Research Article

An Eco-Cruise Control for Electric Vehicles Moving on Slope Road with Constant Speed

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1.Introduction

In the last decades, the lane changing/lane keeping system [1, 2], antilock braking system [3], cruise control system (CCS) [4], advanced vehicle motion control systems [5–7], etc. have been widely implemented on the intelligent vehicles. Cruise control system is one of the first intelligent systems implemented on a vehicle, and it has been vastly applied to different types of ground vehicles. In the constant-speed cruise control mode, the driver can be disengaged from the control tasks of accelerator pedal and brake pedal, which helps to decrease driver’s driving load so as to reduce traffic accidents. However, in the constant-speed cruise control mode, when a vehicle is moving on a complex road, such as on a slope road, the driving torque provided by the motor does not often meet the required torque, which is the unreasonable actuation phenomenon. The unreasonable actuation of the motor drive system usually causes the vehicle to consume a lot of unwanted energy. The unwanted energy consumption will undeniably decrease the vehicle’s driving range, and this is one of the main factors hindering the spread and popularization of electric vehicles [8]. Therefore, improving energy efficiency is an urgent issue in the field of electric vehicles.

The past research on CCS mainly involves collision avoidance, constant-speed control, improvement of cruise system’s fault tolerance, and other intelligent functions. To address the collision problem, an intelligent cruise system is designed to force the vehicle acceleration to converge to the desired acceleration by using the on-board radar information [9]. In addition, [10, 11] propose advanced algorithms to address the problems of control strategy, scheduling, and real-time constraints simultaneously. Literature [12] initiates the longitudinal stop-and-go cruise control system of heavy-duty trucks, and the test results show that the method not only meets the desired dynamic response, but also enjoys good robustness. In the parameters optimization aspect, [13, 14]
propose different methods to select PID controller’s parameters to improve the controller’s performance with constant-speed control. The simulation results of the methods in [13, 14] show a good performance in vehicle’s stability. To maintain the constant time headway with respect to the front vehicle, a neuro-fuzzy controller is proposed for intelligent cruise control of semiautonomous vehicles, and this method demonstrates better performance compared with the conventional PID controller [15]. In order to improve the fault tolerance of CCS, a prototype tool is designed in [16], and a fault recovery technique is proposed in [17] to improve the fault tolerance and robustness of CCS; these methods demonstrate a good performance in guaranteeing the normal work of CCS. In addition, to enable the driver to fully disengage himself/herself from the driving task, the new research on CCS is advancing in more intelligent directions, such as adaptive cruise control [18, 19] and cooperative adaptive cruise control [20–25].

Obviously, the aforementioned intelligent technologies and methods contribute to the development of the autonomous vehicles. However, most of the research has not considered the energy efficiency problem. In the last decades, energy consumption in the transportation field has sharply increased and has become one of the most serious challenges. In reality, the driving conditions greatly affect the vehicle’s energy consumption [26].

Usually, the vehicle moving under traffic signs condition with cruise mode will increase energy consumption level due to the unreasonable start, stop, acceleration, and deceleration. To reduce the idle time at a red light and decrease energy consumption, a predictive cruise control [27] that uses the information of upcoming traffic lights is proposed to judge a predictive manner. By this means, it contributes to the improvement of the energy efficiency of the vehicle’s powertrain. According to the traffic information, the energy-efficient cruise control systems [28, 29] are designed to optimize the acceleration profile so as to minimize energy consumption. Similarly, [30] designs an adaptive cruise control system based on the upcoming traffic signal information to reduce the idle time at stop lights and fuel consumption. To decrease the energy consumption due to the queue effects at a signalized intersection, [31] proposes an eco-cooperative adaptive cruise control to improve the vehicle’s fuel efficiency, and the simulation result demonstrates that the overall fuel consumption could be saved up to 40%.

The latest research indicates that driving conditions such as the road slope, the vehicle’s pitch angle, and the vehicle’s mass are seriously affecting the energy consumption and proposes many excellent strategies to improve the energy efficiency [32–36]. However, these methods obtain the road profile from digital maps or from global positioning system (GPS) [32–34], and this will have poor performance in case of shelter conditions. In addition, most of the research mainly focuses on the fuel vehicles [34–36]. Compared with the fuel vehicles, the electric vehicles call for more urgent need to address the energy efficiency problem because of the limits of the driving range.

Therefore, in this paper, we specifically concentrate on the improvement of the electric vehicle’s energy efficiency in constant-speed cruise control mode on slope road. Different from the prevailing methods, in this paper, a novel ECC scheme is proposed without using the digital map’s information or the GPS information. To guarantee that the electric vehicle has good speed maintenance ability and energy efficiency performance in constant-speed cruise control mode, the ECC scheme is realized by considering the deviation in vehicle speed and the deviation in the required torque. With the ECC scheme, the driving torque and the braking torque are optimized so as to reduce the unreasonable actuation of the motor drive system. In summary, the major innovations and significance of this paper are as follows:

1. There is methodological innovation in decreasing electric vehicle’s energy consumption in the constant-speed cruise control mode on slope road. In this paper, an ECC strategy is proposed to improve the speed maintenance ability and energy efficiency performance. With the ECC strategy, the average driving efficiency and the average regenerative braking efficiency of the motor drive system can be improved.

2. An improved BVCIE is proposed to estimate the vehicle’s driving load factors (total mass and pitch angle). In the framework of the improved BVCIE, a new sliding-model-based strategy is designed to improve the robustness of the estimator. With the sliding-model-based strategy, the phenomenon of signal distortion and data loss can be compensated for.

3. A new three-power nonlinear controller is designed based on the estimated driving load factors to avoid the unreasonable actuation of the motor’s torque caused by the slope road condition. The controller enables the motor drive system to provide reasonable driving torque and braking torque according to the deviations in the vehicle speed and the desired torque. Therefore, the unwanted actuation can be avoided.

The rest of this paper is organized as follows. In Section 2, the vehicle dynamics is analyzed, and the required torque is presented. In Section 3, the vehicle’s total mass and the pitch angle are estimated by an improved BVCIE. In Section 4, a novel ECC scheme is proposed. In the ECC scheme, a new controller is designed, and its stability is proved. In Section 5, the simulation platform is introduced, and the estimation results of vehicle’s mass and pitch angle are presented. In Section 6, the cruise control performances by the proposed ECC scheme and by the benchmarked cruise control are analyzed in detail. In Section 7, the energy consumption and the energy saving performance of the proposed ECC and the benchmarked cruise control are analyzed at different cruise speeds. Finally, we conclude this paper with its main novelties and contributions in Section 8.
2. Vehicle Dynamics

When an electric vehicle is moving on a slope road in the constant-speed cruise control mode, the required torque in the longitudinal motion is a real-time variable due to the variation of the driving conditions, such as the vehicle’s pitch angle and the longitudinal speed. Therefore, to maintain the vehicle at the desired cruise speed, the CCS needs to control the driving torque and the braking torque according to the driving conditions. In vehicle’s moving process, the factors affecting the vehicle’s performance include the rolling resistance, the equivalent aerodynamic drag resistance, the slope resistance, and the acceleration resistance, as shown in Figure 1.

Assuming the vehicle’s total mass is \( m \) and the longitudinal acceleration is \( \dot{v} \), the longitudinal dynamics model can be expressed as

\[
F = F_{\text{rol}} + F_{\text{aero}} + F_{\text{slope}} + m\dot{v},
\]

where \( F \) represents a resultant force of the driving force and the braking force, \( F_{\text{rol}} \) refers to the rolling resistance, \( F_{\text{aero}} \) refers to the equivalent aerodynamic drag resistance, and \( F_{\text{slope}} \) refers to the slope resistance. In (1), the rolling resistance depends on the road condition and the vehicle’s total mass, which can be expressed as follows:

\[
F_{\text{rol}} = mg\mu \cos \theta,
\]

where \( g \) is the acceleration due to gravity, \( \mu \) refers to the rolling resistance coefficient, and \( \theta \) refers to the vehicle’s pitch angle.

The slope resistance in (1) is affected by the factors of the vehicle’s total mass and the pitch angle, and this relationship can be expressed as follows:

\[
F_{\text{slope}} = mg \sin \theta.
\]

The equivalent aerodynamic drag resistance in (1) can be expressed as

\[
F_{\text{aero}} = \frac{1}{2}AC_d \rho v^2,
\]

where \( A \) is the frontal area of the vehicle, \( C_d \) is the aerodynamic drag coefficient, \( \rho \) is the density of air, and \( v \) is the vehicle speed. Assuming the wheel’s radius is \( r \), the resultant torque \( T \) in the longitudinal motion can be expressed as

\[
T = Fr.
\]

In (5), the resultant torque is from the electric motor (EM). The relation between the resultant torque and the motor’s torque can be depicted as

\[
T_m = \frac{T}{i_g \eta_g},
\]

where \( i_g \) refers to the gear ratio, \( \eta_g \) refers to the efficiency of the mechanical system, and \( T_m \) is the motor’s torque.

When a vehicle is moving in the constant-speed cruise control mode, the ideal condition is the vehicle moving at the desired cruise speed and the acceleration equal to zero. In addition, in the real condition, the vehicle’s total mass is affected by the passenger number and the payload state, and the pitch angle is determined by the real-time road condition. Therefore, the vehicle’s total mass is an unknown parameter in the moving process, and the pitch angle is a variable in the moving process. Assuming the total mass can be estimated with \( \hat{m} \) in real time and the vehicle’s pitch angle can be estimated with \( \hat{\theta} \) in real time, the required resultant force at the sampling instance \( t_k \) can be expressed as

\[
F_r(t_k) = F_{\text{rol}}(t_k) + F_{\text{aero}}(t_k) + F_{\text{slope}}(t_k)
= \hat{m}(t_k)\mu g \cos(\hat{\theta}(t_k)) + \hat{m}(t_k)g \sin(\hat{\theta}(t_k)) + 0.5AC_d \rho v^2
= \hat{m}(t_k)g\sqrt{1 + \mu^2 \sin^2(\hat{\theta}(t_k) + \theta_0)} + 0.5AC_d \rho v^2.
\]

In (7), \( F_r \) represents the desired resultant force, \( v_r \) represents the desired cruise speed in the constant-speed cruise control mode, and \( \theta_0 \) can be calculated by \( \theta_0 = \arctan \mu \).

According to (5) and (7), the required torque \( T_r \) under the condition that the acceleration is equal to zero can be expressed as

\[
T_r(t_k) = F_r(t_k)r.
\]

3. Estimation of the Total Mass and Pitch Angle

3.1. Estimator Design. The real-time vehicle speed in constant-speed cruise control mode is affected by the driving condition, and consequently when calculating the real-time required torque, it needs to obtain the real-time variables of the vehicle’s total mass and the vehicle’s pitch angle. To address this problem, in this paper, we adopt a BVCIE because it does not need to reconstruct a state space equation. More importantly, compared with Kalman filter (KF), recursive least square (RLS) method, etc., the BVCIE enjoys a higher estimation accuracy. In addition, compared with the neural network method, the BVCIE does not need to train the model through a large amount of data. To construct the BVCIE, we define \( y = \dot{v}, \varphi_1 = T/r-0.5\rho AC_d v^2, \varphi_2 = -g(1 + \mu^2)^{1/2} \); the vehicle longitudinal dynamics (1) can be rewritten with a linear formula:

\[
y = \phi x.
\]

In (9), \( x \) is the vector which needs be estimated, \( x = [x_1, x_2]^T \in \mathbb{R} \), which can be written as follows:
\[
\begin{align*}
    x_1 &= \frac{1}{m}, \\
    x_2 &= \sin(\theta + \theta_p).
\end{align*}
\]  

(10)

Assuming the vector of \( x \) can be estimated with \( \hat{x}(k/k-1) \), where \( k \) and \( k-1 \) are the indexes of the discrete sampling instants, we can easily obtain the system’s estimated output according to (9), and it can be expressed as follows:

\[
\hat{y}(k) = \phi(\hat{x})\hat{x}\left(\frac{k}{k-1}\right),
\]  

(11)

where \( \hat{x}(k/k-1) \) represents the estimated vector by a cross iteration strategy and \( \hat{y} \) is the estimated output. Based on (9) and (11), we can design the estimator with the following formulation:

\[
\hat{x}(k) = \hat{x}\left(\frac{k}{k-1}\right) + \phi^{-1}(y(k) - \hat{y}(k)).
\]  

(12)

According to (9) and (10), the \( \hat{x}_1(k/k-1) \) can be formulated by a cross iteration strategy:

\[
\hat{x}_1\left(\frac{k}{k-1}\right) = f_1(k) + g_1(k)\hat{x}_1\left(\frac{k}{k-1}\right),
\]  

(13)

where \( f_1(k) = \dot{v}(k)/(\langle T(k)/r \rangle - ((1/2)pAC_d\sigma^2(k))) \), \( g_1(k) = (\sqrt[1+\mu^2]}/((T(k)/r) - ((1/2)pAC_d\sigma^2(k))) \).

In vehicle’s moving process, the total mass of the vehicle can be deemed as a constant; thus, we can formulate the following equation:

\[
\hat{x}_1\left(\frac{k}{k-1}\right) = \hat{x}_1\left(\frac{k-1}{k-2}\right) = \hat{x}_1(k-1).
\]  

(14)

Assuming \( \hat{x}_1(k-1) \) can be known in advance, \( \hat{x}_2(k/k-1) \) can be formulated using a cross iteration strategy:

\[
\hat{x}_2\left(\frac{k}{k-1}\right) = f_2(k) + g_2(k)\hat{x}_1\left(\frac{k}{k-1}\right) = f_2(k) + g_2(k)\hat{x}_1\left(\frac{k-1}{k-2}\right) = f_2(k) + g_2(k)\hat{x}_1(k-1),
\]  

(15)

where \( f_2(k) = -\dot{v}(k)/(\sqrt[1+\mu^2}]\), \( g_2(k) = ((T(k)/r) - ((1/2)pAC_d\sigma^2(k)))/\sqrt[1+\mu^2} \).

For the proof of its convergence, please refer to [37] for the details. Now, the vehicle’s total mass and the vehicle’s pitch angle can be estimated by the above estimator. In the above estimator, the inputs of the estimator are the resultant torque, the vehicle speed, and the acceleration. The outputs of the estimator are the estimated vehicle’s total mass and the estimated vehicle’s pitch angle, as shown in Figure 2.

3.2. Sliding-Mode-Based Strategy. Actually, the input signals of the estimator are bounded by a physical constraint, and this constraint can be described as

\[
\begin{align*}
    &T \in [T_{\text{min}}, T_{\text{max}}], \\
    &\nu \in [\nu_{\text{min}}, \nu_{\text{max}}], \\
    &\dot{\psi} \in [\dot{\psi}_{\text{min}}, \dot{\psi}_{\text{max}}],
\end{align*}
\]  

(16)

where \( \text{min} \) and \( \text{max} \) refer to the minimum value and maximum value, respectively. In the vehicle system, the disturbances due to the internal and external factors and the vehicle vibration could result in the input signals’ distortion and even the measurement data’s loss [38], shown as region 1 in Figures 3(a) and 3(b) and region 2 in Figure 3(c), respectively. These cases will seriously affect the estimation results and even result in the wind-up of the estimator. To fix this problem, a sliding-mode-based strategy for processing the input signals is proposed.

The sliding-mode-based strategy includes a look-backward method and a double-threshold method. When data get lost in an input signal, the look-backward method is put into action to fill in the lost data, as shown in the flow diagrams in Figures 3(e) and 3(f). The double-threshold method can be expressed as

\[
\ell = \ell(t_{k-2}) + \ell(t_{k-1}) - \ell(t_k).
\]  

(17)

When the input data get lost at the sampling instance \( t_k \), the filling value with the look-backward method can be expressed as

\[
\ell(t_k) = \ell(t_{k-1}) + \Delta \ell(t_{k-1}) = \ell(t_{k-1}) + (\ell(t_{k-1}) - \ell(t_{k-2})) = 2\ell(t_{k-1}) - \ell(t_{k-2}).
\]  

(18)

Furthermore, when the input signals are greater than its maximum thresholds or smaller than its minimum thresholds, the double-threshold method is applied to process the input signals, as in the flow diagrams shown in Figures 3(d) and 3(f). The double-threshold method can be expressed as follows:

\[
\ell = \begin{cases} 
\ell_{\text{max}}, & \ell \geq \ell_{\text{max}}, \\
\ell_{\text{min}}, & \ell \leq \ell_{\text{min}}.
\end{cases}
\]  

(19)

With the above signal processing strategy, the robustness of the estimator can be enhanced.
4. Eco-Cruise Control

4.1. Control Scheme. The required torque in (8) in Section 2 represents the torque in the condition that the vehicle maintains the desired constant speed. However, when the vehicle is moving on a slope road, the vehicle speed usually shows fluctuations. In this condition, the CCS needs to regulate the driving torque and the braking torque so as to guarantee that the speed maintains the required value. On the sloping road, the driving load is a variable because the road slope is a variable. Thus, in the vehicle speed regulation process, unreasonable actuation conditions in the driving torque and braking torque may occur due to the slope road condition, which will result in a lot of unwanted energy consumption. For this problem, this section proposes an ECC scheme to reduce the unreasonable actuations of the driving torque and braking torque. In order to clearly describe the ECC scheme, the traditional cruise control scheme and the ECC scheme are shown in Figure 4.

Figure 4(a) shows the traditional cruise control scheme. This scheme only considers the deviation in the speed (e) and does not consider the desired driving torque. For the cruise control scheme in Figure 4(a), a state-of-the-art method is model predictive control (MPC). For the MPC-based cruise control, please refer to [23, 28, 39, 40] for details. Figure 4(b) shows the ECC-based cruise control scheme. As shown in Figure 4(b), the controller has two inputs: one is the deviation in the speed (e), and the other is the deviation in the required torque (ΔT). Hence, the ECC scheme can not only guarantee that the speed maintains the desired value, but also keep the driving torque and the braking torque away from the unreasonable actuation.

4.2. Controller Design and Stability Analysis. In order to design a controller for the ECC scheme, the control system of the electric vehicle in Section 2 can be depicted as

\[
\begin{align*}
\dot{x} &= ax^2 + u - b, \\
y &= x,
\end{align*}
\]

where \( x = v, \) \( u = T/(m \cdot r), \) \( a = -0.5 p A C_d / m, \) \( b = g (\sin \theta + \mu \cos \theta). \) To depict the output deviation of the control system (20), the tracking error in the output \( (e_o) \) can be defined as

\[
e_o = y_o - y.
\]  

In addition, for the control system (20), the tracking error in the input \( (e_i) \) can be depicted as

\[
e_i = u_i - u.
\]  

In (22), \( u_i = T_r/(m-r) \) and \( T_r \) can be obtained by (8). According to (21) and (22), when considering the errors in the input and output, a three-power nonlinear controller can be designed as in the following formulation:

\[
u = K_o e_o^3 + K_i e_i,
\]  

where \( K_o \) refers to the gain of the output \( y \), and \( K_i \) refers to the gain of the required input \( u \).

Theorem 1. For the control system (20), if there exist \( K_o \in [0, \xi_o] \) and \( K_i \in [0, \xi_i] \), and they satisfy the following condition:

\[
3K_o e_o^2 \dot{e}_o + K_i \dot{e}_i - b = \ddot{y} - 2ax \dot{y} + x
\]  

then the output \( y \) will converge to \( y_o \) by the control strategy (23).

Proof. If the output \( y \) converges to \( y_o \), (21) should satisfy \( e_o \rightarrow 0 \) by the control strategy (23). Equation (20) can be differentiated as

\[
\ddot{x} = 2ax^2 + \ddot{u} - \dddot{b}
\]  

\[
= 2axx + 3K_o e_o^2 \dot{e}_o + K_i \dot{e}_i - \dddot{b}.
\]  

Substituting (25) into (21) yields

\[
e_o = y_o - \frac{(\dddot{x} + \dddot{b})}{2ax} - \frac{(3K_o e_o^2 \ddot{e}_o + K_i \dddot{e}_o)}{2ax}.
\]  

According to condition (24), \( \dddot{y} \) can be expressed as

\[
\dddot{y} = 3K_o e_o^2 \ddot{e}_o + K_i \dddot{e}_i - \dddot{b} + 2ax \dddot{y}.
\]  

Following the output equation in (20), one can obtain

\[
\dddot{y} = \dddot{x}.
\]  

Thus, (26) can be rewritten as

\[
\dddot{x} = 3K_o e_o^2 \ddot{e}_o + K_i \dddot{e}_i - \dddot{b} + 2ax \dddot{y}.
\]  

Substituting (29) into (26) yields \( e_o = 0. \)
5. Simulation Environment and Estimation Results

This section first presents the test vehicle and the driving environment; then, the state estimation results and the control performance are presented with detailed analysis.

5.1. The Test Vehicle and the Test Road. In this work, the ECC is validated on a cosimulation platform with CarSim and Matlab/Simulink. The vehicle simulator combining CarSim with Matlab is a high-fidelity platform for validating the vehicle dynamics and control methods. The vehicle’s model in CarSim is close to the real-world vehicle. More importantly, the validation through CarSim and Matlab can effectively avoid the influence from the traffic condition and driver’s behavior. For the cosimulation platform in this paper, the version of the Matlab is R2007a, and the version of the CarSim is 2016.0. The parameters of the vehicle body and road information are set in CarSim, and the electric powertrain, the proposed ECC, and the benchmarked methods are built in Matlab/Simulink. The cosimulation platform is validated on personal computer with Windows 10 64-bit operating system, 16 G memory, i7-10510U CPU, 2.30 GHz.

The simulated vehicle is a front wheel drive electric vehicle, as shown in Figure 5(a). The motor drive system of this vehicle is shown in Figure 5(b). In driving mode, the battery provides power for the EM, and the EM drives the front wheels. The EM is a direct-current motor, and the gearbox has single variable speed ratio. In the driving mode, the battery provides energy to the electric powertrain, and in the braking mode, the regenerative braking energy is fed back to the battery. An asphalt road is selected as the test road, which is shown in Figure 5(c). The profile of the road is from the real world. The length of the test road is about 275 meters, the maximum height of the test road is about 4.173 meters, and the test road includes uphill parts and downhill parts. The profile of the test road is shown in Figure 5(d). The driving environment, the designed parameters, and the specification of the test vehicle are shown in Table 1.

In order to analyze the efficiency of the motor, the efficiency map can be fitted by only considering the motor’s torque, and this simplified efficiency map has been successfully used in [41]. For this reason, in this paper, we regard the motor efficiency as a function of torque. The driving efficiency and regenerative braking efficiency of the EM can be fitted by the least square method. Assume that the curve function of the driving efficiency and regenerative braking efficiency can be expressed as

\[ y = a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0. \]  

(30)

To identify the parameters \( a_0, a_1, a_2, a_3, a_4 \) based on the least square method, we need to measure several groups’ data of the motor’s torque and motor efficiency. Since the motor’s torque, the motor’s rotational speed, and the input/output power of the battery in driving mode and braking mode can be easily collected, the motor efficiency (including the driving efficiency and the regenerative braking efficiency) can be calculated with the following equation: where \( \eta_d \) refers to the driving efficiency, \( \eta_r \) refers to the regenerative braking efficiency, \( \omega \) is the motor’s rotational speed, and \( P_o/P_r \) refers to the input/output power of battery.

In order to derive the motor efficiency map, we calculated 11 groups of the driving efficiencies and 11 groups of the regenerative braking efficiencies based on (31). Thus, the curves of the driving efficiency and the regenerative braking efficiency can be fitted. For the fitted driving efficiency curve, \( a_0 = 0.1311, a_1 = 0.0224, a_2 = -2.3647 \times 10^{-4}, a_3 = 9.8593 \times 10^{-7}, a_4 = -1.4736 \times 10^{-9} \). For the fitted braking efficiency curve, \( a_0 = -8.697 \times 10^{-4}, a_1 = 0.0125, a_2 = -8.685 \times 10^{-2}, a_3 = 2.5372 \times 10^{-7}, a_4 = -2.6187 \times 10^{-10} \). The calculated driving efficiency, the regenerative braking efficiency, and the fitted curves are shown in Figure 6. The discrete red points are the calculated driving efficiency, and the dashed green curve refers to the fitted driving efficiency. The discrete blue points refer to the calculated regenerative braking efficiency, and the solid magenta curve refers to the fitted braking regenerative efficiency. In the braking mode, part of the mechanical energy will be converted to the thermal energy and get lost. In addition, the efficiency of the power conversion circuit is unlikely to reach 100%. Moreover, during the braking process, part of the regenerative electric energy will get lost. For these reasons, in Figure 6, the regenerative braking efficiency is lower than the driving efficiency under the same torque condition.

![Cruise control scheme](image-url)
Table 1: Parameters and specification of the test vehicle.

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Values</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vehicle mass</td>
<td>m</td>
<td>1450</td>
<td>kg</td>
</tr>
<tr>
<td>Air density</td>
<td>$\rho$</td>
<td>1.206</td>
<td>N·s$^2$/m$^4$</td>
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<tr>
<td>Maximum road elevation</td>
<td>$h$</td>
<td>4.173</td>
<td>m</td>
</tr>
<tr>
<td>Vehicle front area</td>
<td>$A$</td>
<td>2.2</td>
<td>m$^2$</td>
</tr>
<tr>
<td>Wheel radius</td>
<td>$r$</td>
<td>0.353</td>
<td>m</td>
</tr>
<tr>
<td>Roll inertia</td>
<td>$I_{xx}$</td>
<td>536.6</td>
<td>kg·m$^2$</td>
</tr>
<tr>
<td>Pitch inertia</td>
<td>$I_{yy}$</td>
<td>1536.7</td>
<td>kg·m$^2$</td>
</tr>
<tr>
<td>Yaw inertia</td>
<td>$I_{zz}$</td>
<td>1536.7</td>
<td>kg·m$^2$</td>
</tr>
<tr>
<td>Road distance</td>
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<td>275</td>
<td>m</td>
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<tr>
<td>Battery voltage</td>
<td>$V_{bat}$</td>
<td>335</td>
<td>V</td>
</tr>
<tr>
<td>Battery capacity</td>
<td>$E_{bat}$</td>
<td>61</td>
<td>kwh</td>
</tr>
<tr>
<td>EM’s maximum torque</td>
<td>$T_{m\text{-max}}$</td>
<td>320</td>
<td>Nm</td>
</tr>
<tr>
<td>EM’s maximum power</td>
<td>$P_{m\text{-max}}$</td>
<td>160</td>
<td>kw</td>
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<tr>
<td>Gear ratio</td>
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<tr>
<td>Drag coefficient</td>
<td>$C_d$</td>
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<td>Rolling friction coefficient</td>
<td>$\mu$</td>
<td>0.012</td>
<td>—</td>
</tr>
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</table>

Figure 5: Diagram of the test vehicle and the test road.

Figure 6: Driving efficiency and regenerative braking efficiency of EM.
\[ \eta_o = \frac{T_m \omega}{P_o}, \]
\[ \eta_i = \frac{P}{T_m \omega}, \]

To analyze the proposed ECC scheme, the state-of-the-art method of MPC-based cruise control is selected as a benchmark. The scheme of the benchmarked method is introduced in Figure 4(a) in Section 4.1. For the MPC in Figure 4(a), assuming \( P \) is the predictive horizon, \( M \) is the control horizon, and \( M \leq P \), the predictive output sequence is \( \hat{Y}(k+1) \) and the future control sequence \( \Delta U(k) \) at sample time \( k \) can be formulated as follows:

\[
\begin{bmatrix}
    \hat{Y}(k+1) \\
    \hat{Y}(k+2) \\
    \vdots \\
    \hat{Y}(k+P)
\end{bmatrix}
\]

\[
\begin{bmatrix}
    \Delta U(k) \\
    \Delta U(k+1) \\
    \vdots \\
    \Delta U(k+m-1)
\end{bmatrix}
\]

In addition, the cost function \( J \) can be constructed as

\[
J = \sum_{j=1}^{P} (\hat{Y}(k+j) - y(k+j))^2 + \sum_{j=1}^{M} \lambda(j) [\Delta U(k+j-1)]^2,
\]

where \( \lambda \) is the weighting coefficient. The controller of MPC is used to make the cost function minimal. To obtain the optimum control sequence, we can make the derivative of the cost function equal to zero:

\[
\frac{\partial J}{\partial \Delta U} = 0.
\]

Then, the solution of \( \Delta U(k) \) can be obtained. Moreover, by referring to the method in [23] and using the trial-and-error method, the prediction horizon length \( M \) and the control horizon length \( P \) are specified to be 10. The benchmarked cruise control and the proposed ECC are validated on the cosimulation platform of CarSim and Matlab/Simulink. With the cosimulation environment, the ECC and the benchmarked method are tested with different working points.

6. Control Performances of ECC Scheme

6.1. Control Performance at 40 km/h. To analyze the control performances of the proposed ECC and the benchmarked cruise control, the vehicle speed, the motor’s torque (including the driving torque and the braking torque), and the motor’s efficiency are analyzed in detail at 40 km/h when moving on the test road. The results are shown in Figure 10. The blue curve and the red curve in Figure 10(a), respectively, reflect the vehicle speed by the benchmarked cruise control and ECC. The vehicle speed has a little perturbation when moving on the test road. On uphill part, the vehicle speed decreases less by ECC than by the benchmarked cruise control, and on downhill part, the vehicle speed increases less by ECC than by the benchmarked cruise control. Therefore, it can be obviously observed that ECC is better than the benchmarked cruise control in speed maintenance ability. From Figure 10(b), one can know that the motor’s torques vary by different methods. Combining the speed profiles in Figure 10(a), we can find that the cruise speed by ECC has less fluctuation compared with that by the benchmarked cruise control, and most of the working points of the motor’s torque by ECC are in the small value interval. Therefore, the motor’s torque by ECC has less unreasonable actuation condition compared with that by the benchmarked cruise control. Figure 10(c) demonstrates the driving efficiency and the regenerative braking efficiency. According to the results in Figure 10(c), we can observe that at some sampling instances the motor’s efficiency by ECC is greater than that by the benchmarked cruise control, but at other sampling instances, the motor’s efficiency by ECC is lower than that shown in Figures 7 and 8, respectively. In Figure 7, the blue curves represent the real value, the dotted black curves represent the estimated value by RLS-MFF, the dash-dotted green curves represent the estimated value by EKF, and the dashed orange curves represent the estimated value by the original BVCIE. From the results in Figure 7, especially the zoom-in curves in Figure 7, it can be found that the original BVCIE outperforms RLS-MFF and EKF in estimation accuracy. However, in case of the input data loss, the estimation results by RLS-MFF, EKF, and original BVCIE have a sharp wind-up. Figure 8 depicts the estimated results by the improved BVCIE. The blue curves represent the real value, and the dashed magenta curves represent the estimated value. From the results in Figure 9, we can find that the estimated values have good performances and can accurately reflect the real values. In addition, the wind-up phenomenon can be eliminated when the input data are lost. From the local zoom-in curves in Figures 9(a) and 9(b), we know that there exists a little error between the estimated value and the real value. To analyze the deviation, the estimation errors in total mass and in pitch angle by the improved BVCIE are shown in Figures 9(a) and 9(b). Compared with the estimated values in Figures 8(a) and 8(b), the estimation errors are very small. In this condition, the vehicle’s state estimated by the method in Section 3 can be applied to the proposed ECC scheme in Section 4.

5.2. Results of Vehicle State Estimation. To analyze the performance of the improved BVCIE in Section 3, the test on the vehicle moving at 40 km/h is presented. In addition, the recursive least square method with multiple forgetting factors (RLS-MFF), the extended Kalman filter (EKF), and the original method, i.e., BVCIE, are adopted for comparison.

For the original BVCIE, RLS-MFF, and EKF and the improved BVCIE, the initial values of the estimated vehicle total mass and pinch angle are set to 0. The estimated total mass and the estimated pitch angle by the RLS-MFF, the EKF, the original BVCIE, and the improved BVCIE are
Figure 7: Estimation results by RLS-MFF, EKF, and BVCIE at 40 km/h on asphalt road. (a) Estimated total mass. (b) Estimated pitch angle.

Figure 8: Estimation results by the improved BVCIE at 40 km/h on asphalt road. (a) Estimated total mass. (b) Estimated pitch angle.

Figure 9: Estimation errors by the improved BVCIE at 40 km/h on asphalt road. (a) Estimation error in mass. (b) Estimation error in pitch angle.

Figure 10: Control performances and comparison of ECC and benchmarked cruise control. (a) Vehicle speed. (b) Motor’s torque. (c) Motor’s efficiency.
by the benchmarked cruise control. The reason for this phenomenon is that the motor drive system works in unreasonable actuation conditions at some sampling instances by the benchmarked cruise control. When the driving torque provided by the motor is smaller than the torque demands, the energy consumption by the benchmarked cruise control is less than that by ECC, but when the driving torque provided by the motor is greater than the torque demands, the energy consumption by the benchmarked cruise control is greater than that by ECC. In this condition, it is difficult to judge which method is better according to Figure 10(c). By referring to the analysis method in [41], the average driving efficiency and the average regenerative braking efficiency are introduced to compare the ECC and the benchmarked cruise control.

In addition, by referring to the analysis method in [42], the ride comfort can be assessed by vehicle’s jerk ($\vec{J}$), which is the second derivative of the vehicle’s longitudinal velocity. In the moving process, the jerk values include positive values and negative values. For this reason, we adopt the average absolute jerk to compare the ride comfort of ECC and the benchmarked cruise control. The smaller the average absolute jerk, the better the ride comfort. The average absolute jerk is defined as

$$|\vec{J}| = \frac{1}{N} \sum_{k=1}^{N} |\vec{v}(k)| \cdot (35)$$

The average driving efficiency, the average regenerative braking efficiency, and the average absolute jerk are shown in Table 2.

According to the results in Table 2, in the driving mode, the average driving efficiency by the benchmarked cruise control is significantly lower than that by ECC. In the braking mode, the average driving efficiency by ECC is similar to that by the benchmarked cruise control. Thus, ECC reasonably adjusts the motor’s torque so that the motor works in the high efficiency range. In addition, the average absolute jerk by ECC is smaller than that by the benchmarked cruise control. From the results in Table 2, we can conclude that the motor’s efficiency and the ride comfort by ECC outperform those by the benchmarked cruise control in the driving mode and braking mode.

### 6.2. Control Performance at 80 km/h

To demonstrate the performance of the proposed ECC at high cruise speed, the cruise speed of 80 km/h is investigated in this part. The vehicle speed, the motor’s torque, and the motor’s efficiency are presented in Figure 11. In Figure 11(a), it is obvious that the speed maintenance ability by ECC is still more excellent than that by the benchmarked cruise control. Figures 11(b) and 11(c), respectively, demonstrate the motor’s torque and the motor’s efficiency. Similar to the results in Figures 11(b) and 11(c), it is still difficult to distinguish which method is better. That is because sometimes the motor’s torque and the motor’s efficiency by ECC are greater than those by the benchmarked cruise control, but sometimes the motor’s torque and the motor’s efficiency by ECC are lower than those by the benchmarked cruise control. Therefore, we also calculate the average driving efficiency, the average regenerative braking efficiency, and the average absolute jerk, and they are shown in Table 3.

From Table 3, it can be found that in the driving mode, the driving efficiency by ECC is higher than that by the benchmarked cruise control. More importantly, the regenerative braking efficiency by ECC is also higher than that by the benchmarked cruise control. In addition, the average absolute jerk by ECC is still smaller than that by the benchmarked cruise control. Therefore, it can be concluded that ECC is better than the benchmarked cruise control at high cruise speed.

### 7. Energy Saving Performance Analysis

To demonstrate vehicle’s energy saving performance of the proposed ECC, the energy consumption of the two scenarios in Sections 6.1 and 6.2 is analyzed in detail. The energy consumption in the driving mode and the energy feedback in the braking mode are calculated as follows:

$$E_o = \int_{t_0}^{t_f} P_o(t)dt,$$

$$E_i = \int_{t_0}^{t_f} P(t)dt,$$

where $E_o$ refers to the energy consumption in the driving mode, $E_i$ refers to the energy feedback in the braking mode, and $t_f$ refers to the termination time.

The energy consumption and energy feedback of the two scenarios in Sections 6.1 and 6.2 are shown in Figures 12(a) and 12(b), respectively. When the test vehicle is moving at 40 km/h, the energy consumption by the ECC and that by the benchmarked cruise control are 0.2033 kWh and 0.1956 kWh, respectively. The energy feedback by ECC and the benchmarked cruise control is 0.0424 kWh and 0.0496 kWh, respectively. Obviously, it can be found that the vehicle consumes less energy by ECC when moving at 40 km/h compared with that by the benchmarked cruise control. For the high cruise speed of 80 km/h, the energy consumption by the ECC and by the benchmarked cruise control is 0.1709 kWh and 0.1583 kWh, respectively. In addition, the energy feedback by the ECC and by the benchmarked cruise control is 0.0472 kWh and 0.0483 kWh. The results in Figure 12(b) show the advantage of ECC because the vehicle not only consumes less energy in the driving mode, but also regenerates more energy in the braking mode.

For the two scenarios, the real energy consumption ($E$) in the whole process can be calculated as

<table>
<thead>
<tr>
<th>Control performances</th>
<th>Benchmark</th>
<th>ECC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Driving efficiency</td>
<td>0.5827</td>
<td>0.6468 x 100%</td>
</tr>
<tr>
<td>Regenerative braking efficiency</td>
<td>0.2790</td>
<td>0.2900 x 100%</td>
</tr>
<tr>
<td>Average absolute jerk</td>
<td>1.3964</td>
<td>1.1930 km/s²</td>
</tr>
</tbody>
</table>

Table 2: Motor’s average efficiency and ride comfort by the benchmarked cruise control and the proposed ECC (40 km/h).
To analyze the real energy consumption on the test road in detail, the cruise speeds of 40 km/h, 50 km/h, 60 km/h, 70 km/h, 80 km/h, 90 km/h, 100 km/h, and 110 km/h are selected to investigate ECC performance, and the proposed ECC is detailedly compared with the benchmarked cruise control. The total energy consumption on the test road at 40 km/h, 50 km/h, 60 km/h, 70 km/h, 80 km/h, 90 km/h, 100 km/h, and 110 km/h is shown in Figure 13. It is obvious that the test vehicle
Figure 13: Energy consumption at different cruise speeds. (a) At 40 km/h. (b) At 50 km/h. (c) At 60 km/h. (d) At 70 km/h. (e) At 80 km/h. (f) At 90 km/h. (g) At 100 km/h. (h) At 110 km/h.
consumes less energy in all cruise speeds by ECC compared with that by the benchmarked cruise control. The results in Figure 13 effectively prove that the proposed ECC has better performance in decreasing the energy consumption.

Furthermore, to compare the energy saving performance of the proposed ECC and the benchmarked cruise control, the state of charge (SOC) of the battery is adopted. Before implementing the simulation, the battery SOC is 100%. After the simulation, the battery SOC at 40 km/h, 50 km/h, 60 km/h, 70 km/h, 80 km/h, 90 km/h, 100 km/h, and 110 km/h is shown in Figure 14. The dotted blue line refers to the battery SOC by the benchmarked cruise control, and the solid red line refers to the battery SOC by the proposed ECC. It can be easily found that the battery SOC by the proposed method is higher than that by the benchmarked cruise control. Therefore, the proposed ECC outperforms the benchmarked cruise control in energy saving performance.

8. Conclusion

Motivated by the driving range limits of electric vehicles, this paper proposes an ECC to improve the energy utilization efficiency of electric vehicles. Different from the prevailing research, this paper focuses on the condition that the electric vehicle is moving on the slope road without using the digital map’s information and the GPS information. Additionally, energy saving is realized by reducing the unreasonable actuation of the motor’s torque. Compared with the benchmarked cruise control, the proposed ECC not only improves the electric vehicle’s speed maintenance ability and ride comfort, but also improves the energy efficiency. Moreover, different cruise speed tests indicate that the proposed ECC can obviously decrease the energy consumption, and the statistical results of the battery SOC show that the proposed ECC can improve the energy saving performance. The research in this paper provides a novel method to improve electric vehicles’ energy efficiency.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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