

Research Article Graph-Based Collaborative Filtering with MLP

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The collaborative filtering (CF) methods are widely used in the recommendation systems. They learn users' interests and preferences from their historical data and then recommend the items users may like. However, the existing methods usually measure the correlation between users by calculating the coefficient of correlation, which cannot capture any latent features between users. In this paper, we proposed an algorithm based on graph. First, we transform the users' information into vectors and use SVD method to reduce dimensions and then learn the preferences and interests of all users based on the improved kernel function and map them to the network; finally, we predict the user's rating for the items through the Multilayer Perceptron (MLP). Compared with existing methods, on one hand, our method can discover some latent features between users by mapping users' information to the network. On the other hand, we improve the vectors with the ratings information to the MLP method and predict the ratings for items, so we can achieve better effects for recommendation.

1. Introduction

With the rapid development of the Internet, recommendation systems play an important role in e-business. The collaborative filtering (CF) methods are commonly used in recommendation systems, which can recommend items based on some features. In general, the CF methods can be divided into memory-based CF and model-based CF [1], and the latter can be further divided into the methods based on users or items [2].

The CF methods are based on users, the users' correlations are analyzed through users' behavior, interests, and other features, and then the items liked by other users who are similar to the user are recommended to the user [3]. For a user with some interests and preferences in the past, they may also have similar interests and preferences in the future [4].

The CF methods based on items analyze the correlation between the items and recommend the similar items. The K-Nearest Neighbor method [5] is extensively applied in the CF area. In general, the correlation of items is more stable than those of users, so it often appears in online CF [6]. Online CF is an effective approach to reduce the amount of online calculation [7].

The model-based CF is different from memory-based CF [8]. The model-based methods learn from statistical model [9], using machine learning methods [10] to learn the features and train a model. Then we use the previous trained model to predict the rating of items that have not been rated previously. Finally, we recommend the items whose ratings are higher than others for the user [11]. The common models of CF include Bayesian Networks [12], latent factor models [13], Singular Value Decomposition (SVD) [14], matrix factorization [15], and Probabilistic Latent Semantic Analysis (PLSA) [16]. In these methods, the matrix factorization method is the most widely used, because it can effectively extract some latent features between users and items with the matrix decomposition [17]. With a vector to represent the feature of users or items, through calculating the relationship of vectors and mapping to the graph, the recommendation systems can recommend some related items to the users [18].

Recently, graph methods have been applied to the recommendation systems. Some researchers put forward the application of graph to learn the correlation between users



FIGURE 1: Framework of our algorithm.

or items. With the vectors of user or items mapped to the network, some latent relationship between them can be discovered. For example, Shameem Ahamed Puthiya Parambath et al. put forward a method applied to recommendation systems based on the similarity graph [11]. Li Xin et al. proposed a method based on graph kernel to learn the relationship between the users and items [19]. Yuan Zhang et al. proposed a method based on graph and the label applying to recommendation systems [20]. The successful experiment results of these methods show the CF based on graph that has some advantages compared to the existing methods [1], because they can learn more latent information in the network [13]. However, most of the methods based on the graph are nonlinear, which predict the users' ratings of unknown items by using a single classifier.

We proposed an improved method based on graph for recommendation systems: first, we map the users' information into vectors representation and transform the highdimensional vectors into low-dimensional vectors by the SVD decomposition [21], which can concentrate the vectors of the users' information. We use the improved kernel function to compute the correlation between users [22]. Then the users' vectors are mapped to the network and learn the relationship between users. We filter out other users who are similar to the given user. Next, the interests and preference of other similar users are analyzed, and the interaction between users and items is learned to make predictions through Multilayer Perceptron (MLP) method [23]. Finally, we predict the unknown rating and sort the items and recommend Top-N to the user. Compared with the existing CF methods [1], our method has some advantages and innovation, as follows:

- (1) Our method learns the correlation between users and items based on the graph [16], and more potential relationships can be discovered in the network [24]. Furthermore, compared with the existing methods based on graph, our method firstly uses the SVD method to reduce dimensions for the vectors of users' information. It can not only reduce the amount of calculation to shorten the time but also enrich the vector of users.
- (2) We use the improved kernel method [22] which learns from Skip-gram model [25] to analyze more latent information by decomposition of the substructures.
- (3) Our method uses the MLP method to learn the latent features further. Our method is different from existing methods, which directly map the features of similar users to the classifier. We used the MLP learning method to learn the relationship between users and items to predict the rating of items [23].

The framework of our algorithm is shown in Figure 1.

2. Background and Related Work

The recommendation systems benefit people in their daily lives. However, many of the recommendation algorithms face the problem of sparsity that performs poorly. Wei Zeng proposed a method based on the semilocal diffusion process on the user-object bipartite network which improves the accuracy of the algorithm greatly [26]. In general, Static user-item networks may ignore the long-term impact. We often used heterogeneous models to learn users' behavior patterns and improve performance by balancing optimization models and relational models [27]. Recommendation algorithms search for similar users through clustering methods or computing correlations. Ming-Sheng Shang proposed cooperative clustering coefficients to describe the selection mechanism of users and quantify the clustering behavior based on collaborative selection [28].

2.1. Kernel Function. In many fields, such as social networks [29] and chemicals, we often need to calculate the similarities between the internal components and then find out some potential relationships between them. The graph represents the overall structure. We consider computing the correlation between nodes to explore some latent features. In the network, the node represents the users and the edge indicates whether there is a connection between them.

There is a popular method for calculating the similarity between the object components by use of kernel methods [30]. In general, kernel methods use kernel functions to calculate the correlation between components [31]. The setting of proper kernel function is important for calculating the correlation because different structures adapt to different calculations [32]. In the graph, let the kernel function $K(V_i, V_j)$ compute the correlation between nodes. Let $\emptyset(V_i)$ represent the vector of node V_i and let <,>H represent dot product operation. This method of kernel function can capture the potential relationship between nodes. In the graph, the node is represented by the vector which contains the information of nodes. The kernel function between two nodes V_i and V_j can be given by

$$K\left(V_{i}, V_{i}\right) = \langle \emptyset\left(V_{i}\right), \emptyset\left(V_{i}\right) \rangle H \tag{1}$$

This is the common kernel function for the graph to calculate the relationship between nodes. However, we propose an improved kernel function learnt from the language model [33].

2.2. Skip-Gram Model. Our approach learns from the Skipgram model to compute the probability [34]; then we introduce the background about the Skip-gram model [35]. The Skip-gram model represents the words by calculating the probability that a word and its surrounding words appear simultaneously in a sentence [36]. The objective of the method is not to predict the current word according to the surrounding words but to predict the surrounding words by the current word. Given the words $\{w_i\}_{i=1}^k$ from a sequence, the aim of the Skip-gram model is to maximize the following equation:

$$\sum_{t=1}^{T} \log \Pr\left(w_{t-c}, \dots, w_{t+c} \mid w_t\right)$$
(2)

 $Pr(w_{t-c}, \ldots, w_{t+c} \mid w_t)$ is computed as follows:

$$\prod_{-c \le j \le c, j \ne 0} \Pr\left(w_{t+j} \mid w_t\right) \tag{3}$$

Here, it is assumed that the current and the surrounding words are dependent. Therefore, $Pr(w_{t+j} | w_t)$ is defined:

$$\frac{\exp\left(V_{w_t}^T V_{w_{t+j}}'\right)}{\sum_{w=1}^V \exp\left(V_{w_t}^T V_w'\right)} \tag{4}$$

where V_w represents the input vectors of word w and V'_w represents the output vectors.

Hierarchical softmax is an efficient algorithm used to train the Skip-gram model [34]. It uses the binary Huffman tree for decomposition; the Huffman tree is the partition function of the Skip-gram model. Then it maps the similar words to similar positions in the vector spaces. The Skipgram model considers the substructure in the kernel function as a word in the sentence and uses the word embedding to represent the similarity between substructures.

3. Method

We first define the basic notations that will be used in the paper. Then, we introduce the concept and function of the graph in our method and explain the process of the learning of the correlation based on the improved kernel function between users in the network. With the algorithm of Graph Kernel Method (GKM), we compute the feature vectors of users and items. Finally, we introduce the MLP, which learns the interaction between users and items to predict the rating.

3.1. Notations. Let U represent a set of users; let I represent a set of items and let R represent a set of the rating of users for items: $R = \{R_{ij} \in R \mid i \in U, j \in I\}$. Let G = (V, E) represent a graph, where V is a set of vertices; $E \subseteq (V \times V)$ is a set of edges in the graph; and G is an undirected graph with nodes V and edges E. |V| represents the total number of the nodes. The adjacency matrix A of the graph G is defined as

$$A = \begin{cases} 0 & if (u, v) \in E \\ 1 & otherwise \end{cases}$$
(5)

In the graph, $V_i\{i \mid i \in V\}$ represents the user, and the edge $e_{ij}\{i, j \mid i \in V, j \in V\}$ describes the interaction between V_i and V_I .

In Table 1, we summarize the important notations throughout this paper.

3.2. Improved Kernel Function. Our approach uses the Skipgram model [32] to learn the latent features of substructures and represents the similarity between nodes by the corpus generation [33]. The method learns the features of nodes by a matrix [37] that represents the similarity between substructures, and the matrix is calculated by the vectors of the substructures. Then we learn the representation of the substructures through the Skip-gram model.

(1) Inp	put: Rating Matrix: $R, R \in \mathbf{R}^{m \times n}$ The dimension of feature: K		
(2) Pro	ocedure:		
(3)	Decompose matrix R with SVD method. $R \longrightarrow P \in \mathbf{R}^{m \times k}, Q \in \mathbf{R}^{n \times k}$		
(4)	For all user <i>u</i> do		
(5)	Receive the vector of v_{μ}		
(6)	Compute the similarity between users with Equation (6)		
(7)	end for		
(8)	Through the activation function and compute the adjacency matrix A		
(9)	Establish graph		
(10)	For all user u do		
(11)	Traverse graph and receive the neighbors <i>w</i>		
(12)	Compute the feature vector of p_{μ} with v_{μ} , w		
(13)	end for		
(14) Output: The feature vector of user: p_{μ} The vector of item: q_i			

Algorithm	1:	GKM
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TABLE	1:	Notations.
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N _v	the set of neighbor nodes of node v
f_{v}	the vector of node v
$\emptyset\left(\nu ight)$	the eigenvalue of node v in low dimension
$K(V_i, V_J)$	kernel function
$\Pr(w_t)$	the possibility of w_t
V_w	the input vectors of word <i>w</i>
W_x	the weight matrix
b_x	the bias vector
a_x	the activation function for every layer

Our framework lists a set of U and decomposes them into substructures to compute the similarity between users. Then each substructure of decomposition is regarded as a sentence, and this sentence is generated by vocabulary V. In this vocabulary, vocabulary V is corresponding to the training data observed in the unique set of substructures. However, different from the words in the traditional text corpus, there is no linear cooccurrence relationship between the substructures. Therefore, we need to establish a corpus, and it is meaningful to coexist in this corpus. Next, we will discuss how to generate a meaningful corpus of common occurrence relationships.

In the graph, even a medium-size graph is pretty expensive for exhaustive enumeration. In order to adopt the sampling subgraphs effectively, several sampling heuristic algorithms are proposed such as biased random sampling and random sampling scheme. In practice, the random sampling of graphlets of size k in a graph G involves placing a randomly generated window of size $k \times k$ on the adjacency matrix of G and collecting the observed graphlet in that window. This process is repeated n times, where n is the number of graphs we want to sample. However, because this is a random sampling percept, it does not retain any concept of cooccurrence, which is the desired attribute of our framework. Therefore, we make use of the concept of neighborhood and modify the random sampling percept, so that we can partially preserve the coexistence relationship between them. In other words, whenever we randomly select a user, we also sample its neighbor. Users and their neighbors are interpreted as a common occurrence of our methods. Therefore, users with similar neighbors will receive similar representations. In this paper, we use the neighbor, which can extend the coexistence relationship to the neighborhood of distance ≥ 1 . For verification, we discussed the influence of similar patterns in the language model and in the graph. We proposed the combination objective as follows:

$$\underset{a^* \ b^* \in V}{\operatorname{argmax}} \frac{\cos\left(b^*, b\right)\cos\left(b^*, a^*\right)}{\cos\left(b^*, a\right) + \alpha} \tag{6}$$

where *a* and *b* represent the substructures from the vocabulary *V*; a^* and b^* represent the related substructures which are similar to substructures *a* and *b*. And $\cos(\cdot)$ is the function used to compute the similarity between the vectors of substructures. $\alpha = 0.001$ is a parameter to prevent that the division is zero.

Then we normalize $K(V_i, V_j)$ in the range (0, 1) and take it into an activation function. If the output from the activation function exceeded the threshold value(*S*), then A_{ij} =1; otherwise, A_{ij} =0. The size of the threshold value is determined by the parameter *S*; the setting of *S* is through supervised learning [35]. We proposed the Algorithm 1 of GKM to compute the feature vectors of users and items.

3.3. *MLP*. In general, a vector connection does not consider any interaction about the latent features between the users and items, and the effect is not sufficient for the model of CF. To solve this issue, as for the concatenated vectors, we propose to add hidden layers and use the standard MLP method [23] to learn the latent features between users and items. In this term, we can give the model a lot of flexibility and nonlinearity to learn the interaction between p_u and q_i , instead of using only fixed elements. The MLP model is defined as follows:

$$z_1 = \emptyset_1 \left(p_u, q_i \right) = \begin{bmatrix} p_u \\ q_i \end{bmatrix} \tag{7}$$

$$\emptyset_2(z_1) = a_2\left(W_2^T z_1 + b_2\right) \tag{8}$$



FIGURE 2: The framework of MLP.

$$\delta_L(z_{L-1}) = a_L \left(W_L^T z_{L-1} + b_L \right) \tag{9}$$

$$y_{ui} = \sigma \left(h^T \emptyset_L \left(z_{L-1} \right) \right) \tag{10}$$

where W_x represents the weight matrix; b_x represents the bias vector; and a_x represents the activation function of the perceptron for the *x*th layer. For a_x , the activation functions of layers, the functions can be selected freely such as sigmoid, Rectified Liner Units (ReLU), and hyperbolic tangent (tanh). Here, we analyze these functions.

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(1) The sigmoid function limits each neuron in (0,1), which may limit the performance of the model. It is known that neurons stop learning when their output approaches 0 or 1.

(2) tanh as a better choice has been widely adopted, but it only alleviates the problems of sigmoid in some degree, because it is as a cancelled version of sigmoid $(tanh(x/2) = 2\sigma(x) - 1)$.

(3) Finally, we choose ReLU, which is more reasonable and is proven to be unsaturated. In addition, ReLU encourages sparse activation, which is suitable for sparse data [38], and makes the model less likely to be overfitting. Our empirical results show that the performance of ReLU is better than the result of tanh, and tanh is better than sigmoid.

To design the network structure, a common solution is to follow the pattern. The bottom of the layer is the widest and it has a small number of neurons for each successive layer. The premise is that they can learn more latent feature by using a small amount of hidden units to higher units. We implement the tower structure in an empirical way, halving the size of layers per layer.

The framework of MLP method is shown in Figure 2.

4. Experiments

In this section, the extensive experiments are conducted in detail to evaluate the effectiveness of our algorithm on the different data sets.

4.1. Data Sets. To demonstrate the performance of our algorithm, the experiments are conducted on four public data sets, MovieLens100K(ML 100K), MovieLens1M(ML 1M), MovieLens10M(ML 10M), and MovieLens20M(ML 20M). The four data sets are collected from the MovieLens website (https://grouplens.org/datasets/movielens).

4.2. Evaluation Metrics. To evaluate the performance of our algorithm, we use two evaluation metrics: recall and F1. In detail, we regard the top *P* as the recommended items for each user and sort them by the ratings. Then evaluation metrics are defined as follows:

$$precision = \frac{P}{N}$$

$$recall = \frac{P}{T}$$
(11)
$$F1 = \frac{2 \times precision \times recall}{precision + recall}$$



FIGURE 3: F1 of four data sets.

where P represents the number of items that the user likes in the top P; T represents total number of items which is related to the user; N represents the total number of items on the recommendation list.

4.3. Baseline Approaches. We list the models that are compared to our algorithm as follows:

Graph+MLP: we use the structure of graph and MLP method to compute the similarity and predict the rating.

LDA: the method treats the item as a word and regards the user as a document to compute the probability for recommendation [37].

CMF: Collective Matrix Factorization is a model to incorporate different sources of information by simultaneously factorizing multiple matrices [35].

KNN+GBDT: it uses KNN to find the similar users and gets the information about them. Then it uses the GBDT model to predict the ratings for items [5].

KNN+Bayes: similar to the model we described above, it searches the similar users and predicts the ratings by Bayes model [12].

SVD: SVD is a model of CF based on features. The useritem matrix is decomposed into two matrices, U and I, and then they are used to predict ratings directly [21].

UCF: users-based CF uses KNN to calculate the users' correlation and recommends the items that similar users may like to the user.

ICF: items-based CF uses KNN to calculate the items' correlation and recommends the similar items to the user.

4.4. Results and Analysis. To empirically evaluate our algorithm, we compare our algorithm with all baselines we listed above on the real-world data sets. First, we split the data sets into train set and test set, with a ratio of 7:3. The effects of the experiment are as follows.

Figure 3 shows F1 to measure the performance of all algorithms in four data sets. We can see that our proposed



FIGURE 4: The recall of four data sets.

Graph+MLP algorithm performs better in the ML 100K data set than other baseline methods in different number of recommend items. It is obvious that only use of KNN method for collaborative filtering is weaker than other algorithms whether based on users or items. Those algorithms that use KNN as preprocessing and classification to predict ratings can make a great effect. We can see that the effects of the KNN+GBDT and KNN+Bayes are better than UCF and ICF. For the KNN+GBDT and KNN+Bayes algorithms, with the same data preprocessing, the algorithm using Bayes classifier is better than the GBDT classifier, because the data set is too sparse with noise, which is not suitable for GBDT classifier. On the contrary, Bayes classifier is more suitable to predict ratings for the data set. Our algorithm used the graph method as preprocessing and then used the MLP method to predict ratings for the items. Our algorithm can perform better than the algorithms that use KNN as a preprocessing and input the prepared data to the classifier. We can see the performance effect in different data sets in Figure 3. In the data set of ML

100K, the effect of UCF is likely to ICF. However, there are larger data volumes in ML 1M, ML 10M and ML 20M. The effect of ICF in ML 20M is better than UCF, because the data set has small data volume; the ratio of the number of users to the number of items will be smaller. However, ICF algorithm is the opposite and it performs well when the ratio of the number of users is more than the number of items.

On the ML 10M and ML 20M data sets, comparing our algorithm with the Bayes algorithm, when the value of p is 5, our algorithm does not perform better. With the value of p becoming larger, our algorithm performs better. On the four data sets, the performance of the CMF algorithm is the worst.

Figure 4 shows the recall to measure the performance of all algorithms on four data sets. We can see that our algorithm performs best regardless of different data sets with the value of p. Combined with the results shown in Figure 3, we can conclude that our algorithm performs best in both accuracy and recall. According to the results of Figure 3, data is prepared with KNN algorithm and classifier is used



to predict ratings. The effects of KNN + GBDT and KNN + Bayes are better than the KNN. Further, the effect of the KNN + Bayes is better than the KNN + GBDT in most of p values.

Figure 5 shows the relationship between the recall and training ratio. We can see from that that our algorithm performs better than baseline algorithms in most cases. On the ML 100K dataset, our algorithm's performance effect is worse than that of other datasets. The ML 100K dataset is too sparse, which has a large impact on the algorithm. In general, with the increase of data, the performance of all algorithms will improve. In the case of small training samples, our algorithm can perform better than other algorithms. What is more, as the amount of data increases, our algorithms. Our algorithm can adapt to large-scale data sets better than other algorithms.

Table 2 shows the execution time of all algorithms in four data sets. We used ML 1M data set to test with 70%

data in train and 30% data in test. The main equipment in the experiment included E5 processor, GPU (GTX-1060), and 8 GB memory. We calculated the time including data preprocessing and model prediction. We can see from Table 2 that if our algorithm does not use SVD method to reduce the dimensions, it needs more time to complete the whole process. Especially with the increase of data sets, the gap between our algorithm and other algorithms is becoming more obvious. The complexity of our decomposition of subgraph in graph method will increase exponentially with the increase of the amount of data. But the speed of our algorithm with SVD is faster than the Graph+MLP without SVD regardless of our value of K in 10 or 15 on all of the data sets. Among all the classifier algorithms, our algorithm performs the fastest except for KNN + Bayes. We can see that the classifiers have a great effect on the accuracy of these algorithms. The performance of the UCF and ICF algorithm without the classifier is worse than KNN+GBDT

A.1	ML	100K	MI	. 1M	ML	10M	ML	20M
Algorithm	k=10	k=15	k=10	k=15	k=10	k=15	k=10	k=15
Graph+MLP (without SVD)	2.01	3.12	4.97	8.61	10.28	16.34	23.72	33.25
Graph+MLP	1.21	2.01	3.31	5.12	8.12	10.26	15.11	19.51
KNN+GBDT	2.12	3.31	5.11	6.31	9.15	11.58	17.43	21.18
KNN+Bayes	0.91	1.87	2.98	4.67	7.21	10.07	14.87	18.91
CMF	1.12	2.11	3.51	5.33	8.44	10.51	15.67	19.32
LDA	1.23	2.23	3.71	5.87	8.81	10.79	15.98	19.83
SVD	1.02	1.91	3.02	4.71	7.31	10.13	15.03	19.21
UCF	0.87	1.31	2.72	4.32	6.98	10.01	13.97	17.61
ICF	0.92	1.52	2.88	4.41	7.05	10.12	14.01	17.76

TABLE 2: The execution time of all algorithms in different data sets.

and KNN+Bayes. We used the SVD method to reduce the dimensions in data preparing, which can improve the speed of our algorithm.

5. Conclusions and Future Work

In this paper, we proposed a CF model based on graph for recommendation systems. We improve the traditional graph model and use the kernel method to compute the relationship between users. Based on the improved kernel method, the similarity is calculated by the generation of the corpus of the Skip-gram model. By using the kernel method, the relation between users can be calculated and more latent information between users can be mined. On the other hand, the MLP method is adopted on the basis of the graph in our model. The method maps the vectors of users and items to neural network and learns more latent information between users and items by the operation of neurons. Therefore, compared with the baseline methods, our proposed model can achieve higher accuracy and recommendation effects. The items recommended by our model are more suitable for users

Well, in future work, we will further improve our model in several ways. First, we optimize the MLP method to mine more latent information between the users and items. Then, we optimize the time complexity and extend the method to online. Finally, with the rapid development of ecommerce, the time consumption of the recommendation is very important for users. So, we will consider applying it to the online recommendation systems.

Data Availability

The data that support the findings of this study are openly available at https://grouplens.org/datasets/movielens.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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