

Research Article Numerical Study of Pollutant Emissions in a Jet Stirred Reactor under Elevated Pressure Lean Premixed Conditions

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Numerical study of pollutant emissions (NO and CO) in a Jet Stirred Reactor (JSR) combustor for methane oxidation under Elevated Pressure Lean Premixed (EPLP) conditions is presented. A Detailed Flow-field Simplified Chemistry (DFSC) method, a low computational cost method, is employed for predicting NO and CO concentrations. Reynolds Averaged Navier Stokes (RANS) equations with species transport equations are solved. Improved-coefficient five-step global mechanisms derived from a new evolutionary-based approach were taken as combustion kinetics. For modeling turbulent flow field, Reynolds Stress Model (RSM), and for turbulence chemistry interactions, finite rate-Eddy dissipation model are employed. Effects of pressure (3, 6.5 bars) and inlet temperature (408–573 K) over a range of residence time (1.49–3.97 ms) are numerically examined. A good agreement between the numerical and experimental distribution of NO and CO was found. The effect of decreasing the operating pressure on NO generation is much more than the effect of increase in the inlet temperature.

1. Introduction

In recent decades, natural-gas-fired turbine industries have been proceeded to lean premixed technology due to stringent environment regulations especially for NO_x suppression, and Elevated Pressure Lean Premixed (hereinafter referred to as EPLP) has been recognized as the practical operating condition. Numerical investigation of pollutant emissions in a combustor under such conditions relies on employing both the suitable method of pollutant prediction and chemical kinetics. However, due to high computational cost for a realscale combustor, the laboratory-scale combustors, that is, Jet Stirred Reactor (JSR), may be emphasized. Issues mentioned above are briefly reviewed in the following paragraphs.

Generally, four different numerical schemes can be found in the literature for predicting of NO and CO emissions, Detailed Flow-field Detailed Chemistry (DFDC), Detailed Flow-field Simplified Chemistry (DFSC), Simplified Flowfield Detailed Chemistry (SFDC), and Simplified Flow-field Simplified Chemistry (SFSC). In the first, 2D/3D numerical solution must be performed using a detailed mechanism, and despite very high accuracy of this method, the computational cost is huge; therefore, it is barely used for industrial applications [1]. In the 2nd, a 2D/3D numerical solution using a reduced (or global) mechanism may be applied. This scheme is used for predicting of NO and CO emissions for some combustors under lean premixed conditions, that is, Hamer and Roby [2], Nicol et al. [3], and Novosselov and Malte [4]. In the 3rd, a detailed mechanism is employed in a Chemical Reactor Network (CRN) created based on either analyzed numerical results or empirical data, for example, Glarborg et al. [5], Miller and Bowman [6], Drake and Blint [7], Michaud et al. [8], and Nicol et al. [9]. In the last method, instead of a detailed mechanism used in the third method, a simplified mechanism is replaced. This scheme is used by Novosselov and Malte [4].

Mostly, two different chemical kinetic mechanisms, including detailed and simplified, are available for methane oxidation and NO formation. Limited numbers of detailed mechanisms are available, for instance, GMK [5], MB [6], DB [7], GRI 2.11, GRI 3.0, Hughes et al. [10], Petersen et al. [11], and Pillier et al. [12]. However, there are a large number of studies on simplified mechanisms, for example, Goussis and Kelly, 1990 [13], Lam and Goussis, 1994 [14], Mallampalli et al.,

1998 [15], Massias et al. [1], Sung et al., 2001 [16], Belcadi et al., 2012 [17], and Karalus et al. [18]. Utilizing such mechanisms in computational fluid dynamics (CFD) problems needs a huge computational cost due to high number of species. Furthermore, despite introducing a few numbers of global mechanisms with less number of species, for example, Nicol et al. [3] and Novosselov [19], the rate coefficients of these mechanisms are case dependent and of limited use for variety of operating conditions especially for EPLP situations.

There exist a lot of studies about lean premixed JSR combustors. First time, Thornton et al. [20] experimentally studied this combustor to investigate the kinetic oxidation of the hydrocarbon fuels. Corr et al. [21] investigated the formation of NO and CO in JSR with the volume of 15.8 cc under atmospheric pressure lean premixed conditions ($\phi =$ 0.6) using experiment and a PSR solver. Steele et al. [22] did a similar work but over a range of equivalence ratio (0.41–0.67) and residence time (1.7-7.4 ms). Furthermore, Steele et al. [23] examined effects of inlet temperature (300-600 K), pressure (1–7.1 atm), volume (2, 16 cc), and the ratio of area to volume using a solver consisting of a PSR and a plug flow reactor (PFR). Bengtsson et al. [24] used alternative conditions in the experiment, that is, pressure up to 20 bars, equivalence ratio of 0.55, a range of temperature (1783-1823 K), and three different residence times (1.0, 1.5, and 2.0 ms). Shuman [25] empirically inspected the formation of NO and CO over a wider range for residence time (0.5-4.0 ms), temperature (1815-1910 K), and different range for pressure (3-6.5 atm.) and inlet temperature (344-573 K).

The main objective of this study is to numerically investigate effects of pressure and inlet temperature and a range of residence time on NO and CO emissions in a laboratory-scale JSR combustor under EPLP operating conditions. Nine operating conditions from the experiment of Shuman [25] and general form of the five-step global mechanism suggested by Nicol et al. [3] are considered as the base operating conditions and base mechanism, respectively. However, in this mechanism the rate coefficients include analytical relationships between the reaction rate and the net rate of species. They have used regression analysis based on the mechanism of MB, but he did not present his model for high pressure condition. In addition, the effect of some parameters such as initial temperature of the mixture on rate coefficients was not considered. Here, the optimization is improved by using the DE algorithm. In this way we do not need any analytical relationship, and the optimal rate coefficients corresponding to the desired operating conditions are determined. So, the new evolutionary-based approach is used to obtain the reaction rate coefficients of this mechanism under nine EPLP operating conditions. A DFSC scheme using CFD software (FLU-ENT) is employed to numerical simulation.

2. Derivation of Chemical Kinetic Coefficients

A new evolutionary-based approach is implemented to obtain the reaction rate coefficients of the methane-air combustion kinetics, and the details are elaborately explained in the following subsections. The method consists of two modules, namely, the simple Chemical Reactor Modeling (CRM) and the numerical optimizer. For any given operating condition and a user defined detailed mechanism (as the target mechanism), the CRM gives the corresponding values of species concentrations, that is, NO and CO. These are reserved as the target values for optimizer module. With the aim of predicting NO and CO, a global mechanism is specified. The unknown rate coefficients of this global mechanism are considered as the design variables used in the differential evolution (DE) module. Employing an interactive process, the CRM calculates the species concentrations through the coefficients which are obtained by the DE. The results are compared with the detailed mechanism and this process is continued till the discrepancy between the predicted and the target values becomes as small as possible.

2.1. The Chemical Reactor Modeling (CRM). According to the previous paragraph, species concentrations are obtained from the CRM module. Here, a Perfectly Stirred Reactor (PSR) combined with a plug flow reactor (PFR) is addressed as the CRM. Possible detailed or predefined global mechanisms along with a set of parameters, that is, operating pressure, initial mixture temperature, residence time, and equivalence ratio, are the inputs. Furthermore, the length and diameter of the combustor are also added. The CRM calculations have been carried out using the method described by Turns [26]. It is noted that CHEMKIN [27] software is used for the calculation of CRM. The PSR-PFR output is distribution of concentrations along the reactor.

2.2. Optimizer Module. In this study, the differential evolution (DE) optimization algorithm [28] is employed to find the rate coefficients for a predefined global mechanism through the procedure addressed in Section 2. Three key elements should be provided for the optimizer module, (i) the design variables, (ii) the objective function, and (iii) the constraints. The design variables are the unknown rate coefficients of the global mechanism. The cost function is intended to evaluate the deviation of some species concentrations (i.e., NO and CO) predicted using the global mechanism from those calculated with the detailed mechanism. Consequently, the cost function for the PSR-PFR is specified as

$$I_{\rm PFR} = \frac{1}{X_{\rm NO}^{\rm det,max}} \int_{0}^{L} \left| X_{\rm NO}^{\rm det}(x) - X_{\rm NO}^{\rm glb}(x) \right| dx + \frac{1}{X_{\rm CO}^{\rm det,max}} \int_{0}^{L} \left| X_{\rm CO}^{\rm det}(x) - X_{\rm CO}^{\rm glb}(x) \right| dx,$$
(1)

where x, X, L are distance along the PFR, mole fraction, and length of the reactor, respectively. Also, det and glb denote detailed and global mechanism, respectively. The optimization constraints are imposed by considering a finite interval for each design variable. The intervals are assigned such that the best values lie between the lower and the upper bounds. The objective function is normalized based on the maximum mole fraction of NO and CO. It is obvious that one may add other target mole fractions to the above, but then the model accuracy for predicting these two species will decrease.

Case number	τ (ms)	φ (—)	T_{t0} (K)	P (atm)	Fuel flow (gr/sec)	PH/NPH*
1	1.49	0.58	573	6.5	1.219	PH
2	2.09	0.61	573	6.5	0.871	PH
3	3.97	0.66	573	6.5	0.460	PH
4	1.65	0.64	573	3	0.523	PH
5	2.36	0.67	573	3	0.366	PH
6	3.33	0.74	573	3	0.259	PH
7	1.63	0.69	408	3	0.526	NPH
8	2.40	0.74	418	3	0.360	NPH
9	3.33	0.80	432	3	0.260	NPH

TABLE 1: Base operating conditions [25].

*PH: preheated conditions, NPH: no preheated conditions.

TABLE 2: General form of the five-step global mechanisms for CH₄ air combustion [3].

Number	Reaction description	Reaction rate [mole/cm ³ /s]
1	$\rm CH_4 + 1.5O_2 \rightarrow \rm CO + 2H_2O$	$R_1 = A_1 [CH_4]^{B_1} [O_2]^{C_1} \exp(-D_1/R_u/T)$
2	$\rm CO + 0.5O_2 \rightarrow \rm CO_2$	$R_{2} = A_{2} [\text{CO}]_{2}^{B} [\text{O}_{2}]_{2}^{C} \exp(-D_{2}/R_{\mu}/T)$
3	$\rm CO_2 \rightarrow \rm CO + 0.5O_2$	$R_3 = A_3 [CO_2]^{B_3} \exp(-D_3/R_u/T)$
4	$\rm N_2 + O_2 + CO \rightarrow 2NO + CO$	$R_4 = A_4 [O_2]^{B_4} [CO]^{C_4} \exp(-D_4/R_u/T)$
5	$N_2 + O_2 \rightarrow 2NO$	$R_5 = A_5 T^{-0.5} [N_2] [O_2] \exp(-D_5 / R_u / T)$

2.3. Base Operating Conditions and Global Mechanism. The above procedure has been applied to generate nine models, based on nine operating conditions. These operating conditions are selected based on the studies of Shuman [25]. In all cases, the combustion pressure is estimated from pressure loss in the premixed tube, nozzle inlet, and combustor Mach number. Similar estimates are used to deduce the residence time based on the flow parameters and combustor volume. All the flow parameters are given in Table 1 and the combustor volume is assumed equal to 1.0 cm³.

The general form of the five-step global mechanism proposed by Nicol et al. [3] is considered as the base mechanism. This mechanism and its unknown rate parameters are presented in Table 2. According to Table 2, the five steps of the mechanism are as follows: oxidation of the methane fuel to CO and H_2O , oxidation of the CO to CO_2 , dissociation of the CO₂ to CO, flame-NO formation, and post-flame-NO formation.

3. Numerical Solution Procedure

JSR combustor together with the relevant geometrical parameters is schematically shown in Figure 1.

This standard geometry is consisted of two truncated cones, one at the first and the other at the end of the combustor, and a cylinder in the middle. Combustor inlet (with diameter of d_i) is located at the center of the lower base, while four equally spaced holes (with individual diameter of d_0), with elevation of h_0 from the base, are positioned on the lateral surface of the first truncated cone. Several researchers used a similar shape (but with different dimensions) for JSR in their experiments, for example, Corr et al. [21], Steele et al. [22], Steele et al. [23], Steele et al. [29], Shuman [25], and



FIGURE 1: JSR combustor geometry.

Rutar and Malte [30]. Some geometrical dimensions of these can be seen in Table 3.

Here, geometry of the JSR of Shuman's work is considered in our numerical study. Since some of the reactors dimensions were not clear in their references, we have used ratio of a power of one-third of their volume to guess unknown dimensions.

3.1. Governing Equations. Here, a brief description of conservation equations for mass, momentum, chemical species, energy, and turbulence is introduced. These equations are

TABLE 3: Dimensions of different JSRs.

d_i	d _o	d_b	d_m	h_1	h_o	h	A
			mm				сс
4.40	4.00	16.0	25.0	25.00	6.00	45.00	15.8
4.40	4.00	16.0	25.0	25.00	6.00	45.00	15.8
0.74	9.50	_	_	_	_	_	49.5
4.40	4.00	16.0	25.0	25.00	6.00	45.00	15.8
1.00	2.40	_	12.7	14.20	14.2	22.20	2.00
1.40	1.27	7.30	11.5	13.46	—	20.19	1.50

applicable for turbulent flow in a nonaccelerating reference frame, and details are available in certain reference [31].

(i) Conservation of Mass. Continuity equation can be introduced as follows:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \left(\rho \vec{\nu}\right) = 0, \qquad (2)$$

where ρ is the density and \vec{v} is the velocity vector.

(ii) Conservation of Momentum. Conservation of momentum is described by

$$\frac{\partial}{\partial t} \left(\rho \vec{v} \right) + \nabla \cdot \left(\rho \vec{v} \vec{v} \right) = -\nabla p + \nabla \cdot \left(\overline{\overline{\tau}} \right) + \rho \vec{g} + \vec{F}, \qquad (3)$$

where p is static pressure, $\overline{\overline{\tau}}$ is the stress tensor, and $\rho \overline{g}$ and \overrightarrow{F} are the gravitational body force and external body force, respectively. The stress tensor is described by

$$\overline{\overline{\tau}} = \mu \left[\left(\nabla \overline{\nu} + \nabla \overline{\nu}^T \right) - \frac{2}{3} \nabla \cdot \overline{\nu} I \right], \tag{4}$$

where μ is the molecular viscosity and *I* is the unit tensor.

(iii) Species Transport Equations. The conservation equations for chemical species can be written as

$$\frac{\partial}{\partial t} \left(\rho Y_i \right) + \nabla \cdot \left(\rho \vec{v} Y_i \right) = -\nabla \cdot \overrightarrow{J_i} + R_i, \tag{5}$$

where Y_i is the mass fraction of each species, R_i is the net rate of production of species *i* by chemical reaction, and $\overrightarrow{J_i}$ is the diffusion flux of species *i* and can be written as

$$\overrightarrow{J}_{i} = -\rho \left(D_{i,m} + \frac{\mu_{t}}{\mathrm{S}c_{t}} \right) \nabla Y_{i}, \tag{6}$$

where Sc_t is the turbulent Schmidt number, μ_t is turbulent viscosity, and D_t is the turbulent diffusivity.

Here, the source terms R_i in (5) are computed by Eddy dissipation model.

(v) *Turbulence Model*. The exact transport equations for the transport of the Reynolds stresses $(\rho \vec{u}_i \vec{u}_j)$ are also solved as the flow is turbulent. These equations can be written as

$$\frac{\partial}{\partial t} \left(\rho \overline{\dot{u}_i \dot{u}_j} \right) + \frac{\partial}{\partial x_k} \left(\rho u_k \overline{\dot{u}_i \dot{u}_j} \right)$$

$$= D_{T,ij} + D_{L,ij} + P_{ij} + \emptyset_{ij} + \epsilon_{ij},$$
(7)

where $D_{T,ij}$ is turbulent diffusion, $D_{L,ij}$ is molecular diffusion, P_{ij} is stress production, \emptyset_{ij} is pressure strain, and ϵ_{ij} is dissipation. For details of modeling these terms, it can be referred to Lien and Leschziner [32].

3.2. Grid and Boundary Conditions. We use axisymmetric assumption to reduce the computational cost. The output holes are replaced with a slot with an area equivalent to the area of all four holes. A structured grid consisting of 40000 cells is used for numerical solution. Mass-flow-inlet and pressure-outlet are considered for the inlet and outlet boundaries, respectively. Mass fractions of the both reactants and products are calculated in terms of equivalence ratio considering one-step global mechanism for methane-air combustion. Hydraulic diameter-turbulence intensity approach is used to calculate both kinetics and dissipation rate of turbulence energy. Inlet and outlet diameters are considered as hydraulic diameter, and turbulence intensities are determined based on $I = 0.16 \text{ Rep}_0^{-0.125}$.

3.3. Method of Numerical Solution. The CFD software (FLU-ENT) is used for numerical simulation. For faster convergence, first a cold flow procedure is used and then the reactive-flow simulation is performed. A pressure-based method is employed to solve the RANS equations together with species transport equations. For modeling turbulent flow field, Reynolds Stress Model (RSM), and for turbulence chemistry interactions, finite rate-Eddy dissipation model are used. To discretize the pressure, the standard discretization method of the software is used. For other parameters (i.e., density, momentum, turbulence kinetic energy, dissipation rates, and species concentrations) the upwind scheme is used for discretization. For better convergence, based on our experience an under relaxation factor of 0.6 is used for the turbulence kinetic energy, dissipation rate of energy, and viscosity, and a factor of 0.8 is used for density, energy, and chemical species equations. It is noted that here heat transfer is not modeled.

4. Validation and Results

Results are separately presented in three subsections. In Section 4.1, validated results of the generated chemical kinetics using the PSR-PFR module and evolutionary-based method simultaneously are examined over different operating pressures, residence times, and inlet temperatures. In Section 4.2, the attention is confined to compare the numerical predicted of NO and CO emissions with the experiments. Also, grid independency of the numerical solution is performed and results are presented for pollutant species (e.g., NO and CO). In Section 4.3, we turn to investigate effects of operating pressure and inlet temperature on NO and CO emissions at different residence times.

4.1. Validated Results of the Obtained Kinetics. Our algorithm is a very fast algorithm which produces a kinetic model for each reactor, at each operating condition (i.e., inlet temperature, pressure, and the total equivalence ratio). As presented

in Table 1, nine different operating conditions (case numbers) are chosen, six to investigate effects of the combustor pressure and three to examine impacts of the inlet temperature on NO and CO concentrations. Mass flow is not a dependent parameter in our analysis but is used in our CFD simulations as part of our boundary conditions. Also as reported in Table 2, the global five-step mechanism of Nicol with unknown reaction rate coefficients is used as the base of our mechanism, and then the optimal values of these unknowns are obtained from the evolutionary-based procedure (explained in Sections 2.1 and 2.2). The calculated coefficients are tabulated for eight case numbers (Table 1) in Table 4. Comparison of the rate coefficients obtained for the temperature and pressure conditions (Table 1) shows that these factors are more a function of pressure and temperature changes have less effect on them.

To compare the computational cost of this 5-step model with a full GRI-3.0 mechanism, we use the PREMIXED model of CHEMKIN software. The computational cost for full mechanism was about 16 times the reduced 5-step mechanism. Since this is a one dimensional model, we expect significant computational cost advantage for real three dimensional computations.

NO and CO concentrations and adiabatic flame temperature for nine cases are comparatively plotted in Figures 2– 4 which show that there is a reasonable agreement between the generated five-step mechanisms and the detailed GRI 3.0 mechanism.

4.2. Comparing the Predicted Emissions with Experiment. Some empirical data of Shuman is used for validation of the numerical study. However, the experiments were performed for three different pressures of premixed tube (3, 4.7, and 6.5 atm.), residence time, and inlet temperature ranged between 0.5–4.08 ms and 323–573 K, respectively, at lean equivalence ratios (0.58–0.80); here validations are presented for two different pressures (3 and 6.5 atm.) and inlet temperatures (418 and 573 K) and three different residence times (2.1, 2.5, and 4 ms).

Comparison between predicted and empirical data for NO and CO versus radial coordinate inside the JSR combustor at fixed axial position of 13.46 mm are illustrated in Figures 5 and 6 for cases 2 and 8 (two different pressures and inlet temperatures).

As is obvious from these figures, there is a reasonable agreement between the numerical and experimental data for different case numbers.

To investigate grid independency of the numerical solution, concentrations of NO and CO for the other case (e.g., case 3) based on two meshes with different cells (40000 and 110000) are illustrated in Figure 7 and the distributions are compared with the experiment.

4.3. Effects of Inlet Temperature and Operating Pressure on NO. It is found that increasing residence time under a specified inlet temperature and operating pressure leads to increasing the NO concentration at the exhaust of the JSR combustor. Furthermore, increasing both the inlet temperature and operating pressure at a specified residence time leads to decreasing

T	Case number	Derived coefficients					
-	Case number	Α	В	С	D		
1		1.228e + 18	1.40034	0.402908	57735.3		
2		4.924e + 21	1.41719	1.727700	39913.7		
3	1	2.775e + 14	1.00304	—	120189		
4		1.281e + 35	4.00016	0.849971	114989		
5		2.568e + 16	—	—	145000		
1		9.155e + 17	1.5887	0.409601	44373.2		
2		4.901e + 21	1.51202	1.721500	35039.7		
3	2	2.201e + 14	1.00000	—	120002		
4		1.318e + 35	4.08662	0.836052	114839		
5		3.719e + 16	—	—	144979		
1		1.166e + 18	1.59108	0.468756	42085.8		
2		4.570e + 21	1.51016	1.745650	34044.6		
3	3	2.304e + 14	1.00277	_	120085		
4		1.059e + 35	4.09869	0.846993	114377		
5		3.970e + 16	_	_	140660		
1		1.255e + 18	1.40001	0.400577	40105.8		
2		3.759e + 21	1.53675	1.610820	34464.8		
3	4	1.995e + 14	1.00554	_	121056		
4		1.043e + 35	4.01789	0.849956	104282		
5		2.542e + 16	—	_	144977		
1		1.256e + 18	1.45728	0.480269	40000.2		
2		3.432e + 21	1.53525	1.643350	33422.8		
3	5	2.124e + 14	1.00633	_	121677		
4		1.068e + 35	4.03624	0.849769	104989		
5		2.588e + 16	—	_	144994		
1		9.511e + 17	1.40852	0.400297	40034.4		
2		3.846e + 21	1.51501	1.609680	38742.8		
3	6	2.489e + 14	1.00011	_	124250		
4		1.235e + 35	4.01041	0.849784	106649		
5		2.513e + 16	_	_	144999		
1		9.219e + 17	1.41493	0.592969	40008.7		
2		4.867e + 21	1.51367	1.725150	30257.7		
3	7	2.031e + 14	1.00414	_	120267		
4		1.315e + 35	4.00065	0.843531	104076		
5		2.512e + 16	_	_	144693		
1		1.198e + 18	1.51732	0.413664	40355.4		
2		4.946e + 21	1.53938	1.620760	35262.2		
3	8	2.818e + 14	1.00000	_	123114		
4		1.190e + 35	4.00200	0.849999	104004		
5		2.555e + 16	_	_	144994		

levels of the exhausted NO. It is quantitatively found that increasing the operating pressure about 116% may decrease the NO level about 66%, while for inlet temperature the values of 36% and 3% are obtained, respectively. Therefore, the impact of operating pressure on NO is about seven times more than the effects of inlet temperature. Concentrations of NO versus residence times at different pressures are illustrated in Figure 8.



FIGURE 2: NO concentration versus distance along the PFR using the PSR-PFR based on the generated five-step mechanism for methane oxidation, comparing with GRI 3.0 for different cases of 1, 3, 7, 8, and 9 (a) and 2, 4, 5, and 6 (b).



FIGURE 3: CO concentration versus distance along the PFR using the PSR-PFR based on the generated five-step mechanism for methane oxidation, comparing with GRI 3.0 for different cases of 1, 3, 7, 8, and 9 (a) and 2, 4, 5, and 6 (b).



FIGURE 4: Adiabatic flame temperature versus distance along the PFR using the PSR-PFR based on the generated five-step mechanism for methane oxidation, comparing with GRI 3.0 for different cases of 1, 3, 7, 8, and 9 (a) and 2, 4, 5, and 6 (b).



FIGURE 5: NO (a) and CO (b) concentrations along the radial position between central line and sidewall of the JSR at fixed axial position (13.46 mm), using the generated five-step mechanism in PSR-PFR obtained from CFD simulation for methane oxidation, comparing with the experimental data for case 2.

5. Conclusion

In this paper, numerical study of pollutant emissions (NO and CO) in a Jet Stirred Reactor (JSR) combustor for methane oxidation under Elevated Pressure Lean Premixed (EPLP) conditions has been carried out. A Detailed Flow-field Simplified Chemistry (DFSC) method, a low computational cost approach, has been employed for predicting NO and CO concentrations. Effects of pressure (3, 6.5 bars) and inlet

temperature (408–573 K) over a range of residence time (1.49–3.97 ms) has been numerically examined. A good agreement between the numerical and experimental distributions for NO and CO was found. It was found that increasing both the operating pressure and inlet temperature tends to decrease the NO levels. It was quantitatively found that increasing the operating pressure about 116% may decrease the NO level about 66%, while for inlet temperature the values of 36% and 3% were obtained, respectively.



FIGURE 6: NO (a) and CO (b) concentrations along the radial position between central line and sidewall of the JSR at fixed axial position (13.46 mm), using the generated five-step mechanism in PSR-PFR obtained from CFD simulation for methane oxidation, comparing with the experimental data for case 8.



FIGURE 7: NO (a) and CO (b) concentrations along the radial position between central line and sidewall of the JSR at fixed axial position (13.46 mm), using the generated five-step mechanism in PSR-PFR obtained from CFD simulations based on two meshes with 40000 and 110000 cells for methane oxidation, comparing with the experimental data for case 3.



FIGURE 8: NO concentrations versus residence times at different EPLP conditions obtained from the CFD simulations based on the generated five-step global mechanisms using the DE evolutionary-based method.

Competing Interests

The authors declare that they have no competing interests.

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