

Research Article

An Improved Harmony Search Algorithm for Power Distribution Network Planning

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Distribution network planning because of involving many variables and constraints is a multiobjective, discrete, nonlinear, and large-scale optimization problem. Harmony search (HS) algorithm is a metaheuristic algorithm inspired by the improvisation process of music players. HS algorithm has several impressive advantages, such as easy implementation, less adjustable parameters, and quick convergence. But HS algorithm still has some defects such as premature convergence and slow convergence speed. According to the defects of the standard algorithm and characteristics of distribution network planning, an improved harmony search (IHS) algorithm is proposed in this paper. We set up a mathematical model of distribution network structure planning, whose optimal objective function is to get the minimum annual cost and constraint conditions are overload and radial network. IHS algorithm is applied to solve the complex optimization mathematical model. The empirical results strongly indicate that IHS algorithm can effectively provide better results for solving the distribution network planning problem compared to other optimization algorithms.

1. Introduction

Distribution network planning can reduce the probability of blackouts, reduce transmission loss, and improve power quality, so that it is an important part of power distribution automation system. The main task of distribution network planning is to optimize network structure and find the optimal expansion scheme of power distribution network. The distribution network planning problem consists of minimizing investment and operation cost of the objective function subject to technical constraints, such as overload, voltage drop, and radial network. Distribution network expansion planning is a complex and large scale combinatorial optimization problem; the classical mathematical methods cannot perform satisfactorily for solving it [1–4]. Modern metaheuristic methods, such as Genetic Algorithm (GA), Particle Swarm Optimization (PSO), and Ant Colony System (ACS), are used recently to solve the distribution network planning problem and have achieved some results. However, the heuristic algorithms mentioned above have some defects: GA is a stochastic search algorithm for global optimization

problems. It can reduce the difficulty of solving distribution network planning which is a nonlinear, multiconstraint, and multiobjective problem [5]. But in the practical application of the distribution network planning, it always falls into local optimum prematurely and converging slowly; there may even be infeasible solutions; PSO is a classic biological intelligence algorithm and has some advantages over other similar optimization techniques such as PSO which is easier to implement and there are fewer parameters to adjust, but it is prone to premature convergence [6]; ACS is a swarm intelligence algorithm based on distributed parallel search mechanism. It has strong robustness, but it also has some defects such as long calculation time, prone to stagnation and premature convergence [7, 8].

HS algorithm is a heuristic search algorithm for global optimization, which has been recently developed in an analogy with music improvisation process where musicians in an ensemble continue to polish their pitches in order to obtain better harmony [9]. The algorithm has the advantages of simple concept and model, easy implementation, less adjustable parameters, and quick convergence. However, when to solve

the complex optimization problems, the standard HS algorithm still has some defects such as premature convergence. According to the defects of the standard algorithm and characteristics of distribution network planning, this paper proposed an improved harmony search (IHS) algorithm with the mechanism for dynamically adjusting parameters. We apply IHS algorithm to solve power distribution network planning. The simulation of example obviously shows that the solution is superior to that of other optimization algorithms.

2. Mathematical Model of Distribution Network Planning

In this paper, the model of distribution network planning adopts the objective function to minimize comprehensive costs per year, including the line investment expenses, the depreciation and maintenance costs, and the running year electrical energy loss expense. Considering overload constraints and radial network structure constraints, the objective function can be described as follows [10]:

$$\min f(x) = \begin{cases} \sum_{i=1}^n (C_{1i}T_i x_i + C_{2i}\tau_{\max i} \Delta P_i) + M_1 \times L, & \text{when the network is radial} \\ M_2, & \text{else,} \end{cases} \quad (1)$$

where $f(x)$ is the cost per year of distribution network planning; $C_{1i} = \gamma_i + \partial_i$, γ_i is the rate of return on investment; ∂_i is annual depreciation rate of equipment; T_i is the total investment for the i th newly built line; X is n -dimensional decision vectors; $X = (x_1, x_2, \dots, x_n)$ is the n transmission lines which is to be elected in the optimization problem. x_i is the element of X , $x_i = 1$ when the i th line is newly built, and $x_i = 0$ otherwise; C_{2i} is unit power price; $\tau_{\max i}$ is annual maximum load utilization hours; $\Delta P_i = (P_i^2 + Q_i^2)R_i/U_i^2$ is the active power loss of the i th line; M_1 is penalty coefficient of overload; L is the load which exceeds the total load demand of power system; M_2 is a very large penalty value when the network is not radial.

3. Harmony Search Algorithm

Harmony search (HS) algorithm is a relatively new meta-heuristic algorithm, which was proposed by Geem et al. [9]. Like other heuristic algorithms imitating natural phenomena or artificial ones, HS algorithm is also a heuristic algorithm mimicking the improvisation process of music players, where musicians improvise the pitches of their instruments to search for a perfect state of a harmony.

In HS algorithm, musical performances seek a perfect state of harmony determined by aesthetic estimation, as the optimization algorithms seek a global optimum determined by objective function value. Specifically, musical instrument i ($i = 1, 2, \dots, n$) is analogous to the i th decision vector of the optimization problems. Each tone of the instrument is analogous to each value of the decision variable. The harmony H_j ($j = 1, 2, \dots, n$) produced by musical instruments is analogous to the j th solution of the optimization problems.

Aesthetic evaluation is analogous to the objective function. The main control parameters of HS algorithm are harmony memory (HM), Harmony Memory Size (HMS), Harmony Memory Considering Rate (HMCR), Pitch Adjusting Rate (PAR), and Band Width (BW). Here, HM is a memory location where all the solution vectors are stored; HMCR and PAR are parameters that are used to improve the solution vector [11].

In the process of iteration, each new harmony vector $x^{\text{new}} = (x_1^{\text{new}}, x_2^{\text{new}}, \dots, x_n^{\text{new}})$ is generated based on three rules: (i) memory consideration, (ii) pitch adjustment, and (iii) random selection. Generating a new harmony is called "improvisation" [11]. In the memory consideration, the value of each component is updated as follows:

$$x_i^{\text{new}} = \begin{cases} x_i^j, & j \in (1, 2, \dots, \text{HMS}), \text{rand}_1 < \text{HMCR} \\ x_i \in X_i, & \text{else,} \end{cases} \quad (2)$$

where rand_1 is a random number uniformly distributed in the range of $[0, 1]$ and X_i is the value space of the i th variable.

Each component obtained by the memory consideration is examined to determine whether it should be pitch-adjusted. The PAR parameter is the rate of pitch-adjustment. The equation of pitch-adjustment can be described as follows:

$$x_i^{\text{new}} = \begin{cases} x_i^j \pm \text{rand}_2 * \text{BW}, & \text{rand}_2 < \text{PAR (when } x_i \text{ is continuous)} \\ x_i(k+m), & \text{rand}_2 < \text{PAR (when } x_i \text{ is discrete)} \\ x_i^{\text{new}}, & \text{else,} \end{cases} \quad (3)$$

where rand_2 is a random number uniformly distributed in the range of $[0, 1]$ and m is a constant, which belongs to the $(-1, 1)$.

4. Improved Harmony Search Algorithm

4.1. *HMCR*. $\text{HMCR} \in [0, 1]$ determines whether the value of a decision variable is to be chosen from HM. In order to ensure that the algorithm can quickly find local optima in the early operation and the solutions obtained in the later are diverse, this paper adopts the following linear decreasing strategy to update HMCR [12]:

$$\text{HMCR}(t) = \text{HMCR}_{\max} - \frac{(\text{HMCR}_{\max} - \text{HMCR}_{\min}) * t}{T_{\max}}, \quad (4)$$

where t denotes iteration number; T_{\max} is the maximum total number of iterations; HMCR_{\max} and HMCR_{\min} represent maximum and minimum harmony memory considering rate, respectively.

4.2. *PAR*. In HS algorithm, PAR plays a role in controlling local search. The appropriate PAR can avoid the search being trapped in local optimum effectively. Normally, the smaller

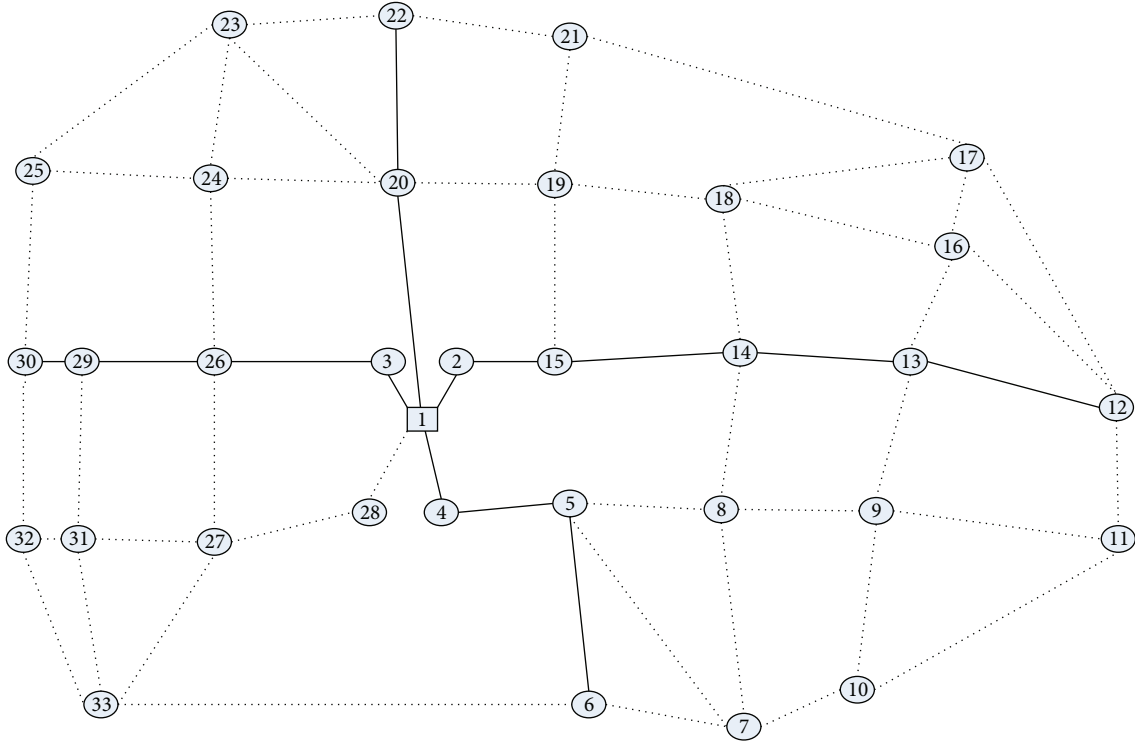


FIGURE 1: The existing network.

PAR is beneficial to quickly find the local optimal solution in early search stage, while the larger PAR is propitious to jump out the local optimal in the later stage. Therefore, dynamic change strategy for PAR is incorporated into the algorithm in this paper; the mathematical expression for PAR is

$$\text{PAR}(t) = \frac{\text{PAR}_{\max} - \text{PAR}_{\min}}{\pi/2} * \arctan t + \text{PAR}_{\min}, \quad (5)$$

where $\text{PAR}(t)$ denotes pitch adjusting rate for the t th generation; PAR_{\max} and PAR_{\min} represent maximum and minimum harmony memory considering rate, respectively.

4.3. *BW*. The appropriate BW can be potentially useful in adjusting convergence rate of algorithm to optimal solution. In this paper, BW changes from large to small. BW changes dynamically with generation number as expressed as follows:

$$\text{BW}(t) = \text{BW}_{\max} - \frac{\text{BW}_{\max} - \text{BW}_{\min}}{T_{\max}} * t, \quad (6)$$

where $\text{PAR}(t)$ denotes pitch band width for the t th generation; BW_{\max} and BW_{\min} represent maximum and minimum harmony memory considering rate, respectively.

4.4. *The Optimization Steps after Algorithm Improved*. The optimization steps are summarized in the following.

Step 1. Initialize the HS algorithm parameters. Initialize the maximum number of iterations T_{\max} ; the harmony memory

size (HMS), the maximum and minimum harmony memory considering rate, HMCR_{\max} and HMCR_{\min} ; the maximum and minimum pitch adjusting rate, PAR_{\max} and PAR_{\min} ; the maximum and minimum band width, BW_{\max} and BW_{\min} .

Step 2. Initialize the harmony memory (HM).

Step 3. Improvise a new harmony from the HM. Use (2), (3), (4), (5), and (6) to improvise a new harmony.

Step 4. Update the HM. Use (1) to evaluate fitness of the new harmony. If the new harmony is better than the worst harmony in the HM, the worst harmony is excluded from the HM and the new harmony is included in the HM.

Step 5. Inspect termination condition. The IHS will be terminated if the number of iterations meets the maximum number of iterations T_{\max} . Else go to Step 3.

5. Example Analysis

In this paper, the proposed method for optimal distribution network planning is applied to a 10 kV distribution system in a northern Chinese city using MATLAB 2011b. The network consists of a power supply point (110 KV substation), 32 load points, and 12 existing lines. 18 new load points are added to the existing network. The existing network is shown in Figure 1, in which the solid lines denote the existing lines and the dotted line denotes the expandible line. The coordinates and power of each load point are shown in Table 1.

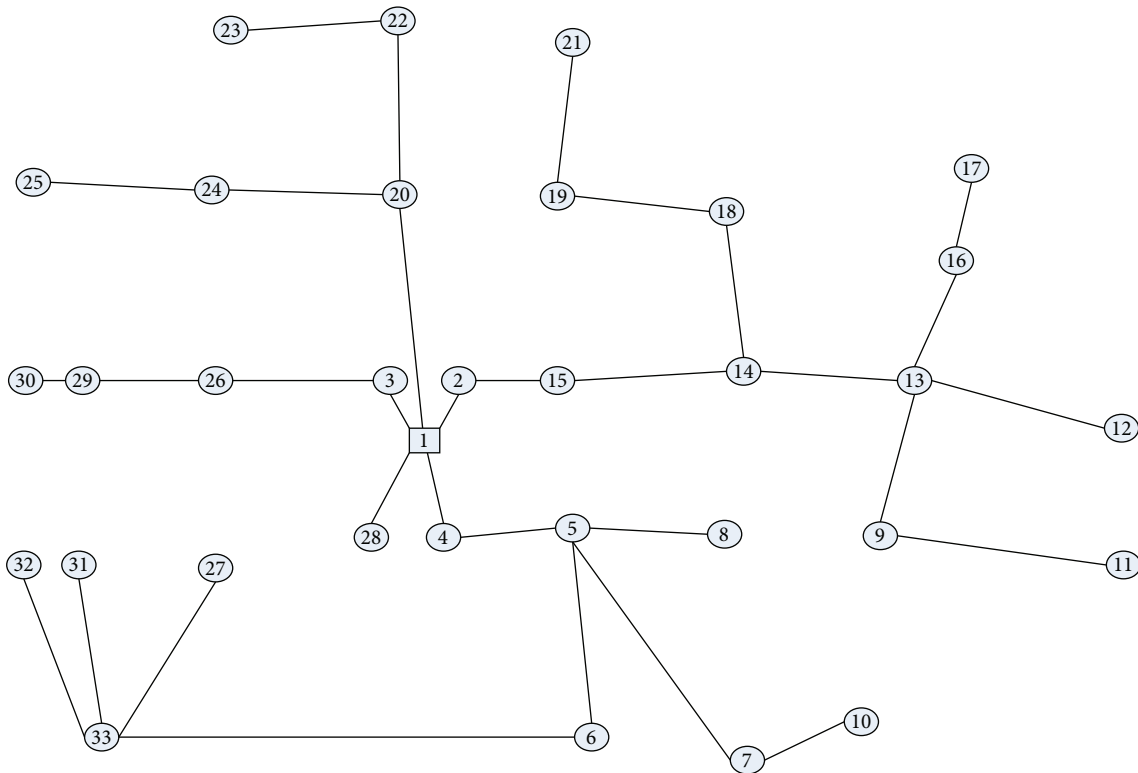


FIGURE 2: The optimal distribution network planning based on the HIS algorithm.

Using the improved algorithm to optimize the distribution network planning mentioned above, the input parameters are set as follows: $C_{1i} = 0.155$, $C_{2i} = 0.05$ yuan/KWh, $\tau_{\max i} = 3000$ h, $HMS = 30$, $HMCR_{\max} = 0.95$, $HMCR_{\min} = 0.6$, $PAR_{\max} = 0.99$, $PAR_{\min} = 0.01$, $BW_{\max} = 1.0$, $BW_{\min} = 0.0001$, and $T_{\max} = 1000$. The optimal distribution network planning based on the HIS algorithm is shown in Figure 2.

For further analysis, the IHS algorithm proposed in this paper, HS from [13], PSO from [14], Artificial Fish Swarm Algorithm (AFSA) from [15], Improved Ant Colony algorithm (IAC) from [16], Cross-Entropy Method (CE) [17–19], and two typical evolutionary multiobjective optimization algorithms, Nondominated Sorting Genetic Algorithm version II (NSGA-II) [20–22] and Multiobjective Particle Swarm Optimization Algorithm (MOPSO) [23–25], are compared in optimizing the power network planning. In the case study, 50 independent runs were made for each of the optimization methods involving 50 different initial trial solutions for each optimization method. The parameters of each optimization method are shown in Table 2. The comparison results are shown in Table 3.

Comparing the results of Table 3, it can be found that the best solution (minimum cost) obtained by IHS algorithm is better than that of any other method. In terms of best solution and average optimal solution, it is very evident that the IHS algorithm proposed in this paper is superior to HS, PSO, AFSA, IAC, CE, NSGA-II, and MOPSO. This suggests that IHS algorithm has very strong stability and robustness. When to solve the multiobjective distribution network planning

problem, the two typical evolutionary multiobjective optimization algorithms: NSGA-II and MOPSO are significantly superior to the HS, PSO, AFSA, IAC, and CE in terms of stability and robustness. But long execution times for these algorithms suggest that they reach the solution at a very slow speed. Though IHS algorithm obtained slightly better minimum cost and average cost than MOPSO, the average execution time used by IHS algorithm is less than that of MOPSO obviously. From the point of execution time, the average execution time of IHS algorithm is the minimum except CE. Although the execution time of CE is less than that of IHS algorithm, the best solution and average optimal solution obtained by the IHS algorithm are significantly better than that of CE. The reasonable average execution time of IHS algorithm suggests that IHS algorithm is capable of reaching the solution at a very high speed. Therefore, it can be concluded that IHS not only has found the highest quality results among all the algorithms compared, but also possesses greater stability and better robustness to solve such kinds of distribution network planning problem. IHS algorithm is an effective method to solve the distribution network planning problem.

6. Conclusion

Distribution network planning is a multiobjective, discrete, nonlinear, and large-scale optimization problem. This paper proposes an improved harmony search (IHS) algorithm to solve the distribution network planning problem. The

TABLE 1: The coordinates and state of load points.

Number	Abscissa (m)	Ordinate (m)	Load (KVA)
1	2463.4	801.7	substation
2	2462.5	808.4	500
3	2457.1	807.9	400
4	2460.6	773.3	200
5	2481.4	775.3	600
6	2477.5	728.8	800
7	2503.2	724.5	400
8	2503.7	772.8	200
9	2530.8	773.4	500
10	2528.5	730.3	800
11	2572.3	778	400
12	2573.6	799.9	600
13	2533.6	807.7	500
14	2508.3	809.4	400
15	2478.7	808.2	200
16	2535.4	837.5	500
17	2537.7	854.4	1000
18	2507	844.7	400
19	2478.5	849	500
20	2455.2	849.4	800
21	2481.4	871.9	600
22	2455.9	873.5	600
23	2434	873	200
24	2433.5	850	200
25	2404.2	851.1	1000
26	2433.9	807.8	500
27	2434.3	775.2	800
28	2456.5	776.3	400
29	2417.6	808.3	200
30	2403.5	808	200
31	2416.4	774.6	600
32	2403.5	773.7	1000
33	2421.3	729.7	200

TABLE 2: The parameters of each optimization method.

Algorithms	Parameters
HS	HMS = 30, HMCR = 0.95, PAR = 0.05, BW = 0.06
PSO	$c_1 = 2, c_2 = 2, w_{\max} = 0.9, w_{\min} = 0.4, \text{population} = 40$
AFSA	Step = 0.3, visual = 1.8, $\delta = 0.618, A_q = 0.9, c = 0.85, t_0 = 50, \text{population} = 50$
IAC	$C = 0.5, a = 1.003, \rho = 0.7, \text{population} = 300$
CE	$P = 0.01, \text{tol} = 0.15, p_0 = 0.5, N = 50$
NSGA-II	$p_c = 0.8, p_m = 0.33, \eta_c = 2, \eta_m = 20, \text{QUOTE } T_{\max} = 500, \text{population} = 200$
MOPSO	$w_0 = 0.35, w_1 = 1.0, \beta = 0.1, \gamma = 0.6, N = 100, T_{\max} = 250, \text{population} = 100$

TABLE 3: The comparison results of distribution network planning for some optimization algorithm.

Algorithms	Best solution/ 10^8 \$	Average optimal solution/ 10^8 \$	Average execution time/s
HS	1.1005	1.2061	70.83
PSO	1.1090	1.2162	71.25
AFSA	1.0746	1.1860	80.61
IAC	1.0772	1.1560	65.34
CE	1.1108	1.2307	53.05
NSGA-II	1.0487	1.1452	108.32
MOPSO	1.0441	1.1367	104.19
IHS	1.0432	1.1358	54.58

parameters of basic HS algorithm are specifically improved for distribution network planning problem. The improved method can improve the global search ability and prevent basic HS algorithm into a local optimum. And the improved algorithm has a fast calculation and a good convergence. The numerical example shows that HIS algorithm not only can obtain the highest quality results but also possesses greater stability and better robustness. It is obvious that IHS can acquire satisfactory solution for distribution network planning.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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