

## Research Article

# Effects of Single Doping and Composite Doping of Yttrium and Antimony on the Structural, Thermodynamic, Mechanical, and Electronic Properties of $Mg_2Si$ by First Principles

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Received 28 May 2018; Accepted 15 October 2018; Published 10 March 2019

Academic Editor: Stefano Bellucci

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The structural, stability, thermodynamic, mechanical, and electronic properties of Y and Sb doped into  $Mg_2Si$  were studied by first principles. The results show that the stable structures are  $Mg_7Si_4Y$ ,  $Mg_8Si_4Sb$ ,  $Mg_6Si_4YSb$ , and  $Mg_7Si_4YSb$ .  $Mg_8Si_4Sb$  has the largest ductility among them. Y doping causes strong orbital hybridization between Mg (2p) and Y (4d), while Sb doping causes strong orbital hybridization between Mg (2p), Si (3p), and Sb (5p). However, the thermal conductivity and hardness of  $Mg_2Si$  will be reduced by Y and Sb doping. The conductivity of  $Mg_8Si_4Sb$  is the best. The anisotropy of the {100}, {010}, and {001} surfaces will increase once doped with Y or Sb.  $Mg_8Si_4Sb$  has the highest degree of anisotropy.

## 1. Introduction

The 6xxx series aluminum alloy is widely used in automobile manufacturing because of its excellent qualities, such as reduced weight and good corrosion resistance [1, 2].  $Mg_2Si$  is the main strengthening phase [3] of the 6xxx series Al alloy, and it possesses a low density and high melting point and impedes grain boundary sliding [4–9]. However, the application of the 6xxx series Al alloy is limited due to its brittleness. This is due to the  $Mg_2Si$  phase which is the preferred phase to form coarse Chinese script or dendritic morphology [10–12]. To improve the mechanical properties of  $Mg_2Si$ , many alloying elements (such as Bi, As, and Sn [13–20]) are doped. Recently, Y and Sb doping into the  $Mg_2Si$  phase was considered. Zhang and Zhang [21] found that the fine modification effect of Y on the primary  $Mg_2Si$  phase is better than that of an equal amount of mixed light rare earth, and it can greatly refine the  $Mg_2Si$  grains and improve the tensile strength and elongation. Emamy et al. [22] found that the addition of Y increases both the hardness and ultimate tensile strength values of the Al-15% $Mg_2Si$  cast

composite. Jiang et al. [23] systematically investigated the modification of in situ-formed  $Mg_2Si$  in Mg–Si alloys with yttrium (Y). Ioannou et al. [24] have prepared Sb-doped  $Mg_2Si$  compounds through ball milling and a solid-state reaction. Hu et al. [25] found that Sb doping can change the type of Chinese script of  $Mg_2Si$  to a fine polygonal shape and decrease the grain sizes. Tani and Kido [26] studied the formation energy and atomic structure of impurities in  $Mg_2Sn$  using first-principles plane-wave total energy calculations. The thermoelectric properties of trace Y-doped  $Mg_2Si$  crystals have been obtained by experiments, and the total energies of  $Mg_7Si_4Y$ ,  $Mg_8Si_3Y$ , and  $Mg_8Si_4Y$  crystals have also been calculated [27]. What are the differences between the single doping and composite doping of Y and Sb? What are the micromechanisms of Y and Sb doping into  $Mg_2Si$ ? At present, there is no theoretical research on the brittleness of  $Mg_2Si$  by Y and Sb codoping as far as we know.

In this work, the structural, thermodynamic, and mechanical properties of Y and Sb doped into  $Mg_2Si$  were studied by first principles. It will provide a theoretical

reference for further research on  $\text{Mg}_2\text{Si}$  and 6xxx series aluminum alloys.

**1.1. Computational Models and Methods.**  $\text{Mg}_2\text{Si}$  has an anti-fluorite ( $\text{CaF}_2$ ) structure [28] (see Figure 1). The atomic coordinates are as follows: Mg (0.25, 0.25, 0.25) and Si (0, 0, 0).

For Y and Sb single doping, the positions of the Mg (or Si) atoms are replaced by Y or Sb, respectively. Despite that both the atom sizes of Y and Sb are larger than those of Mg and Si atoms, to avoid omitting certain configurations, the interpolation Y or Sb atoms into the interval of Mg and Si was considered (see Figure 2).

For the composite doping of Y and Sb, the Mg and (or) Si atoms are replaced by Y and Sb, respectively. Y or Sb enters into the interstitial space of the  $\text{Mg}_2\text{Si}$  cell, and Sb or Y replaces the Mg and (or) Si atoms (see Figure 3).

The hypothetical structures of Y- and Sb doping or codoping  $\text{Mg}_2\text{Si}$  configurations must be optimized. The calculations were performed using the CASTEP package based on the density functional theory (DFT) [29]. The exchange-correlation energy functional was adopted by Perdew, Burke, and Ernzerhof (PBE) from the generalized gradient approximation (GGA) [30]. The plane-wave cutoff energy was set to 340 eV. The Brillouin zone was sampled using a Monkhorst-Pack k-point mesh as follows:  $4 \times 3 \times 4$  for (j)  $\text{Mg}_8\text{Si}_2\text{YSb}$ , (l)  $\text{Mg}_8\text{Si}_3\text{YSb}$ , and (m)  $\text{Mg}_8\text{Si}_4\text{YSb}$  and the rest are  $4 \times 4 \times 4$ . To find the lowest energy structures of Y- and Sb-doped  $\text{Mg}_2\text{Si}$  phases, we observe the following convergence thresholds for geometry optimization: total energy convergence tolerance  $1.0 \times 10^{-5}$  eV/atom steps, 0.03 eV/Å for maximum force, 0.05 GPa for maximum stress components, and  $1 \times 10^{-3}$  Å for maximum displacement. After the optimization, the electronic properties are calculated. The density of states (DOS) is computed by means of a scheme developed by Ackland, while the DOS calculation is based on a Mülliken population analysis with the relative contribution of each atom.

## 2. Results and Discussion

**2.1. Structures.** The optimized lattice parameters of the pure  $\text{Mg}_2\text{Si}$  phase and Y- and Sb-doped  $\text{Mg}_2\text{Si}$  phases are shown in Table 1. It can be seen that the lattice parameters of  $\text{Mg}_2\text{Si}$  are in agreement with the experimental values [31–33]. Y- and Sb-doped  $\text{Mg}_2\text{Si}$  phases have larger lattice parameters and larger volume than the pure  $\text{Mg}_2\text{Si}$  phase. It is due to the lattice distortion of the  $\text{Mg}_2\text{Si}$  phase by Y and (or) Sb doping which possesses a larger atomic radius.

**2.2. Thermodynamic Properties.** In order to understand the thermodynamic stability of the doped system, we calculated the formation energy and cohesive energy. The calculated formation energy and cohesive energy of the  $\text{Mg}_2\text{Si}$  phase agree well with the calculated values ( $-25.92$  kJ/mol and  $-271.15$  kJ/mol in [34] and  $-17.7$  kJ/mol and  $-299.27$  kJ/mol in [35]). The process of Y and Sb doping of  $\text{Mg}_2\text{Si}$  is outlined in Table 2.

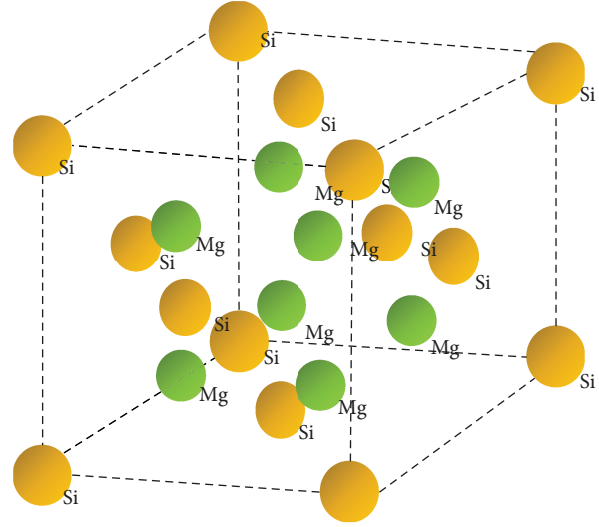


FIGURE 1: The crystal structure of  $\text{Mg}_2\text{Si}$ .

The corresponding formation energies are shown in Figure 4. It can be seen that the formation energies of (a)  $\text{Mg}_7\text{Si}_4\text{Y}$ , (c)  $\text{Mg}_8\text{Si}_4\text{Y}$ , (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$ , (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$ , (i)  $\text{Mg}_7\text{Si}_4\text{YSb}$ , (m)  $\text{Mg}_8\text{Si}_4\text{YSb}$ , and (n)  $\text{Mg}_7\text{Si}_4\text{YSb}$  are negative, indicating that only the structures above are stable. The formation energy is successively (m) < (i) < (n) < (c) < (f) < (g) < (a). It means that (m)  $\text{Mg}_8\text{Si}_4\text{YSb}$  is the easiest to form and (a)  $\text{Mg}_7\text{Si}_4\text{Y}$  is the most difficult to form. Whether for single doping or composite doping, the formation energies of Y and Sb entered into the interstitial space < the formation energies of Y and Sb replaced the Mg sites < the formation energies of Y and Sb replaced the Si sites (even if it cannot form stable structures). It confirms that Y or Sb is difficult to interpolate into  $\text{Mg}_2\text{Si}$  phases. For the seven stable structures of (a), (c), (f), (g), (i), (m), and (n), the formation energies of composite doping are generally smaller than those of single doping. Only the formation of (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  is greater than those of (c)  $\text{Mg}_8\text{Si}_4\text{Y}$  and (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$ ; this is because Y and Sb in (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  has replaced all the Mg sites to form substitutional solid solutions.

For the stable structures (a), (c), (f), (g), (i), (m), and (n), the calculated cohesive energies are shown in Figure 5. It can be seen that the absolute value of (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  is the largest, indicating that (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  is more stable than the other six structures and (m)  $\text{Mg}_8\text{Si}_4\text{YSb}$  has the smallest absolute value and the worst stability. Whether by single doping or composite doping, the structures of Y- or Sb-substituted Mg sites are most stable, while the structures of Y or Sb that entered into the interstitial space are most unstable.

**2.3. Mechanical Properties.** To satisfy the mechanical stability of the formed structures, the elastic constants of  $\text{Mg}_2\text{Si}$ , (a), (c), (f), (g), (i), (m), and (n) are calculated as shown in Table 3. (a)  $\text{Mg}_7\text{Si}_4\text{Y}$ , (c)  $\text{Mg}_8\text{Si}_4\text{Y}$ , and (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$  are still cubic structures, (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  and (m)  $\text{Mg}_8\text{Si}_4\text{YSb}$  are transformed into tetragonal structures, and (i)  $\text{Mg}_7\text{Si}_4\text{YSb}$

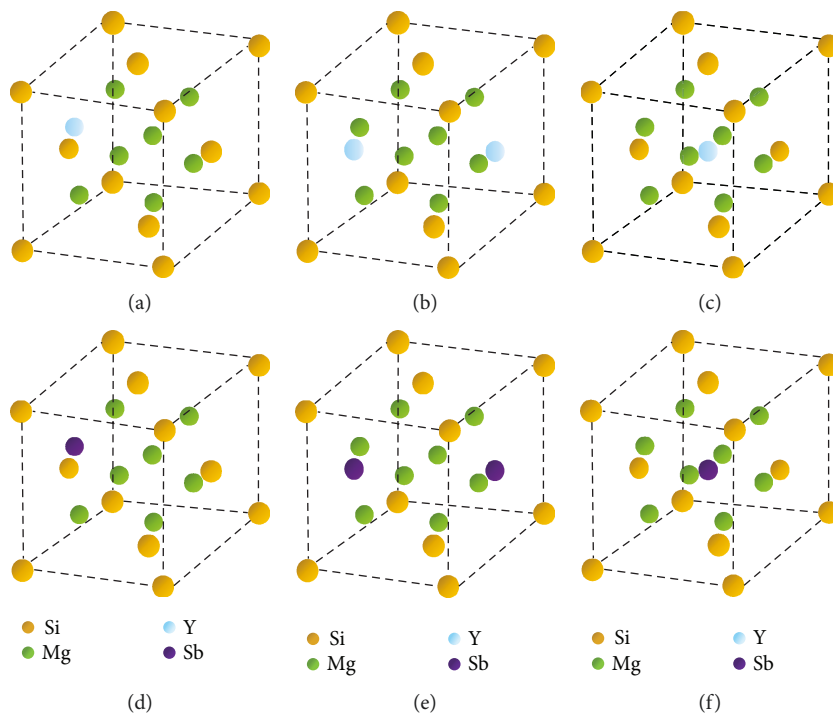


FIGURE 2: The structures of single doping.

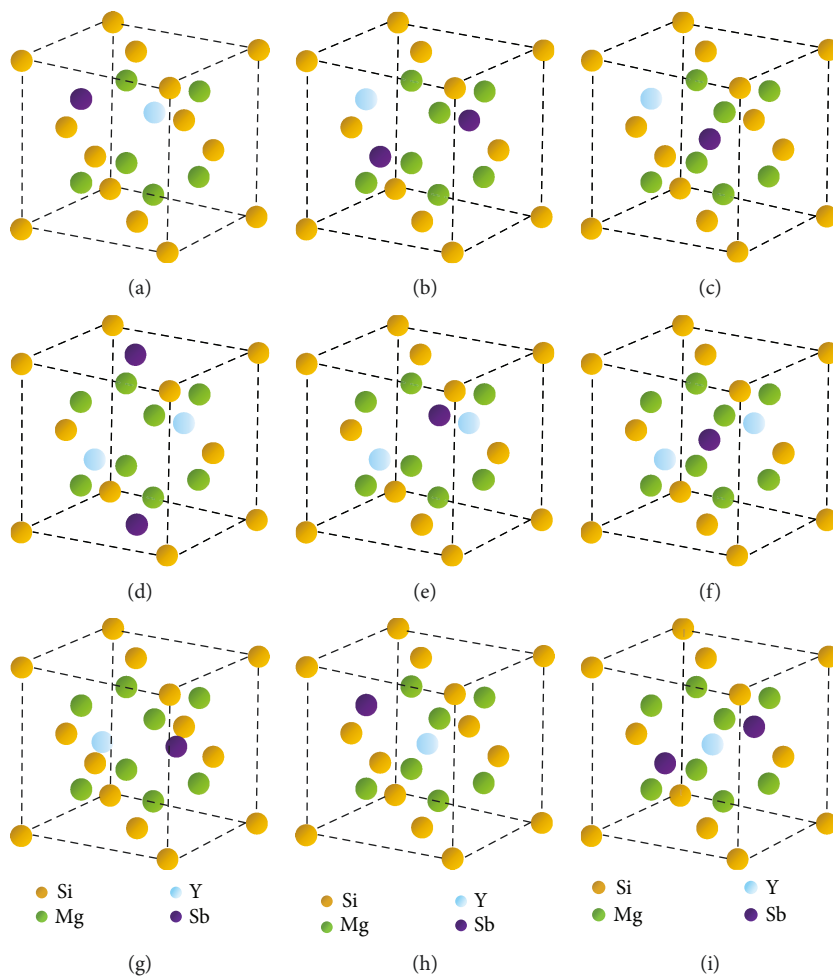


FIGURE 3: The structures of composite doping.

TABLE 1: The optimized lattice parameters for Y and (or) Sb doping of  $Mg_2Si$ .

Phase	Lattice constants (nm)	Cell volume ( $nm^3$ )	Ref.
$Mg_8Si_4$	$a = 0.633$	$V = 0.254$	
	$a = 0.639$	$V = 0.261$	[31]
	$a = 0.635$	$V = 0.256$	[32]
	$a = 0.634$	$V = 0.255$	[33]
(a) $Mg_7Si_4Y$	$a = 0.643$	$V = 0.266$	
(b) $Mg_8Si_3Y$	$a = 0.637$ $b = 0.687$ $c = 0.687$	$V = 0.301$	
(c) $Mg_8Si_4Y$	$a = 0.653$	$V = 0.278$	
(d) $Mg_7Si_4Sb$	$a = 0.640$	$V = 0.263$	
(e) $Mg_8Si_3Sb$	$a = 0.645$ $b = 0.643$ $c = 0.643$	$V = 0.267$	
(f) $Mg_8Si_4Sb$	$a = 0.656$	$V = 0.282$	
(g) $Mg_6Si_4YSb$	$a = 0.659$ $b = 0.629$ $c = 0.659$	$V = 0.273$	
(h) $Mg_7Si_3YSb$	$a = 0.654$ $b = 0.655$ $c = 0.655$	$V = 0.280$	
(i) $Mg_7Si_4YSb$	$a = 0.662$	$V = 0.290$	
(j) $Mg_8Si_2YSb$	$a = 0.607$ $b = 0.833$ $c = 0.607$	$V = 0.307$	
(k) $Mg_7Si_3YSb$	$a = 0.741$ $b = 0.647$ $c = 0.649$	$V = 0.273$	
(l) $Mg_8Si_3YSb$	$a = 0.615$ $b = 0.820$ $c = 0.604$	$V = 0.304$	
(m) $Mg_8Si_4YSb$	$a = 0.662$ $b = 0.787$ $c = 0.662$	$V = 0.345$	
(n) $Mg_7Si_4YSb$	$a = 0.662$	$V = 0.289$	
(o) $Mg_8Si_3YSb$	$a = 0.643$ $b = 0.690$ $c = 0.661$	$V = 0.293$	

TABLE 2: The process of Y and Sb doping of  $Mg_2Si$ .

Reactants		Products	
$Mg_8Si_4$	Y	→	(a) $Mg_7Si_4Y$ Mg
$Mg_8Si_4$	Y	→	(b) $Mg_8Si_3Y$ Si
$Mg_8Si_4$	Y	→	(c) $Mg_8Si_4Y$
$Mg_8Si_4$	Sb	→	(d) $Mg_7Si_4Sb$ Mg
$Mg_8Si_4$	Sb	→	(e) $Mg_8Si_3Sb$ Si
$Mg_8Si_4$	Sb	→	(f) $Mg_8Si_4Sb$
$Mg_8Si_4$	Y Sb	→	(g) $Mg_6Si_4YSb$ Mg Mg
$Mg_8Si_4$	Y Sb	→	(h) $Mg_7Si_3YSb$ Mg Si
$Mg_8Si_4$	Y Sb	→	(i) $Mg_7Si_4YSb$ Mg
$Mg_8Si_4$	Y Sb	→	(j) $Mg_8Si_2YSb$ Si Si
$Mg_8Si_4$	Y Sb	→	(k) $Mg_7Si_3YSb$ Mg Si
$Mg_8Si_4$	Y Sb	→	(l) $Mg_8Si_3YSb$ Si
$Mg_8Si_4$	Y Sb	→	(m) $Mg_8Si_4YSb$
$Mg_8Si_4$	Y Sb	→	(n) $Mg_7Si_4YSb$ Mg
$Mg_8Si_4$	Y Sb	→	(o) $Mg_8Si_3YSb$ Si

and (n)  $Mg_7Si_4YSb$  are transformed into triclinic structures. The mechanical stability of the phases above can be judged by the criterion for cubic, tetragonal, and triclinic systems in References [36] and [37]. Only  $Mg_2Si$ , (a)  $Mg_7Si_4Y$ , (f)  $Mg_8Si_4Sb$ , (g)  $Mg_6Si_4YSb$ , and (i)  $Mg_7Si_4YSb$  satisfies the criteria of mechanical stability.

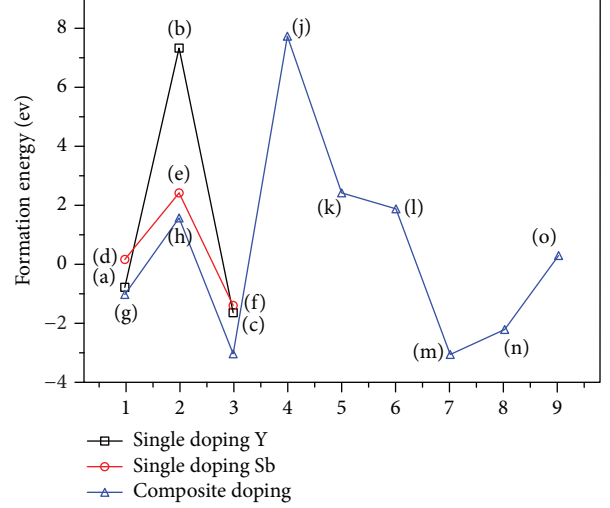


FIGURE 4: The formation energies of single doping and composite doping.

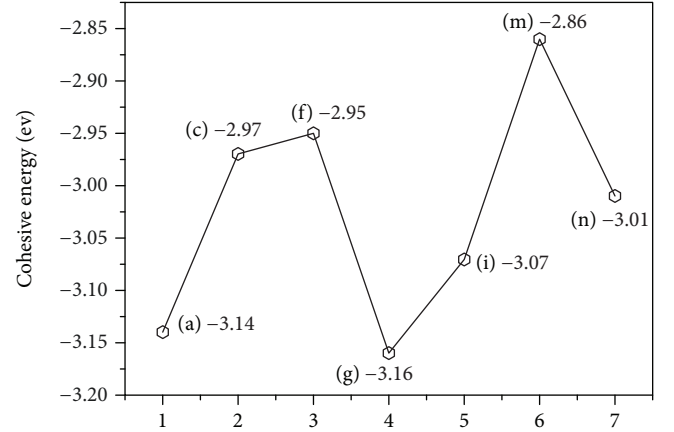


FIGURE 5: The cohesive energies of single doping and composite doping.

The calculated bulk modulus, shear modulus, and Young's modulus (51.23 GPa, 51.50 GPa, and 115.85 GPa) of  $Mg_2Si$  agree well with the calculated results (57.88 GPa, 48.82 GPa, and 114.32 GPa [38]). Young's modulus calculated for  $Mg_2Si$ , (a)  $Mg_7Si_4Y$ , (f)  $Mg_8Si_4Sb$ , (g)  $Mg_6Si_4YSb$ , and (i)  $Mg_7Si_4YSb$  are shown in Figure 6. No matter with what kind of doping, Young's modulus of pure  $Mg_2Si$  will decrease significantly. It means that  $Mg_2Si$  has the highest stiffness. In other words, Y and Sb doping will improve the plasticity of  $Mg_2Si$ . For single doping, Young's modulus of doped Sb is lesser than that of doped Y. This shows that the plasticity of (f)  $Mg_8Si_4Sb$  is better than that of (a)  $Mg_7Si_4Y$ , and the stiffness of (a)  $Mg_7Si_4Y$  is larger than that of (f)  $Mg_8Si_4Sb$ . For composite doping, Young's modulus of (g)  $Mg_6Si_4YSb$  is less than Young's modulus of (i)  $Mg_7Si_4YSb$ . This shows that the plasticity of (g)  $Mg_6Si_4YSb$  is better than that of (i)  $Mg_7Si_4YSb$ , and the stiffness of (g)  $Mg_6Si_4YSb$  is lesser than that of (i)  $Mg_7Si_4YSb$ .

The values of  $K/G$ , Poisson's ratio  $\nu$ ,  $A_U$ , and Debye temperature  $\Theta_D$  for  $Mg_2Si$ , (a)  $Mg_7Si_4Y$ , (f)  $Mg_8Si_4Sb$ , (g)

TABLE 3: The elastic constants for  $Mg_2Si$ , (a)  $Mg_7Si_4Y$ , (c)  $Mg_8Si_4Y$ , (f)  $Mg_8Si_4Sb$ , (g)  $Mg_6Si_4YSb$ , (i)  $Mg_7Si_4YSb$ , (m)  $Mg_8Si_4YSb$ , and (n)  $Mg_7Si_4YSb$ .

Phases	Elastic stiffness constants $C_{ij}$ (GPa)					
$Mg_2Si$	$C_{11} = 131.31$	$C_{12} = 11.19$	$C_{44} = 46.46$			
(a) $Mg_7Si_4Y$	$C_{11} = 106.00$	$C_{12} = 25.76$	$C_{44} = 29.00$			
(c) $Mg_8Si_4Y$	$C_{11} = 22.72$	$C_{12} = 60.54$	$C_{44} = 21.17$			
(f) $Mg_8Si_4Sb$	$C_{11} = 53.73$	$C_{12} = 40.66$	$C_{44} = 16.16$			
(g) $Mg_6Si_4YSb$	$C_{11} = 99.10$	$C_{12} = 26.56$	$C_{13} = 28.41$	$C_{33} = 99.21$	$C_{44} = 13.71$	$C_{66} = 13.03$
	$C_{11} = 96.36$	$C_{12} = 23.99$	$C_{13} = 24.26$	$C_{14} = -1.44$	$C_{15} = 2.91$	$C_{16} = -1.61$
	$C_{21} = 23.99$	$C_{22} = 96.44$	$C_{23} = 24.34$	$C_{24} = -1.78$	$C_{25} = 2.58$	$C_{26} = -1.05$
	$C_{31} = 24.26$	$C_{32} = 24.34$	$C_{33} = 96.63$	$C_{34} = -1.17$	$C_{35} = 1.69$	$C_{36} = -1.56$
	$C_{41} = -1.44$	$C_{42} = -1.78$	$C_{43} = -1.17$	$C_{44} = 21.21$	$C_{45} = -0.91$	$C_{46} = 1.69$
	$C_{51} = 2.91$	$C_{52} = 2.58$	$C_{53} = 1.69$	$C_{54} = -0.91$	$C_{55} = 19.72$	$C_{56} = -2.92$
(m) $Mg_8Si_4YSb$	$C_{61} = -1.61$	$C_{62} = -1.05$	$C_{63} = -1.56$	$C_{64} = 1.69$	$C_{65} = -2.92$	$C_{66} = 20.75$
	$C_{11} = 75.12$	$C_{12} = 20.81$	$C_{13} = 34.21$	$C_{33} = 75.02$	$C_{44} = -11.73$	$C_{66} = -9.39$
	$C_{11} = 52.86$	$C_{12} = 50.91$	$C_{13} = 51.14$	$C_{14} = -8.13$	$C_{15} = -3.89$	$C_{16} = 3.88$
	$C_{21} = 50.91$	$C_{22} = 53.37$	$C_{23} = 52.35$	$C_{24} = 2.55$	$C_{25} = 8.78$	$C_{26} = 1.21$
	$C_{31} = 51.14$	$C_{32} = 52.35$	$C_{33} = 52.71$	$C_{34} = 0.13$	$C_{35} = -0.49$	$C_{36} = -8.16$
	$C_{41} = -8.13$	$C_{42} = 2.55$	$C_{43} = 0.13$	$C_{44} = 21.38$	$C_{45} = -4.73$	$C_{46} = 4.06$
(n) $Mg_7Si_4YSb$	$C_{51} = -3.89$	$C_{52} = 8.78$	$C_{53} = -0.49$	$C_{54} = -4.73$	$C_{55} = 19.08$	$C_{56} = -3.33$
	$C_{61} = 3.88$	$C_{62} = 1.21$	$C_{63} = -8.16$	$C_{64} = 4.06$	$C_{65} = -3.33$	$C_{66} = 18.76$

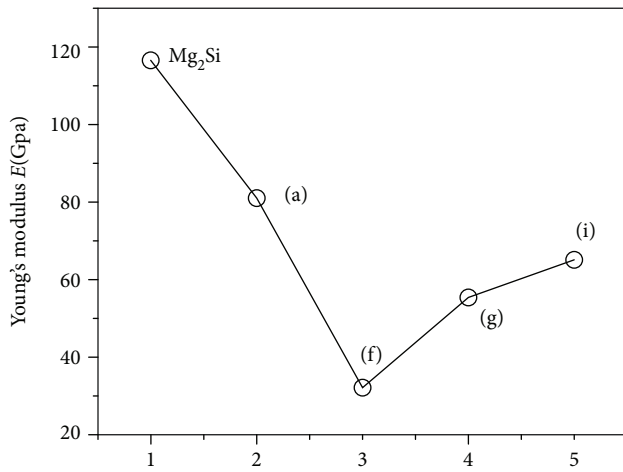


FIGURE 6: The results of Young's modulus.

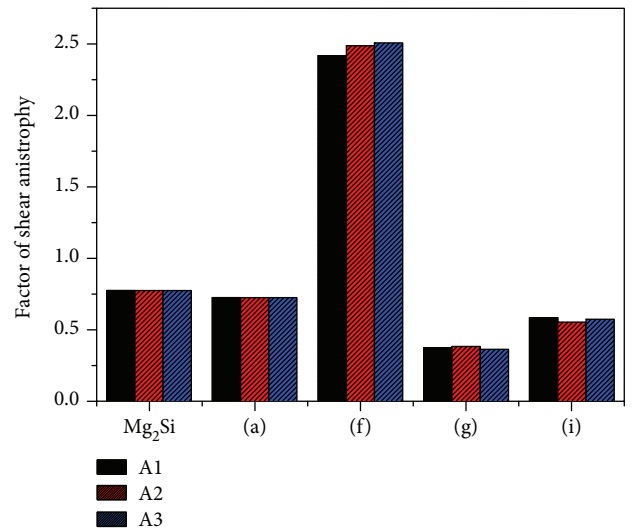


FIGURE 7: The results of shear anisotropy.

TABLE 4: The values of the  $K/G$ ,  $u$ ,  $A_U$ , and  $\Theta_D$  for  $Mg_2Si$ , (a)  $Mg_7Si_4Y$ , (f)  $Mg_8Si_4Sb$ , (g)  $Mg_6Si_4YSb$ , and (i)  $Mg_7Si_4YSb$ .

	$Mg_2Si$	(a) $Mg_7Si_4Y$	(f) $Mg_8Si_4Sb$	(g) $Mg_6Si_4YSb$	(i) $Mg_7Si_4YSb$
$K/G$	0.99	1.59	3.99	2.53	1.88
$u$	0.12	0.24	0.38	0.33	0.27
$A_U$	7.93	12.85	104.51	138.31	49.18
$\Theta_D$ (K)	600.23	445.60	248.77	331.88	346.11

$Mg_6Si_4YSb$ , and (i)  $Mg_7Si_4YSb$  are shown in Table 4. Poisson's ratio  $u$  (0.12) and Debye temperature  $\Theta_D$  (600.23 K) calculated for  $Mg_2Si$  agree with the results (0.161 and 581.6719 K [38]). From the values of  $K/G$ , it can be seen that the values of  $Mg_2Si$  and (a)  $Mg_7Si_4Y$  are less than the threshold value of 1.75, so  $Mg_2Si$  and (a)  $Mg_7Si_4Y$  are brittle materials, while (f)  $Mg_8Si_4Sb$ , (g)  $Mg_6Si_4YSb$ , and (i)  $Mg_7Si_4YSb$  are ductile materials.  $Mg_2Si$  has minimal  $K/G$  and has the worst brittleness, while (f)  $Mg_8Si_4Sb$  has maximal  $K/G$  and



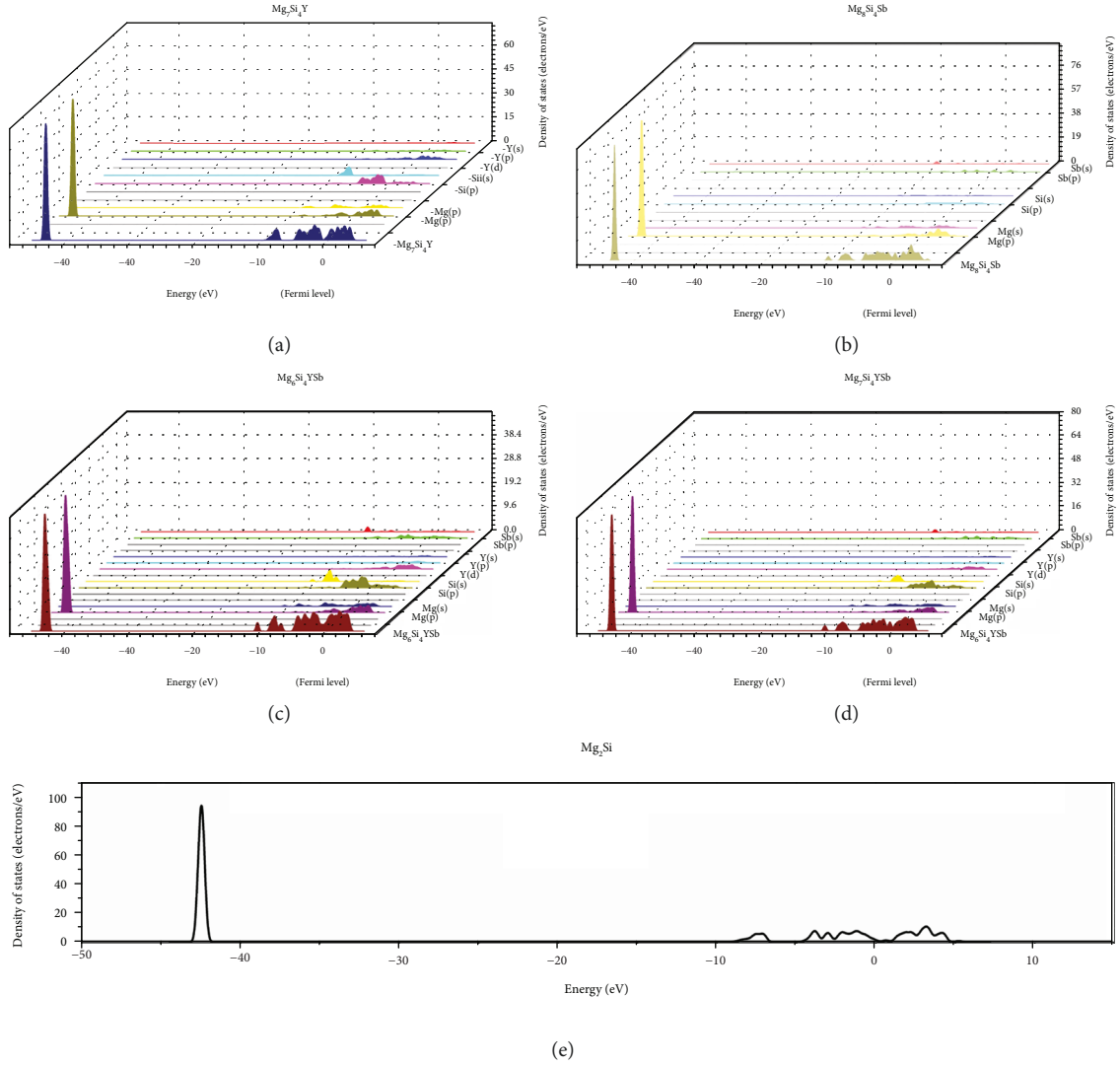


FIGURE 8: The total density of states (DOS) and the partial density of states (PDOS) for five structures.

has the greatest ductility. From the values of  $\mu$ , it can be seen that (f)  $Mg_8Si_4Sb$  has the best plasticity and  $Mg_2Si$  has the worst plasticity. The plasticity is successively (f)  $Mg_8Si_4Sb >$  (g)  $Mg_6Si_4YSb >$  (i)  $Mg_7Si_4YSb >$  (a)  $Mg_7Si_4Y >$   $Mg_2Si$ . From  $A_U$ , it can be seen that the five structures are all anisotropic and  $Mg_2Si$  has minimal value, so the degree of anisotropy is minimal. (g)  $Mg_6Si_4YSb$  has maximal value, and the degree of anisotropy is the highest. The degree of anisotropy of  $Mg_2Si$  will be raised by doped Y and Sb. From the values of  $\Theta_D$ , it can be seen that the Debye temperature ( $\Theta_D$ ) of  $Mg_2Si$  is the highest, which shows that the thermal conductivity of  $Mg_2Si$  is the best, the chemical bonds between the cell's atoms are the strongest, and the hardness is the greatest. (f)  $Mg_8Si_4Sb$  has the lowest Debye temperature ( $\Theta_D$ ), which shows that the thermal conductivity of (f)  $Mg_8Si_4Sb$  is the worst, the chemical bonds between the cell's atoms are the weakest, and the hardness is the least. Furthermore, no matter with what kind of doping, the Debye temperature ( $\Theta_D$ ) of  $Mg_2Si$  will be lowered. It is consistent with the calculated results of Debye temperature ( $\Theta_D$ ) [27].

The shear anisotropic factors  $A_1$ ,  $A_2$ , and  $A_3$  are shown in Figure 7. It can be found that the five structures are all anisotropic on the three planes, and the degree of anisotropy on each plane is very similar. (f)  $Mg_8Si_4Sb$  has the highest degree of anisotropy, while  $Mg_2Si$  has the lowest degree of anisotropy.

**2.4. Electronic Properties.** To understand the action mechanism, the total density of states (DOS) and the partial density of states (PDOS) should be studied. Figure 8(a) shows the density of states of  $Mg_7Si_4Y$ , between  $-3$  eV and the Fermi level, where there exists a very strong orbital hybridization for Mg (2p) and Y (4d) indicating very strong bonding effects. Figure 8(b) shows the density of states of  $Mg_8Si_4Sb$ , where there is strong orbital hybridization between the atoms of Mg, Si, and Sb. Figure 8(c) shows the density of states of  $Mg_6Si_4YSb$ . The mainly orbital hybridization appears in  $-6$  to  $4$  eV. The atoms of Mg and Y have strong bonding effects, while the bonding effects of the other atoms are weak. Figure 8(d) shows the

density of states of  $\text{Mg}_7\text{Si}_4\text{YSb}$ , where all the four atoms show orbital hybridization. In a word, Y doping causes strong orbital hybridization between Mg (2p) and Y (4d), while Sb doping causes strong orbital hybridization between Mg (2p), Si (3p), and Sb (5p). The Fermi surface shifts towards the high-energy region after Y and Sb doping, resulting in an increase in the density of the electron energy states corresponding to the Fermi level. The values are 2 eV ( $\text{Mg}_2\text{Si}$ ), 3.05 eV ( $\text{Mg}_7\text{Si}_4\text{Y}$ ), 5.4 eV ( $\text{Mg}_8\text{Si}_4\text{Sb}$ ), 3.7 eV ( $\text{Mg}_6\text{Si}_4\text{YSb}$ ), and 2.9 eV ( $\text{Mg}_7\text{Si}_4\text{YSb}$ ) in turn, indicating that doping can improve the electrical conductivity of  $\text{Mg}_2\text{Si}$ . This is also consistent with the results which were obtained in Reference [27]. The electrical conductivity of  $\text{Mg}_8\text{Si}_4\text{Sb}$  is the best.

### 3. Conclusions

The structural, stability, thermodynamic, and mechanical properties of Y and Sb doped into  $\text{Mg}_2\text{Si}$  are calculated by the GGA-PBE method. The results revealed that the stable structures that can be formed are (a)  $\text{Mg}_7\text{Si}_4\text{Y}$ , (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$ , (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$ , and (i)  $\text{Mg}_7\text{Si}_4\text{YSb}$ . (g)  $\text{Mg}_6\text{Si}_4\text{YSb}$  is the most stable, while (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$  is the least stable. Young's modulus of  $\text{Mg}_2\text{Si}$  will be reduced by Y and Sb doping, the ductility of  $\text{Mg}_2\text{Si}$  will be improved, and the brittleness of  $\text{Mg}_2\text{Si}$  will be well solved. Among them, the effect of single-doped Sb is better. The Debye temperature ( $\Theta_D$ ) of  $\text{Mg}_2\text{Si}$  will be lowered, and then the thermal conductivity and hardness of  $\text{Mg}_2\text{Si}$  will be reduced by Y and Sb doping. The Debye temperature ( $\Theta_D$ ) of (f)  $\text{Mg}_8\text{Si}_4\text{Sb}$  in the five structures is the lowest. Doping with Y and Sb can improve the conductivity of  $\text{Mg}_2\text{Si}$ , and  $\text{Mg}_8\text{Si}_4\text{Sb}$  has the best conductivity.

### Data Availability

The computational data used to support the findings of this study are included within the article.

### Conflicts of Interest

The authors declare that there is no conflict of interest regarding the publication of this paper.

### Acknowledgments

The authors would like to acknowledge the National Natural Science Foundation of China. This work was also supported by the Key Fund Project (Grant No. 51634004), the Doctoral Scientific Research Foundation of Liaoning Province (Grant No. 20180551213), the Key Laboratory of Chemical Metallurgy Engineering of Liaoning Province, University of Science and Technology Liaoning (Grant No. USTLKFYSY201711), and the Fund Project of University of Science and Technology Liaoning (Grant No. 2017YY02).

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