

## Research Article

# Restoration Methods Selection for Wood Components of Chinese Ancient Architectures Based on TODIM with Single-Valued Neutrosophic Sets

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The selection of restoration methods for ancient architectures is of great significance for the protection of human cultural heritage. This paper proposes a novel restoration methods selection approach for wood components of Chinese ancient architectures, in which a multicriteria group decision-making (MCGDM) method with decision-making information is in the form of single-valued neutrosophic sets (SNNs). Firstly, it establishes an index system by comprehensively considering subjective and objective criteria. In addition, the best-worst method (BWM) and the entropy weight method are combined to produce index weights. Furthermore, the TODIM method is utilized by the single-valued neutrosophic sets to prioritize restoration methods. Finally, a specific case of wood component restoration is conducted to demonstrate the practicability of the proposed model. The robustness and effectiveness of the proposed method is verified by sensitivity analysis and comparison analysis.

## 1. Introduction

There are a large number of ancient architectural heritages with high historical, scientific, and artistic values in China. However, many of them are suffering not only from natural damage such as storms, fires, or insects but also from societal damage by rapid urbanization or inappropriate protective measures. Ancient architectures are nonrenewable, so it is important to choose appropriate restoration measures to reduce damage. The restoration for Chinese ancient architectures is a rather complex task. As the selection of restoration method is usually determined by a group of experts, it is a group decision-making problem affected by several factors such as situation of components, restoration process, restoration outcomes, and situation of commissioned restoration company.

With the development in architectural heritage protection practices, the restoration technologies have achieved rich achievements which have provided more options for the restoration of wood components of Chinese ancient architectures [1]. Although some progress has been made, there are still some issues to be addressed. Firstly, the common principles of restoration for ancient architectures include authenticity, reversibility, and minimal intervention. At present, the restoration technology of ancient buildings continues to advance, but it has not been applied scientifically and reasonably. If the repair method is not adopted properly, it will not only fail to effectively restore the ancient buildings but also cause irreversible secondary damage. Secondly, the evaluation information is usually partially. There is a lack of research on the standardization of selection process of restoration methods. Thirdly, in practice, the

restoration methods selection is often determined based on experts' own knowledge and experience, which might lead to information insufficiency. Relevant research rarely uses quantitative methods to assess the decision-making process of Chinese ancient architectures' restoration.

In summary, the motivation of this paper is to propose a novel model of restoration methods selection for wood components of Chinese ancient architectures, which should improve the scientificity and standardization of decision-making during restoration methods selection and be conducive to the protection of ancient architectures. The rest of the paper is organized as follows. In Section 2, previous studies are reviewed in brief. In Section 3, some basic concepts and definitions about neutrosophic sets are introduced. Subsequently, a restoration methods selection model for wood components of Chinese ancient architectures based on MCGDM is developed in Section 4. In Section 5, a case study is operated concretely, sensitivity analysis and comparative analysis are illustrated to verify the proposed model. Finally, Section 6 summarizes the content of the article and provides some possible directions of future study.

## 2. Literature Review

At present, a lot of restoration technologies for wood components of ancient architectures have been developed. The progress of modern technologies is mainly reflected in the use of new technical methods and new materials. For instance, Zaboklicki and Gebiski [2] generalized that polymer composite inserts (such as epoxy resin, glass, and carbon fiber) enhance the continuity of wooden beams and expand their carrying capacity. Orlando et al. [3] focused on how to repair the ends of wooden beams, which decay easily. The study of Koike [4] reviews the development of wood biomass-sourced epoxy resin systems in Japan over the years. Dourado et al. [5] and Casals et al. [6] studied repaired wood structure adopting epoxy composites. Khelifa and Celzard [7] and Baratta and Corbi [8] recommended applying carbon fibre-reinforced polymer (CFRP) or fibre-reinforced polymer (FRP) to increase the bending capacity of timber structure. In real case, different technologies have different degrees of intervention on ancient architectures, and inappropriate technological advances might lead to negative effects; therefore, the choice of restoration methods must take the nonrenewability of Chinese ancient architectures into account. Therefore, we need to develop a scientific and reasonable measure to choose the restoration method.

Recently, some related indices affecting the restoration of Chinese ancient architectures have been discussed. Existing maintenance theory believes that the best protection and maintenance method would be a combination of active and passive maintenance; however, a lack of skilled operators is an obstacle to protect ancient architectures [9]. Fregonese et al. [10] believed that monitoring the condition of ancient building structures would be helpful in finding suitable restoration schemes. Gao et al. [11] even proposed an ancient timber buildings structural health assessment method based on fuzzy-element theory improved by asymmetric proximity. Lourenço [12] mentioned the importance of

architectural characteristics such as structure and materials for the restoration of ancient architectures and pointed out that the value and authenticity of the building should be taken into consideration. By establishing the economic evaluation index system considering the cost, effect, technical, and other index for the ancient architecture protection scheme, Wang et al. [13] tried to choose a more economical ancient architecture protection scheme. Based on existing studies discussed above, they only focused on objective criteria such as component's conditions and technical methods. There are no studies considering both subjective and objective factors simultaneously, and the situation of restoration company has not been considered in the evaluation; no comprehensive index system has been established for the restoration of ancient architectures.

Neutrosophy has been introduced by Smarandache [14], whose fundamental proposition is that each concept has not only a certain degree of truth but also a degree of falsity and indeterminacy that must be considered independently from each other [15]. The neutrosophic set is similar to human thinking, reflecting the uncertainty caused by incomplete knowledge, incorrect knowledge acquisition, or random guessing [16]. Zhang et al. [17, 18] considered that the neutrosophic set is an effective tool for evaluating vague information. In the process of decision-making on the restoration methods of wood components, due to the uncertainty of actual restoration cases, experts' evaluation information is usually vague, and experts' evaluation information often represents emotional preference, which makes it difficult to be stated in an accurate quantitative form. We would better use neutrosophic numbers to describe the results of assessments [19, 20].

Methods for determining weights usually include subjective weighting methods and objective ones. In order to rank unknown weights, Rezaei [21] proposed the best-worst method (BWM) for multicriteria decision-making problem to calculate subjective weights. Compared with other methods to determine subjective weights (such as AHP), the BWM method has advantages in lesser data comparison and more consistent comparisons. However, the single use of subjective weights cannot guarantee the objectivity of evaluation results, and it will increase the difficulty in decision-makers' analysis and the possibility of errors. Hence, we shall use the entropy weight method. According to the characteristics of entropy, the entropy value shows the randomness and disorder of an index, and then, we can determine the degree of discreteness of the index. Therefore, a combination of BWM method with entropy weight method to compute index weights is necessary, which is not only based on the inherent laws of the index data but also expert experience. Thus, the result of index weights is more reliable [22].

TODIM (an acronym in Portuguese for interactive and multicriteria decision-making model) is based on the prospect theory [23]. Prospect theory [24] is considered to be the most typical behavioral decision theory and has been widely used in multicriteria decision problems [25–27]. TODIM method describes the dominance of each alternative over others fully considered the psychological behavior of decision-makers under risk [28, 29]. In order to depict the

psychological behavior of decision-makers, it is possible to modify parameters to reflect the preferences of decision-makers [30–32]. To prioritize restoration methods, we shall use the TODIM method.

From the discussion above, the purpose of this study is to design a restoration methods selection model based on TODIM with single-valued neutrosophic sets for wood components of Chinese ancient architectures. This model is designed to help experts select the most appropriate restoration method. The contributions of this research are summarized as follows: (1) developing an index system for the restoration of wood components of Chinese ancient architectures; (2) using single-valued neutrosophic weighted average operator to aggregate experts' evaluation results, which make them more comprehensive and reliable; (3) applying the BWM method and entropy weight method to determine the index weights in case of unknown criteria and index weights; (4) introducing the TODIM method to obtain the ranking orders of alternatives; and (5) demonstrating the process of the proposed model by presenting an empirical study of a particular case. Also, to verify the validity and reliability of the model, sensitivity analysis and comparison analysis are conducted.

### 3. Preliminaries

In this section, we introduce some concepts and definitions, which will be useful in developing the wood components restoration methods selection model.

*Definition 1* (neutrosophic set) (see [33]). Let  $X$  be a space of points (objects), with a generic element in  $X$  denoted by  $x$ . Then, a neutrosophic set  $A$  in  $X$  is characterized by three membership functions, including a truth-membership function  $T_A$ , an indeterminacy-membership function  $I_A$ , and

a falsity-membership function  $F_A$  and is defined as  $A = \{ \langle x, T_A(x), I_A(x), F_A(x) \rangle \mid x \in X \}$ , where  $T_A(x)$ ,  $I_A(x)$ , and  $F_A(x)$  are real standard or nonstandard subsets of  $]0^-, 1^+[$ , that is,  $T_A(x): X \rightarrow ]0^-, 1^+[$ ,  $I_A(x): X \rightarrow ]0^-, 1^+[$ , and  $F_A(x): X \rightarrow ]0^-, 1^+[$ . The sum of  $T_A(x)$ ,  $I_A(x)$ , and  $F_A(x)$  is unrestricted and  $0^- \leq T_A(x) + I_A(x) + F_A(x) \leq 3^+$ .

*Definition 2* (single-valued neutrosophic set) (see [34]). Let  $X$  be a space of points (objects), with a generic element in  $X$  denoted by  $x$ . A single-valued neutrosophic set (SVNS)  $A$  in  $X$  is characterized by truth-membership function  $T_A$ , indeterminacy-membership function  $I_A$ , and falsity-membership function  $F_A$  with  $T_A, I_A, F_A \in [0, 1]$  for all  $x$  in  $X$ . The sum of three memberships of a SVNS  $A$ , for all  $x \in X$ ,  $0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3$ .

*Definition 3* (see [35]). Let  $A$  and  $B$  be two single-valued neutrosophic numbers, and then the operations can be defined as follows:

- (1)  $\lambda A = \langle 1 - (1 - T_A)^\lambda, (I_A)^\lambda, (F_A)^\lambda \rangle, \lambda > 0$
- (2)  $A^\lambda = \langle (T_A)^\lambda, 1 - (1 - I_A)^\lambda, 1 - (1 - F_A)^\lambda \rangle, \lambda > 0$
- (3)  $A + B = \langle T_A + T_B - T_A \cdot T_B, I_A \cdot I_B, F_A \cdot F_B \rangle$
- (4)  $A \cdot B = \langle T_A \cdot T_B, I_A + I_B - I_A \cdot I_B, F_A + F_B - F_A \cdot F_B \rangle$
- (5)  $A^C = \langle F_A, 1 - I_A, 1 - T_A \rangle$

*Definition 4* (see [36]). Let  $A = \{ \langle x_1 | \langle T_A(x_1), I_A(x_1), F_A(x_1) \rangle \rangle, \dots, \langle x_n | \langle T_A(x_n), I_A(x_n), F_A(x_n) \rangle \rangle \}$  and  $B = \{ \langle x_1 | \langle T_B(x_1), I_B(x_1), F_B(x_1) \rangle \rangle, \dots, \langle x_n | \langle T_B(x_n), I_B(x_n), F_B(x_n) \rangle \rangle \}$  be two SVNSs for  $x_i \in X (i = 1, 2, \dots, n)$ . Then, the normalized Euclidean distance between  $A$  and  $B$  can be defined as follows:

$$D(A, B) = \sqrt{\frac{1}{3n} \sum_{i=1}^n \{ (T_A(x_i) - T_B(x_i))^2 + (I_A(x_i) - I_B(x_i))^2 + (F_A(x_i) - F_B(x_i))^2 \}}. \tag{1}$$

*Definition 5* (see [36]). According to Majumdar et al.'s study, for single-valued neutrosophic set  $A = \{ \langle x, T_A(x), I_A(x), F_A(x) \rangle \mid x \in X \}$ , an entropy on neutrosophic set  $A$  is computed as follows:

$$E(A) = 1 - \frac{1}{n} \sum_{x_i} (T_A(x_i) + F_A(x_i)) \otimes |I_A(x_i) - I_{Ac}(x_i)|. \tag{2}$$

*Definition 6.* (see [37]). The entropy weight of a neutrosophic set in a study by Tan et al. is shown as follows:

$$W_j = \frac{(1 - E(x_j))}{\sum_j^n (1 - E(x_j))}. \tag{3}$$

*Definition 7.* In the literature of Biswas et al. [38], fuzzification of SVNS  $N(\sim) = \{ \langle x | \langle TN(\sim)(x), IN(\sim)(x), FN(\sim)(x) \rangle \mid x \in X \}$  is defined as follows:

$$\mu_{\tilde{F}}(x) = 1 - \sqrt{\frac{1}{3} \left\{ (1 - T_{\tilde{N}}(x))^2 + I_{\tilde{N}}(x)^2 + F_{\tilde{N}}(x)^2 \right\}}. \tag{4}$$

*Definition 8* (see [39]). The single-valued neutrosophic weighted averaging (SVNWA) aggregation operator proposed by Ye's research can be shown as follows:

$$F_{A_i} = \psi_1 A_1 \otimes \psi_2 A_2 \otimes \dots \otimes \psi_n A_n \\ = \langle \langle 1 - \prod_{i=1}^n (1 - T_{A_i})^{\psi_i}, \prod_{k=1}^n (I_{A_i})^{\psi_i}, \prod_{k=1}^n (F_{A_i})^{\psi_i} \rangle \rangle, \tag{5}$$

where  $\Psi = (\Psi_1, \Psi_2, \dots, \Psi_n)$  is the weight vector of  $A_i (i = 1, 2, \dots, n)$ ,  $\Psi_i \in [0, 1]$ , and  $\sum_{i=1}^n \Psi_i = 1$ .

#### 4. The Proposed Selection Model for Wood Components Restoration Methods

The selection of restoration methods for wood components of Chinese ancient architectures stands for a group decision-making problem seeking to find the best option. In actual cases, many indices could not be evaluated with accurate values in the decision-making process. Thus, the proposed model adopts single-valued neutrosophic sets to describe the characteristics of each index. The general process of the proposed model is shown in Figure 1. Details of the model will be explained in the rest of this section.

*4.1. The Establishment of Index System.* The restoration methods selection for wood components is generally decided by a group of  $k$  experts. Based on analysis proposed in literature and experts' opinion, the evaluation of restoration for wood components of Chinese ancient architectures can be mainly measured by four categories, denoted by four criteria  $A_i (i = 1, 2, \dots, 4)$ : basic situation of components ( $A_1$ ), restoration process ( $A_2$ ), restoration outcomes ( $A_3$ ), and situation of commissioned restoration company ( $A_4$ ). Moreover, under each criterion, there are several subcriteria, which influence the selection of restoration methods. Hence, an index system is established, as shown in Table 1.

*4.2. The Acquisition of Evaluation Matrix.* The aspects to be considered in evaluating wood components restoration of Chinese ancient architectures include practical cases, experts, wood components to be repaired, and diverse evaluation indices. Different experts may make different assessments based on their education background, distinct experiences, different assessment criteria, and different restoration methods suitable for different wood component's conditions. Because of the ambiguity and complexity of information, the evaluation values of indices often cannot be expressed in clear numbers. Decision-makers are more inclined to use fuzzy numbers such as linguistic terms with multiple granularities to evaluate indices. Thus, in this section, the evaluation results obtained from experts can be transformed into single-valued neutrosophic numbers. Hence, we can get the evaluation matrix  $R = (r_{ij})$ . The specific process is as follows:

Step 1. Obtaining linguistic terms with multigranularity.

In practical cases, experts may choose linguistic terms based on their preferences. Therefore, due to semantic differences in linguistic terms, different experts may have different evaluation values. Evaluation values of indices are given in the form of multigranularity linguistic terms [40] by an expert group consisting of different experts. Therefore, a linguistic term set containing ordered linguistic terms needs to be set in advance. Different linguistic term sets show different

characteristics of membership function. For example, linguistic term set  $\{m_0, m_1, m_2, m_3, m_4, m_5, m_6, m_7, m_8\}$  can be donated in linguistic terms as {extremely bad, very bad, bad, medium bad, medium, medium good, good, very good, extremely good}, while linguistic term set  $\{l_0, l_1, l_2, l_3, l_4, l_5, l_6\}$  can be donated in linguistic terms as {very bad, bad, medium bad, medium, medium good, good, very good}, but different experts may have different understanding of these terms [41]. Hence, it would be better that experts provide evaluation values for different restoration methods according to a preset linguistic term set.

Step 2. Transforming the evaluation information from experts' questionnaire according to the symmetric linguistic evaluation scale into single-valued neutrosophic numbers with truth, indeterminacy, and falsity.

The linguistic term set in this study is {extremely high, very high, high, medium high, medium, medium low, low, very low, extremely low}, including nine granular linguistic terms. The linguistic terms along with SVNNS are defined in Table 2 as given in the literature [38] to rate each alternative with respect to each index.

Step 3. Determining the weights of experts.

In accordance with the different backgrounds and experiences of different experts, the importance of decision-making experts differs. In this paper, experts' decision power can be expressed in the linguistic terms set {very important, important, medium, unimportant, very unimportant}, and the corresponding single-valued neutrosophic numbers are shown in Table 3. The weight of expert is donated as  $e_k (k = 1, 2, \dots, n)$ ; according to equation (4), the weights of experts can be computed by the following equation [38]:

$$e_k = \frac{u_k}{\sum_{k=1}^l u_k} = \frac{1 - \sqrt{\{(1 - T^k)^2 + (I^k)^2 + (F^k)^2\}/3}}{\sum_{k=1}^l \left(1 - \sqrt{\{(1 - T^k)^2 + (I^k)^2 + (F^k)^2\}/3}\right)}. \quad (6)$$

Step 4. Aggregating the neutrosophic numbers into  $R = (r_{ij})$ .

We use the single-valued neutrosophic weighted averaging (SVNWA) aggregation operator described by equation (5) introduced in Section 2 to aggregate the neutrosophic numbers. Then, we shall get the evaluation matrix  $R = (r_{ij})$ .

*4.3. The Assignment of Index Weights.* In this section, we employ a combination of subjective and objective weights to determine the index weights. To begin with, we utilize an efficient method called BWM to calculate subjective weights of four criteria. Then, we adopt the principle of objectivity to calculate the entropy weight of each index. Based on the subjective-objective method to determine the synthetic weight of each index, the detailed procedures are as follows.

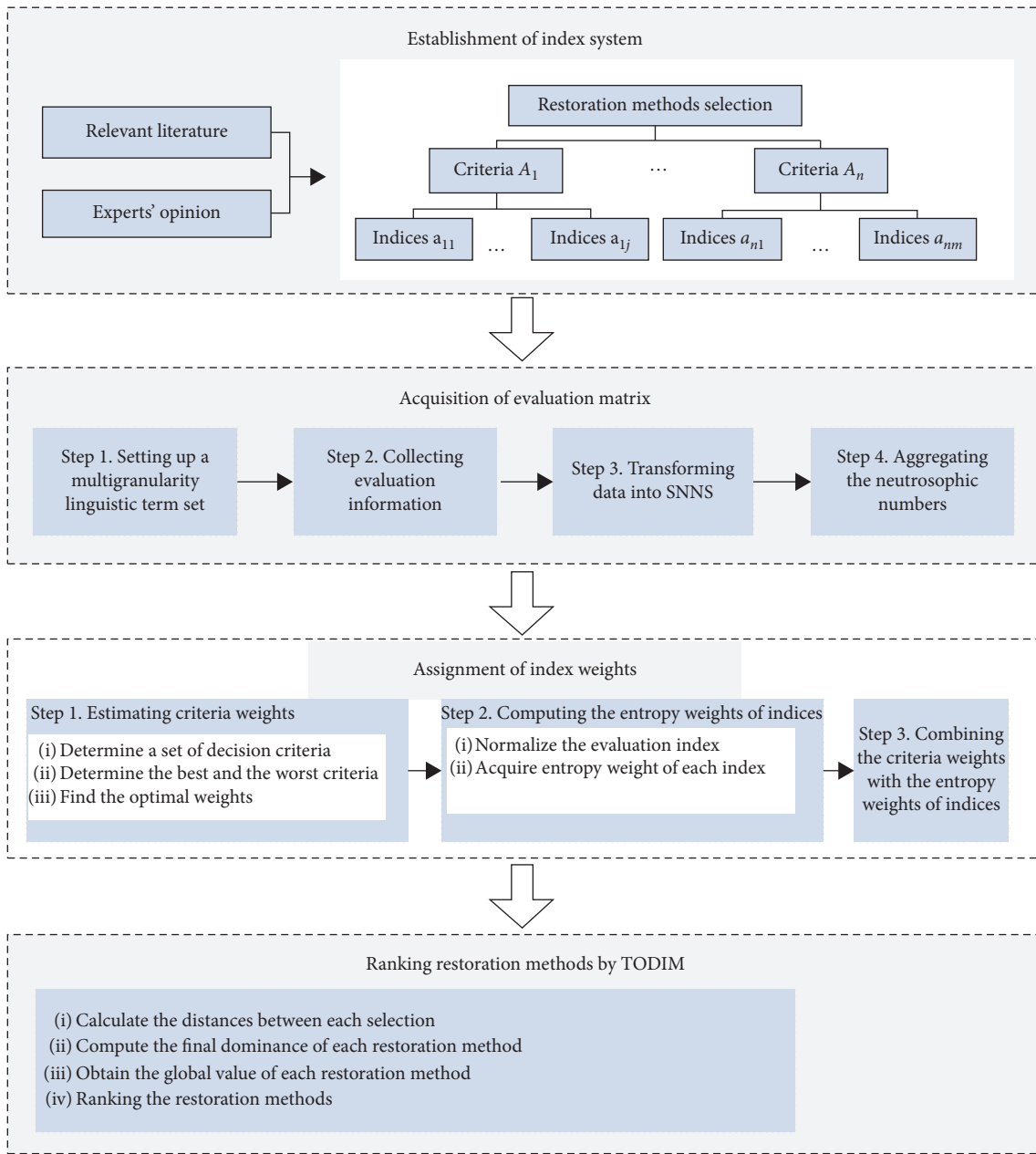


FIGURE 1: Summary of the process of the proposed model.

4.3.1. *Estimating Criteria Weights.* BWM method, introduced by Raize, is the newest method to solve multicriteria decision-making problems [42]. In this section, we apply it to calculate the weights of four criteria [43]:

Step 1. Determining a set of decision criteria. We should consider the criteria  $\{A_1, A_2, \dots, A_n\}$  that should be used to make a decision.

Step 2. The best (e.g., most desirable and most important) and the worst (e.g., least desirable and least important) criteria are determined by decision-maker in general.

Step 3. In the light of the BWM questionnaire, the preference of the best criterion over all the other criteria

using a number between 1 and 9 should be determined. The resulting best-to-others vector would be  $A_B = (a_{B1}, a_{B2}, \dots, a_{Bn})$ , where  $a_{Bj}$  indicates the preference of the best criterion  $B$  over criterion  $j$ . It is clear that  $a_{BB} = 1$ .

Step 4. According to the BWM questionnaire, the preference of all the criteria over the worst criterion, using a number between 1 and 9, should be determined. The resulting others-to-worst vector would be  $A_W = (a_{1W}, a_{2W}, \dots, a_{nW})$ , where  $a_{jW}$  indicates the preference of the criterion  $j$  over the worst criterion  $W$ . It is clear that  $a_{WW} = 1$ .

Step 5. Finding the optimal weights  $\{w_1^*, w_2^*, \dots, w_n^*\}$  by solving (7). The optimal weight for the criterion is the one where for each pair of  $w_B/w_j$  and  $w_j/w_W$ , we



TABLE 1: Index system of restoration methods selection for wood components of Chinese ancient architectures.

Criteria	Index	Definition	Index type
Basic situation of components ( $A_1$ )	Used years ( $a_{11}$ )	The degree that the used years of the component is suitable for these restoration methods	Benefit
	Material properties ( $a_{12}$ )	The degree that the material properties of the component is suitable for these restoration methods	Benefit
	Structural rationality ( $a_{13}$ )	The degree of rationality that the structure of the component is suitable for these restoration methods	Benefit
	Cause of damage ( $a_{14}$ )	The cause of damage of the component is suitable for these restoration methods	Benefit
	Severity of damage ( $a_{15}$ )	The degree of severity that the damage of the component is suitable for these restoration methods	Benefit
	Impact on neighboring components ( $a_{16}$ )	The degree of impact on neighboring components using these restoration methods	Cost
Restoration process ( $A_2$ )	Restoration expense ( $a_{21}$ )	The cost spent for the restoration	Cost
	Material acquisition ( $a_{22}$ )	The degree of difficulty in obtaining materials for the restoration	Cost
	Process complexity ( $a_{23}$ )	The degree of process complexity in the restoration	Cost
	Requirements for equipment ( $a_{24}$ )	The level of requirements for equipment in the restoration	Cost
Restoration outcomes ( $A_3$ )	Probability of authenticity restoration ( $a_{31}$ )	The probability of fixing the components without changing the original materials and processing methods of the component	Benefit
	Degree of preservation of historical information ( $a_{32}$ )	The probability that historical information shall not be destroyed during restoration	Benefit
	Probability of irreversible effects on the original component ( $a_{33}$ )	The probability that the original component could not be returned to the prerepair state after restoration if an error occurred during the repair process	Cost
	Possibility of reversible effects on the original component ( $a_{34}$ )	The possibility that the original component could be returned to the prerepair state after restoration if an error occurred during the repair process	Benefit
	Service life after restoration ( $a_{35}$ )	The length of time that the component may be used after restoration	Benefit
	Difficulty of maintenance ( $a_{36}$ )	The difficulty in maintenance of the component after restoration	Cost
Situation of commissioned restoration company ( $A_4$ )	Teamwork capacity ( $a_{41}$ )	The cooperation efficiency of the restoration team	Benefit
	Proficiency ( $a_{42}$ )	Restoration team professionals' degree of skills	Benefit
	Advanced restoration equipment ( $a_{43}$ )	The performance of the restoration equipment	Benefit

TABLE 2: Linguistic terms for rating the alternatives with SVNNS.

Linguistic terms	SVNNS
Extremely good/high	<1.00, 0.00, 0.00>
Very good/high	<0.90, 0.10, 0.05>
Good/high	<0.80, 0.20, 0.15>
Medium good/high	<0.65, 0.35, 0.30>
Medium/fair	<0.50, 0.50, 0.45>
Medium bad/medium low	<0.35, 0.65, 0.60>
Bad/low	<0.20, 0.75, 0.80>
Very bad/low	<0.10, 0.85, 0.90>
Extremely bad/low	<0.05, 0.90, 0.95>

TABLE 3: Linguistic terms for rating the importance of experts with SVNNS.

Linguistic terms	SVNNS
Very important (VI)	<0.90, 0.10, 0.05>
Important (I)	<0.80, 0.20, 0.15>
Medium (M)	<0.50, 0.40, 0.45>
Unimportant (UI)	<0.35, 0.60, 0.70>
Very unimportant (VUI)	<0.10, 0.80, 0.90>

have  $w_B/w_j = a_{Bj}$  and  $w_j/w_W = a_{jw}$ . In order to meet these conditions for all  $j$ , we should find a solving method where the maximum absolute differences  $|(w_B/w_j) - a_{Bj}|$  and  $|(w_j/w_w) - a_{jw}|$  for all  $j$  are minimized. Considering the nonnegativity and condition for the weights, the following problem results:

$$\min \max_j \left\{ \left| \frac{w_B}{w_j} - a_{Bj} \right|, \left| \frac{w_j}{w_w} - a_{jw} \right| \right\}$$

s.t.

$$\sum_j w_j = 1$$

$$w_j \geq 0, \quad \text{for all } j.$$

(7)

Equation (7) is equivalent to the following equation:

$$\begin{aligned}
 & \min \quad \xi \\
 & \text{s.t.} \\
 & \left| \frac{w_B}{w_j} - a_{Bj} \right| \leq \xi, \quad \text{for all } j \\
 & \left| \frac{w_j}{w_w} - a_{jw} \right| \leq \xi, \quad \text{for all } j \\
 & \sum_j w_j = 1 \\
 & w_j \geq 0, \quad \text{for all } j.
 \end{aligned} \tag{8}$$

Solving equation (8), the optimal weights  $(w_1^*, w_2^*, \dots, w_n^*)$  and  $\xi^*$  can be obtained.

Then, the consistency ratio using  $\xi^*$  and the corresponding consistency index can be calculated using the following formula:

$$\text{consistency ratio} = \frac{\xi^*}{\text{consistency index}}. \tag{9}$$

The maximum values of  $\xi$  (consistency index) for different values of  $a_{Bw}$  are shown in Table 4.

Consistency ratio  $\in [0, 1]$ : the value approaching 0 proved more consistency; instead, the value close to 1 shows less consistency. If the consistency ratio is  $\leq 0.1$ , it indicates a very good consistency. If not, we should revise  $a_{Bj}$  and  $a_{jw}$  to make the solution more consistent.

In the case when the number of criteria exceeds three, the BWM introduced above is limited in deriving the unique optimal weight vector. This leads to multiple optimal solutions. The improved method presented in the study of Rezaei [21] is used to acquire optimal weights with  $n$  criteria. If we use  $\{|w_B - a_{Bj}w_j|, |w_j - a_{jw}w_w|\}$  instead of  $\{|(w_B/w_j) - a_{Bj}|, |(w_j/w_w) - a_{jw}|\}$ , the problem can be solved as follows:

$$\begin{aligned}
 & \min \max_j \left\{ |w_B - a_{Bj}w_j|, |w_j - a_{jw}w_w| \right\}, \\
 & \text{s.t.} \quad \sum_j w_j = 1 \\
 & w_j \geq 0, \quad \text{for all } j.
 \end{aligned} \tag{10}$$

Equation (10) can be transferred to a linear programming problem as follows:

$$\begin{aligned}
 & \min \quad \xi^L \\
 & \text{s.t.} \\
 & |w_B - a_{Bj}w_j| \leq \xi^L, \quad \text{for all } j \\
 & |w_j - a_{jw}w_w| \leq \xi^L, \quad \text{for all } j \\
 & \sum_j w_j = 1 \\
 & w_j \geq 0, \quad \text{for all } j.
 \end{aligned} \tag{11}$$

Equation (11) is a linear program problem, which can compute the unique optimal weight  $\{w_1^*, w_2^*, \dots, w_n^*\}$ .

Therefore, we can obtain the weight vector  $\{w_1, w_2, w_3, w_4\}$  of basic situation of components  $A_1$ , restoration process  $A_2$ , restoration outcomes  $A_3$ , and situation of commissioned restoration company  $A_4$ .

4.3.2. *Calculating Index Weights.* In this section, we follow the combination of subjective and objective principles to compute the index weights. Firstly, we use entropy weight method to compute the entropy weight of each index. Then, we obtain synthesized weight of each index by combining criteria weights with entropy weights. The detailed processes are as follows:

Step 1. Normalizing the evaluation index.

The normalization equation [35] for neutrosophic numbers is as in the following equation. Then, we obtain the normalization matrix  $R = (\beta_{ij})$ :

$$r_{ij} = \begin{cases} T_{ij}, I_{ij}, F_{ij}, & \text{if } j \text{ is benefit index,} \\ 1 - T_{ij}, 1 - I_{ij}, 1 - F_{ij}, & \text{if } j \text{ is cost index.} \end{cases} \tag{12}$$

Step 2. Computing the entropy weights of indices.

According to equations (2) and (3) introduced in Section 2, first, we shall compute the entropy value of each index  $E(x_j)$ . Then, we can acquire the entropy weight  $w_j$  of each index based on the evaluation matrix.

Step 3. Calculating combination weights.

It is important to confirm the weights of the evaluation indicators of the restoration methods, which affects the accuracy of the evaluation results. Subjective weight method relies on knowledge and experience of the experts, and the evaluation results are usually arbitrary. The objective weighting method is based on objective actual conditions and can reduce subjective arbitrariness. So, a combination of subjective and objective methods is necessary. The optimal weight vector of criteria is  $w_i^*$  according to the explanation of BWM in Section 4.3.1. Then, we compute a comprehensive index weight  $H_{ij}$  which combines the subjective weights of criteria with the entropy weights of indices according to the following equation [44]:

$$H_{ij} = \frac{w_i^* \times w_j}{\sum_{i=1}^n w_i^* \times w_j}. \tag{13}$$

4.4. *The Process of Decision-Making Based on TODIM.* To solve multicriteria decision-making problems, Gomes and Lima [45] proposed the TODIM method based on prospect theory. Lourenzutti and Krohling [46] introduced the primary principle of the TODIM method. Recently, an unexpected initiative of the TODIM method was pointed out by Lourenzutti et al., which states that both the losses and the gains should be amplified proportionally by the criterion weight, and then applied to prospect function. The suggested modification in the  $\phi_c$  function is as follows:

TABLE 4: Consistency index (CI) table.

$a_{Bw}$	1	2	3	4	5	6	7	8	9
Consistency index (max $\xi$ )	0.00	0.44	1.00	1.63	2.30	3.00	3.73	4.47	5.23

$$\phi_c(X_i, X_j) = \begin{cases} \sqrt{w_c(s_{ic} - s_{jc})}, & \text{if } s_{ic} \geq s_{jc}, \\ -\frac{1}{\theta} \sqrt{w_c(s_{jc} - s_{ic})}, & \text{otherwise.} \end{cases} \quad (14)$$

$$\varepsilon_i = \frac{\sum_j \delta(X_i, X_k) - \min_i \sum_j \delta(X_i, X_k)}{\max_i \sum_j \delta(X_i, X_k) - \min_i \sum_j \delta(X_i, X_k)}. \quad (17)$$

The selection of restoration methods for wood components of Chinese ancient architectures is a multicriteria group decision-making (MCGDM) problem consisting of expert  $e_k (k = 1, 2, \dots, n)$ , denoted by  $\omega = \{e_1, e_2, \dots, e_k\}$ . Suppose that there exist  $n$  restoration methods  $X_i (i = 1, 2, 3, \dots, n)$ , denoted by  $X = \{X_1, X_2, \dots, X_n\}$ . In this part, we use the TODIM method to solve the restoration methods selection problem. The main procedure is generalized as follows:

Step 1. Calculating the distances  $d_{ij}$  between each selection based on equation (1).

Step 2. Computing the final dominance of restoration method  $X_i$  over each restoration method  $X_k$  under each criterion  $A_j$  as follows [23]:

$$\delta(X_i, X_k) = \sum_{j=1}^n \phi_j(X_i, X_k), \quad \forall (i, k) \text{ where}$$

$$\phi_j(X_i, X_k) = \begin{cases} \sqrt{w_j d(b_{ij}, b_{kj})}, & \text{if } b_{ij} > b_{kj}, \\ 0, & \text{if } b_{ij} = b_{kj}, \\ -\frac{1}{\theta} \sqrt{w_j d(b_{ij}, b_{kj})}, & \text{otherwise,} \end{cases} \quad (15)$$

where  $d(b_{ij}, b_{kj})$  is the distance between  $b_{ij}$  and  $b_{kj}$ . The  $w_j$  is the weight of the  $j$  criterion calculated by the BWM method. In this paper, we use comprehensive index weight  $H_{ij}$  instead of  $w_j$ , where  $H_{ij}$  is the index weight calculated by a combination of the criteria weights calculated by BWM and the indices weights obtained by the entropy weight method. So, we shall apply equation (16) to acquire the final dominance of restoration method  $X_i$  over each restoration method  $X_k$  under each index  $a_{ij}$ :

$$\delta(X_i, X_k) = \sum_{j=1}^n \phi_j(X_i, X_k), \quad \forall (i, k) \text{ where}$$

$$\phi_j(X_i, X_k) = \begin{cases} \sqrt{H_{ij} d(b_{ij}, b_{kj})}, & \text{if } b_{ij} > b_{kj}, \\ 0, & \text{if } b_{ij} = b_{kj}, \\ -\frac{1}{\theta} \sqrt{H_{ij} d(b_{ij}, b_{kj})}, & \text{otherwise.} \end{cases} \quad (16)$$

Step 3. The global value of restoration method  $X_i$  is obtained as follows [23]:

Step 4. Ranking the restoration methods  $X_i$  by their value  $\varepsilon_i$ .

According to the value  $\varepsilon_i$ , we could select restoration method  $X_i$ . The higher the value  $\varepsilon_i$ , the better the restoration method  $X_i$ .

## 5. Empirical Study

The proposed model is applied to solve the selection problem of restoration methods for wood components of Chinese ancient architectures. A Chinese ancient architecture called ‘‘Fuhoutang’’ needed to be restored. Fuhoutang is a state-level cultural legacy, which was constructed during the Xianfeng period of Qing Dynasty. The management authority of Fuhoutang commissioned company  $R$  to restore it. One of the components to be restored is a beam at the bottom of the wooden frame in the hall, denoted by  $C_1$ . The original information of  $C_1$  is outlined in Table 5. Four experts, denoted by  $DM_1, DM_2, DM_3$ , and  $DM_4$ , respectively, studied the condition of  $C_1$  and then provided four possible restoration methods, including stabilizing by outer iron hoop, inserting internal steel, filling with epoxy, and replacing the component, which are denoted by  $X_1, X_2, X_3$ , and  $X_4$  (shown in Figure 2). These four restoration methods are evaluated by experts through several evaluation indices to determine the advantages and disadvantages of each method, and the evaluation index system is listed in Table 1.

According to the selection model presented in Section 3, first, we get the evaluation matrix through the conditions of the wood component to be restored, restoration process, the possible outcomes, and restoration company’s conditions. Then, the index weights are calculated by a combination of criteria weights and entropy weights. Finally, the ranking order of the four restoration methods can be acquired by using the TODIM method. Furthermore, the effectiveness and reliability of the proposed model are verified by sensitivity analysis and comparison analysis.

**5.1. Evaluation Matrix.** The evaluation matrix is obtained from experts according to the evaluation index system. In the light of the evaluation method proposed in Section 4.2, experts evaluate the four methods, and the index evaluation value is represented by linguistic terms with multi-granularity. We transform the linguistic terms into single-valued neutrosophic numbers (SVNNs) according to Table 2. Based on experts’ distinct experience, the importance of four experts differs from each other, as shown in Table 6. According to Table 3, the importance of each expert could be



TABLE 5: The information of the condition of the specific component to be repaired.

$C_1$	Component's condition
Used years	About 150 years
Original material	Chinese fir
The cause of damage	Crack, decay
Damage situation	The beam is 35 cm in diameter and 4.2 meters long. The crack is about 80 cm long, about 4 cm wide, and about 5 cm deep, which is caused by material properties. Near the crack, a decay of about 8 cm in width, 20 cm in length, and 3 cm in depth was eroded by bugs

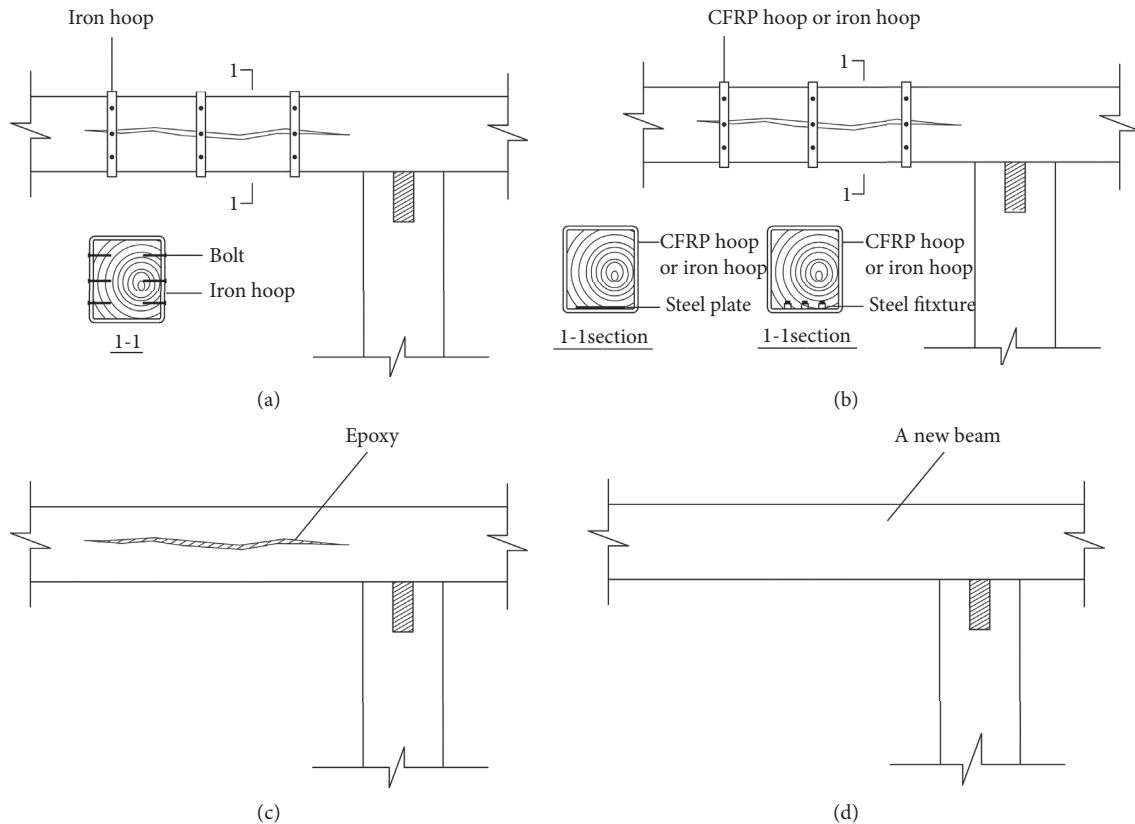


FIGURE 2: Four alternative restoration methods for  $C_1$ : (a) stabilizing by outer iron hoop; (b) inserting internal steel (CFRP stands for carbon fibre-reinforced polymer); (c) filling with epoxy; (d) replacing the component.

TABLE 6: Importance of experts expressed with SVNNS.

	$DM_1$	$DM_2$	$DM_3$	$DM_4$
Linguistic terms	M	M	I	VI
SVNNS	<0.50, 0.40, 0.45>	<0.50, 0.40, 0.45>	<0.80, 0.20, 0.15>	<0.90, 0.10, 0.05>

described by linguistic terms with its relevant SVNNS. Therefore, the weights of experts ( $e_k$ ) are determined by using equation (6):  $e_1 = 0.1950$ ,  $e_2 = 0.1950$ ,  $e_3 = 0.2899$ , and  $e_4 = 0.3201$ . Then, the evaluation values of these indices do need to be aggregated. We shall use equation (4), the single-valued neutrosophic weighted averaging (SVNWA) aggregation operator to aggregate these indices. Finally, we obtain the evaluation matrix  $R = (r_{ij})$  based on single-valued neutrosophic sets outlined in Table 7.

5.2. *The Calculation of Index Weights.* According to the BWM method introduced in Section 4.3.1, we calculate the subjective weights of four criteria. Firstly, the criteria shown in Table 1 are denoted by  $A_1$  to  $A_4$ ; among them, basic situation of components ( $A_1$ ) is the most important criterion, and restoration process ( $A_2$ ) is the least important criterion, which is confirmed by experts. Secondly, the pairwise comparison vectors for the best and the worst criteria are outlined in Tables 8 and 9. Table 8 represents that

TABLE 7: The aggregated SVNNS-based decision matrix.

Criteria	Index	Alternatives			
		$X_1$	$X_2$	$X_3$	$X_4$
$A_1$	$a_{11}$	<0.719, 0.281, 0.229>	<0.5, 0.5, 0.45>	<0.777, 0.223, 0.172>	<0.465, 0.525, 0.491>
	$a_{12}$	<0.761, 0.239, 0.187>	<0.506, 0.494, 0.442>	<0.8, 0.2, 0.15>	<0.545, 0.455, 0.398>
	$a_{13}$	<0.704, 0.296, 0.240>	<0.648, 0.352, 0.298>	<0.733, 0.267, 0.214>	<0.262, 0.709, 0.715>
	$a_{14}$	<0.625, 0.375, 0.325>	<0.473, 0.526, 0.476>	<0.777, 0.223, 0.172>	<0.453, 0.547, 0.496>
	$a_{15}$	<0.625, 0.375, 0.325>	<0.579, 0.421, 0.370>	<0.8, 0.2, 0.15>	<0.159, 0.791, 0.841>
	$a_{16}$	<0.191, 0.776, 0.790>	<0.492, 0.507, 0.456>	<0.186, 0.782, 0.796>	<1, 0, 0>
$A_2$	$a_{21}$	<0.281, 0.697, 0.690>	<0.765, 0.235, 0.183>	<0.534, 0.466, 0.416>	<0.714, 0.286, 0.232>
	$a_{22}$	<0.181, 0.769, 0.819>	<0.565, 0.435, 0.384>	<0.413, 0.587, 0.536>	<0.765, 0.235, 0.183>
	$a_{23}$	<0.35, 0.65, 0.6>	<0.825, 0.175, 0.121>	<0.456, 0.544, 0.493>	<0.766, 0.234, 0.169>
	$a_{24}$	<0.305, 0.680, 0.658>	<0.8, 0.2, 0.15>	<0.5, 0.5, 0.45>	<0.738, 0.263, 0.210>
$A_3$	$a_{31}$	<0.205, 0.756, 0.783>	<0.627, 0.373, 0.319>	<0.534, 0.466, 0.416>	<0.081, 0.869, 0.919>
	$a_{32}$	<0.761, 0.239, 0.187>	<0.623, 0.377, 0.323>	<0.534, 0.466, 0.416>	<0.133, 0.817, 0.867>
	$a_{33}$	<0.247, 0.720, 0.736>	<0.707, 0.293, 0.240>	<0.554, 0.446, 0.395>	<1, 0, 0>
	$a_{34}$	<0.836, 0.164, 0.109>	<0.589, 0.410, 0.354>	<0.534, 0.466, 0.416>	<0.1, 0.85, 0.9>
	$a_{35}$	<0.474, 0.526, 0.476>	<0.579, 0.421, 0.370>	<0.65, 0.35, 0.3>	<0.860, 0.140, 0.085>
	$a_{36}$	<0.576, 0.424, 0.364>	<0.612, 0.388, 0.337>	<0.474, 0.526, 0.476>	<0.2, 0.75, 0.8>
$A_4$	$a_{41}$	<0.825, 0.175, 0.121>	<0.533, 0.466, 0.416>	<0.777, 0.223, 0.172>	<0.701, 0.299, 0.244>
	$a_{42}$	<0.857, 0.143, 0.088>	<0.5, 0.5, 0.45>	<0.8, 0.2, 0.15>	<0.608, 0.392, 0.342>
	$a_{43}$	<0.886, 0.114, 0.062>	<0.530, 0.469, 0.418>	<0.8, 0.2, 0.15>	<0.625, 0.375, 0.325>

TABLE 8: Pairwise comparison vector of the most important criterion.

Criteria	$A_1$	$A_2$	$A_3$	$A_4$
Best criterion: $A_1$	1	6	2	4

TABLE 9: Pairwise comparison vector of the least important criterion.

Criteria	$A_1$	$A_2$	$A_3$	$A_4$
Worst criterion: $A_2$	6	1	4	2

the preference values of the best criteria ( $A_1$ ) over criterion ( $A_2$ ), criterion ( $A_3$ ), and criterion ( $A_4$ ) are 6, 2, and 4, respectively. The preference values of criteria ( $A_1$ ), criterion ( $A_3$ ), and criterion ( $A_4$ ) over the worst criterion ( $A_2$ ) are 6, 4, and 2, respectively, as shown in Table 9. Finally, the weight vector of criteria  $w^* = \{w_1^*, w_2^*, w_3^*, w_4^*\}$  is calculated by Equation (11), and we can get  $w_1^* = 0.5098$ ,  $w_2^* = 0.0784$ ,  $w_3^* = 0.2745$ ,  $w_4^* = 0.1373$ , and  $\xi^* = 0.0392$ . For the consistency ratio based on the BWM method, as  $a_{BW} = a_{12} = 6$ , the consistency index for this problem is 3.00 (shown in Table 4), and the consistency ratio according to equation (9) is  $0.0392/3.00 \approx 0.0131$ , which illustrates a very good consistency.

Afterwards, the weights of indices can be computed by applying the entropy weight method outlined in Section 4.3.2. First, by normalizing the evaluation indices by utilizing equation (12), we shall get the evaluation matrix  $R = (\beta_{ij})$ , which is shown in Table 10. Then, we can obtain the entropy weight of each index based on the normalized evaluation matrix.

At last, index weights can be acquired by combining the subjective weights of criteria with the entropy weights of indices, which is obtained as in Table 11.

5.3. *The Sequence of Restoration Methods.* We use the TODIM method based on MCGDM introduced in Section 4.4 to solve the restoration methods selection problem. First, we calculate the final dominance of restoration methods  $X_i$  over each other plan  $X_k$  under each index  $a_{ij}$  by using equation (16), and the parameter  $\theta$  is usually 1; the result can be shown in Table 12. Then, the global value of each restoration method is obtained by equation (17). Finally, according to value  $\epsilon_i$ , we could sort out restoration methods selection  $X_i$ , which is obtained as in Table 13. Hence, the most appropriate restoration method for  $C_1$  is “ $X_1$ ,” namely, stabilizing by outer iron hoop.

5.4. *Sensitivity Analysis.* The parameter  $\theta$  in TODIM is the loss attenuation coefficient that controls the influence caused when a loss occurs. We believe that if  $\theta < 1$ , the loss is amplified; if  $\theta > 1$ , the loss is attenuated. The prospect theory states that, in general, individuals are more sensitive to losses than gains, which suggests that  $\theta < 1$ . Therefore, the value of this parameter greatly affects the ranking order of the alternatives. Choosing a small  $\theta$  means we are looking for an alternative which provides less loss under all conditions; on the contrary, if we choose a big  $\theta$ , then we are looking for an alternative which provide greater benefits, even if we have losses on certain criteria [46]. For the purpose of analyzing the influence of different values of  $\theta$  on the final ranking orders, we take different  $\theta$  values to calculate the examples for restoration methods to check the stability of the ranking results. The results are outlined in Table 14 and Figure 3. We can see the different ranking orders calculated by different  $\theta$  clearly. When  $\theta \geq 0.8$ , the ranking order is the same as in the previous example, and the ranking order is  $X_1 > X_3 > X_2 > X_4$ ; when the loss attenuation coefficient becomes smaller,  $\theta \leq 0.5$ ,  $X_3$  and  $X_1$  are replaced, and the ranking result becomes  $X_3 > X_1 > X_2 > X_4$ . This proves that when the loss is

TABLE 10: The normalized evaluation matrix.

Criteria	Index	Alternatives			
		$X_1$	$X_2$	$X_3$	$X_4$
$A_1$	$a_{11}$	<0.719, 0.281, 0.229>	<0.5, 0.5, 0.45>	<0.777, 0.223, 0.172>	<0.465, 0.525, 0.491>
	$a_{12}$	<0.761, 0.239, 0.187>	<0.506, 0.494, 0.442>	<0.8, 0.2, 0.15>	<0.545, 0.455, 0.398>
	$a_{13}$	<0.704, 0.296, 0.240>	<0.648, 0.352, 0.298>	<0.733, 0.267, 0.214>	<0.262, 0.709, 0.715>
	$a_{14}$	<0.625, 0.375, 0.325>	<0.473, 0.526, 0.476>	<0.777, 0.223, 0.172>	<0.453, 0.547, 0.496>
	$a_{15}$	<0.625, 0.375, 0.325>	<0.579, 0.421, 0.370>	<0.8, 0.2, 0.15>	<0.159, 0.791, 0.841>
	$a_{16}$	<0.809, 0.224, 0.210>	<0.508, 0.493, 0.544>	<0.814, 0.218, 0.204>	<0, 1, 1>
$A_2$	$a_{21}$	<0.719, 0.303, 0.310>	<0.235, 0.765, 0.817>	<0.466, 0.534, 0.584>	<0.286, 0.714, 0.768>
	$a_{22}$	<0.819, 0.231, 0.181>	<0.435, 0.565, 0.616>	<0.587, 0.413, 0.464>	<0.235, 0.765, 0.817>
	$a_{23}$	<0.65, 0.35, 0.4>	<0.175, 0.825, 0.879>	<0.544, 0.456, 0.507>	<0.234, 0.766, 0.831>
	$a_{24}$	<0.695, 0.320, 0.342>	<0.2, 0.8, 0.85>	<0.5, 0.5, 0.55>	<0.262, 0.738, 0.790>
$A_3$	$a_{31}$	<0.205, 0.756, 0.783>	<0.627, 0.373, 0.319>	<0.534, 0.466, 0.416>	<0.081, 0.869, 0.919>
	$a_{32}$	<0.761, 0.239, 0.187>	<0.623, 0.377, 0.323>	<0.534, 0.466, 0.416>	<0.133, 0.817, 0.867>
	$a_{33}$	<0.753, 0.280, 0.264>	<0.293, 0.707, 0.760>	<0.446, 0.554, 0.605>	<0, 1, 1>
	$a_{34}$	<0.836, 0.164, 0.109>	<0.589, 0.410, 0.354>	<0.534, 0.466, 0.416>	<0.1, 0.85, 0.9>
	$a_{35}$	<0.474, 0.526, 0.476>	<0.579, 0.421, 0.370>	<0.65, 0.35, 0.3>	<0.860, 0.140, 0.085>
	$a_{36}$	<0.424, 0.576, 0.636>	<0.388, 0.612, 0.663>	<0.526, 0.474, 0.524>	<0.8, 0.25, 0.2>
$A_4$	$a_{41}$	<0.825, 0.175, 0.121>	<0.533, 0.466, 0.416>	<0.777, 0.223, 0.172>	<0.701, 0.299, 0.244>
	$a_{42}$	<0.857, 0.143, 0.088>	<0.5, 0.5, 0.45>	<0.8, 0.2, 0.15>	<0.608, 0.392, 0.342>
	$a_{43}$	<0.886, 0.114, 0.062>	<0.530, 0.469, 0.418>	<0.8, 0.2, 0.15>	<0.625, 0.375, 0.325>

TABLE 11: The weights of criteria and index for restoration methods selection.

Criteria	Weight	Index	Weight
$A_1$	0.5098	$a_{11}$	0.0705
		$a_{12}$	0.0882
		$a_{13}$	0.1025
		$a_{14}$	0.0570
		$a_{15}$	0.1050
		$a_{16}$	0.1232
$A_2$	0.0784	$a_{21}$	0.0142
		$a_{22}$	0.0132
		$a_{23}$	0.0135
		$a_{24}$	0.0140
$A_3$	0.2745	$a_{31}$	0.0539
		$a_{32}$	0.0532
		$a_{33}$	0.0640
		$a_{34}$	0.0578
		$a_{35}$	0.0444
		$a_{36}$	0.0368
$A_4$	0.1373	$a_{41}$	0.0302
		$a_{42}$	0.0280
		$a_{43}$	0.0302

TABLE12: The final dominance of restoration methods alternatives ( $\theta = 1$ ).

	$X_1$	$X_2$	$X_3$	$X_4$
$X_1$	0	-1.5129	-0.0042	-2.1098
$X_2$	1.5129	0	1.4057	-0.9879
$X_3$	0.0042	-1.4057	0	-2.0915
$X_4$	2.0081	0.8676	2.0915	0

magnified, the decision-makers tend to choose  $X_3$ . When the loss is reduced, that is, the larger the loss attenuation coefficient, the lower the degree of evasion by the decision-

TABLE 13: Ranking order of restoration methods by  $\epsilon_i$ .

Alternatives	Values $\epsilon_i$	Ranking orders
$X_1$	1	1
$X_2$	0.3601	3
$X_3$	0.9963	2
$X_4$	0	4

TABLE 14: Ranking order of restoration methods with different  $\theta$ .

Different values of $\theta$	Values $\epsilon_i$				Ranking orders
	$X_1$	$X_2$	$X_3$	$X_4$	
$\theta = 2.25$	1	0.2803	0.9464	0	$X_1 > X_3 > X_2 > X_4$
$\theta = 2.0$	1	0.3246	0.9893	0	$X_1 > X_3 > X_2 > X_4$
$\theta = 1.5$	1	0.3386	0.9922	0	$X_1 > X_3 > X_2 > X_4$
$\theta = 1.0$	1	0.3601	0.9963	0	$X_1 > X_3 > X_2 > X_4$
$\theta = 0.8$	1	0.3716	0.9985	0	$X_1 > X_3 > X_2 > X_4$
$\theta = 0.5$	0.9973	0.3925	1	0	$X_3 > X_1 > X_2 > X_4$
$\theta = 0.3$	0.9937	0.4101	1	0	$X_3 > X_1 > X_2 > X_4$

maker, the decision-makers tend to choose  $X_1$ . It means that adjusting the decision-maker's risk aversion tendency will affect the ranking results, and it also indicates that the psychological behavior of the decision-maker will affect one's decision-making. The results of sensitivity analysis show that the proposed method can well express the cognition of decision-makers, quantify the uncertainty to a certain extent, and avoid the loss and distortion of information as much as possible. Therefore, to an extent, the feasibility and robustness of the proposed model is verified.

5.5. Comparison Analysis. As explained in Section 2, the model is proposed to select restoration methods for wood components of Chinese architectures. In order to verify that

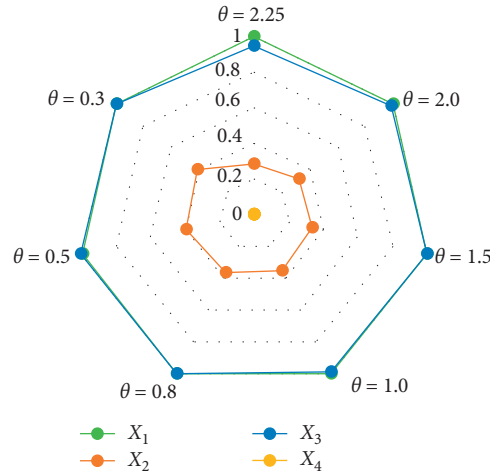


FIGURE 3: The radar chart displaying the result of sensitivity analysis.

TABLE 15: The comparison of different ranking methods.

Alternatives	TOPSIS			VIKOR		
	Close degree	Ranking orders	$S_i$	$R_i$	$Q_i$	Ranking orders
$X_1$	0.6666	$X_3 > X_1 > X_2 > X_4$	0.3119	0.0531	0.0099	$X_1 > X_3 > X_2 > X_4$
$X_2$	0.4413		0.5142	0.0843	0.4615	
$X_3$	0.7533		0.3276	0.0508	0.0244	
$X_4$	0.3655		0.6328	0.0244	1.0000	

the proposed model can be validly and practically used to identify the most suitable restoration method for specific wood components, we employ the TOPSIS [47] and VIKOR [48] to make comparative analysis of the above empirical study. The ranking order of the four restoration methods obtained by TOPSIS and VIKOR is outlined in Table 15. From Table 15, the ranking result of the proposed model is consistent with those computed by the TOPSIS when  $\theta \leq 0.5$ . And the ranking order of the case study is the same as those computed by VIKOR. But in the calculation of the VIKOR method,  $Q(X_1) - Q(X_3) < 0.25$ , it means the ranking results of  $X_1$  and  $X_3$  are similar, so both  $X_1$  and  $X_3$  are close to the ideal restoration method. It can be seen that TODIM can better reflect the psychological behavior of the decision-makers and can flexibly respond to the trend of risk aversion. Therefore, the validity of the proposed model can be verified. Compared with the existing approaches for restoration methods selection for wood components of Chinese architectures, the advantages of the model proposed can be summarized as follows:

- (i) The model comprehensively considers the subjective and objective criteria in the index system. According to the index system, the evaluation information characterized by multigranularity linguistic terms is obtained from the experts, and the single-valued neutrosophic set is used to quantify the expert evaluation information. Therefore, this makes the selection of restoration methods more realistic.

- (ii) In order to solve the ranking problem with unknown criteria weights and index weights in the TODIM scheme, combine BWM method and entropy weight method to calculate the criteria and index weights, respectively. As a result, index weights are reliable and more accurate.
- (iii) The proposed model employs TODIM prioritized alternative restoration methods. The TODIM method fully considers the risk aversion of decision-makers and reflects the preferences of decision-makers by adjusting parameter  $\theta$ . Hence, the proposed restoration methods selection model based on TODIM with single-valued neutrosophic sets is a suitable method to solve multicriteria group decision-making problems considering the psychological behavior of decision-makers.

## 6. Conclusion

A selection model of restoration methods for wood components of Chinese ancient architectures has been developed in this paper, which is helpful to assisting experts to solve the problem of selecting appropriate restoration methods. Subjective and objective criteria have been simultaneously utilized in the establishment of index system. Moreover, single-valued neutrosophic sets are employed to characterize the evaluation information given by experts in multigranularity language terms and to quantify the assessment information. In addition, the BWM method and entropy

weight method are used to obtain the criteria and index weights. Finally, the TODIM method has been used to get the prioritization of restoration methods. The proposed model has been conducted to an empirical study in Fuhoutang for restoration methods selection of a specific wood component. The detailed process of the model has been illustrated in this paper. Furthermore, the sensitivity analysis and comparison analysis proved the reliability and effectiveness of the proposed selection model.

In conclusion, the proposed model not only improves extant approaches in the field of restoration methods decision-making for Chinese ancient architectures but also gives rational support to experts in the process of decision-making. So, both theoretical development and practical application are reflected in this work. There are several implications for possible directions of further study. First, more types of information of restoration methods selection should be taken into consideration in the proposed model in future studies. Second, the model can be extended to apply other decision methods, such as TOPSIS and VIKOR. Finally, the proposed selection model can also be applied to other kinds of components of Chinese ancient architectures besides wood components.

## Data Availability

The data used to support the findings of this study are included within the article.

## Conflicts of Interest

The authors declare that there are no conflicts of interest.

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