alpha \in I_0} U_\alpha$. So $f(K)$ is an s -set in Y .

LEMMA 5. (See [12]) Let X be a T_2 -space. Then for any disjoint NC-sets A and B , there exist disjoint regular open sets U and V such that $A \subset U$ and $B \subset V$.

THEOREM 13. If $f : X \rightarrow Y$ is an s - θ -closed, \mathcal{V} -continuous surjection with s -set point inverses and if X is locally compact T_2 , then Y is locally s -closed.

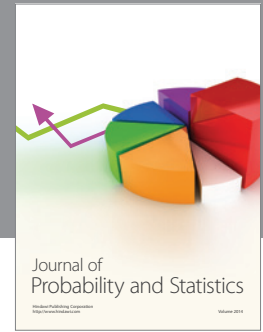
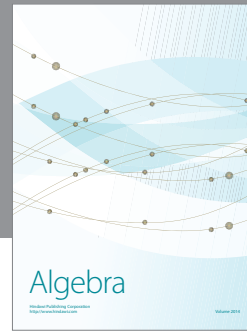
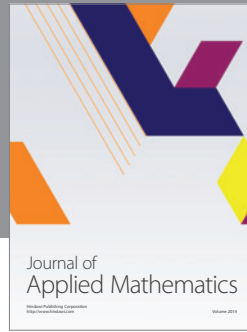
PROOF. We shall first prove that Y is T_2 . Let y_1 and y_2 be two distinct points of Y . Then $f^{-1}(y_1)$ and $f^{-1}(y_2)$ are disjoint s -sets and hence disjoint NC-sets. By Lemma 5, there exist disjoint regular-open sets U_1 and U_2 such that $f^{-1}(y_1) \subset U_1$ and $f^{-1}(y_2) \subset U_2$. But every regular-open set is an s - θ -open set and so, by Theorem 10, there exist open sets V_j , $j = 1, 2$ containing y_j in Y such that $f^{-1}(V_j) \subset U_j$ where $j=1, 2$. Thus Y is T_2 . Let X be locally compact T_2 ; for each point x of $f^{-1}(y)$, there exists a compact closed nbd. U_x of x in X . Since interior of a closed nbd. is a regular-open set, it is semi-regular as well. Therefore the family $\{\text{int } U_x : x \in f^{-1}(y)\}$ is a cover of an s -set $f^{-1}(y)$ by semi-regular sets. By Proposition 4.1

of Maio and Noiri [8], there exist points x_1, \dots, x_n in $t^{-1}(y)$ such that $f^{-1}(y) \subset \bigcup_{i=1}^n \text{int}U_{x_i}$. Let $U = \bigcup_{i=1}^n U_{x_i}$. Then $f^{-1}(y) \subset \bigcup_{i=1}^n \text{int}U_{x_i} \subset \text{int}U$. Since $\text{int}U$ is clearly an s-open set containing $t^{-1}(y)$ and since, t is an s- θ -closed function by Theorem 10, there exists an open set V_y containing y such that $f^{-1}(V_y) \subset \text{int}U$ i.e., $y \in V_y \subset t(\text{int}U) \subset f(U)$. But f being \mathcal{V} -continuous, $t(U)$ is an s-set by Lemma 4. Since Y is T_2 , $f(U)$ is closed by Theorem 2.1 of Noiri [12]. Therefore $y \in V_y \subset \text{intcl}V_y \subset f(U)$. Clearly $\text{intcl}V_y$ is a regular-open set and hence by Corollary 2, $\text{intcl}V_y$ is an s-set. Hence Y is locally s-closed.

ACKNOWLEDGEMENT. The author gratefully acknowledges the kind guidance of Prof. S. Ganguly of the Department of Pure Mathematics, Calcutta University, and is also thankful to the referee for certain constructive suggestion towards the improvement of the paper. He is also grateful to the University Grants Commission, New Delhi, for sponsoring this research work.

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