

Research Article

The Efficiency of Economic Performance, Electricity Consumption, and Environmental Pollutants in Taiwan

Wen-jie Zou,¹ Tai-Yu Lin^(b),² Yung-ho Chiu^(b),³ Ting Teng,⁴ and Kuei Ying Huang³

¹Institute of Economics of Fujian Normal University, Fuzhou, China

²Department of Business Administration, National Cheng Kung University, No.1, University Road, Tainan City 701, Taiwan ³Department of Economics, Soochow University 56, Kueiyang St., Sec. 1, Taipei 10048, Taiwan

⁴Business School, Soochow University 56, Kueiyang St., Sec. 1, Taipei 10048, Taiwan

Correspondence should be addressed to Tai-Yu Lin; eickyla@gmail.com

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Finding the balance between economic development and environmental protection is a major problem for many countries around the world. Air pollution caused by economic growth has caused serious damage to humans' living environment, and as improving energy and resource efficiencies is the first priority, many countries are targeting to move towards a sustainable environment and economic development. This study uses the modified dynamic SBM (slack-based measure) model to explore the economic efficiency and air pollutants emission efficiency in Taiwan's counties and cities from 2012 to 2015 by taking labor, motor vehicles, and electricity consumption as inputs and average disposable income as output. Particulate matter ($PM_{2.5}$), nitrogen oxide emissions (NO_2), and sulfur oxide emissions (SO_2) are undesirable outputs, whereas factory fixed assets are a carry-over variable, and the results show the following: (1) the regions with the best overall efficiency between 2012 and 2015 include Taipei City, Keelung City, Hsinchu City, Chiayi City, and Taitung County; (2) in counties and cities with poor overall efficiency performance, the average disposable income per household has no significant relationship with air pollutant emissions; (3) in counties and cities where overall efficiency is poor, the average efficiency of each household's disposable income is small; and (4) except for the five counties and cities with the best overall performance, the three air pollutants in the other fourteen counties and cities are high. Overall, the air pollution of most areas needs improvement.

1. Introduction

Taiwan, one of the Asian four dragons, has high energy (electricity) consumption, population, and vehicle density and severe air pollution. This study is going to explore the economic performance efficiency, energy consumption (electricity), and air pollutant emission efficiency of Taiwan.

From the World Health Organization's [1] national ranking of $PM_{2.5}$ concentrations in September 2011, Taiwan ranks 32nd among 38 survey countries. Among nearly 600 cities worldwide, Chiayi and Kaohsiung made it among the top ten. From the average concentration of $PM_{2.5}$ in 2013, the risk of lung cancer and asthma in

children increased to 15%, with the risk from stroke, heart disease, and chronic respiratory disease increasing by 25%. In 2014, more than 6,000 deaths in Taiwan were caused by exposure to $PM_{2.5}$.

Indeed, $PM_{2.5}$ causes damage in Taiwan. The impact of CO_2 , SO_2 , and $PM_{2.5}$ cannot be overlooked. Most studies in the literature explore the effects of energy and environmental efficiencies on CO_2 , SO_2 , and NO_2 emissions. Many researches analyze the energy efficiency of China. Wu et al. [2] use two-stage network DEA (data envelopment analysis) to assess China's energy conservation and emission reduction efficiency during 2006–2010. Energy saving and emission reduction in the eastern region are better than in the central and western regions. Lin and Du [3] employ the

new nonradial directional distance function to assess regional energy and carbon dioxide emissions efficiency in China from 1997 to 2009. The results show that most of China's performances in energy use and carbon dioxide emissions are poor. Industrial sector expansion is negatively correlated with China's regional energy and CO₂ emissions performance. Wang et al. [4] utilize multidirectional efficiency analysis (MEA) to look at regional energy and emissions efficiencies in China from 1997 to 2010. The eastern region is more efficient than the central and western regions. Hebei, Shanxi, Inner Mongolia, Shandong, Henan, and Hubei have higher potentials for energy conservation and emission reduction. Li et al. [5] collect energy data from 2000 to 2009 in China and analyze the impact of three internal factors (economic structure, energy consumption structure, and technological progress) on energy intensity in China using the DEA-based Malmquist method. They convert technology into three components to see the different impacts in various regions. Other researches such as [6-19] also focus on the energy efficiency of China.

Some in the literature analyze the impacts of energy and environmental efficiencies on PM2.5 emissions, such as [20-30]. Martínez [20] uses two-stage DEA to assess the energy efficiency of non-energy-intensive industries (NEISs) in Germany and Colombia from 1998 to 2005. The highest energy efficiency in non-energy-intensive industries (NEISs) in Colombia is derived from the cost minimization model, showing that energy prices are not the key to improving energy efficiency. Sueyoshi and Yuan [21] utilize the DEA model to explore regional environmental efficiency performance in China from 2013 to 2014. The Chinese government should allocate economic resources to cities located in the northwestern region (including Lanzhou, Xining, Yinchuan, and Urumqi) and strengthen stricter regulation of energy consumption in major urban environments (such as Beijing, Tianjin, Shanghai, and Chongqing). Ma et al. [22] use the spatial autoregressive model to analyze the spatial diffusion effects of PM_{2.5} in 152 cities in China. PM_{2.5} is significantly affected by geospatial and regional economies. Li et al. [23] utilize the multilevel frontiers DEA model to explore the environmental efficiency of 49 cities in China. Their results present that PM_{2.5} and SO₂ emissions are significantly related to urban population and energy technologies.

There are two contributions of this study. First, we use small economy as the research sample. As can be seen from the above literature, most of the research on air pollutants is based on large economies, such as China. These large economies have rich natural resources and focus on industrial and manufacturing development. However, the problem of air pollution is not limited to large economies, and it cannot be overlooked in some non-industrial-oriented small economies. For example, according to the Taiwan Environmental Protection Agency's 2016 and 2017 Air Quality Monitoring Report [31], the annual air quality indicators (AQIs) hit 39.34% and 42.1%, respectively, or out of reach from a good grade of 50%. The other contribution is model modification. Most past models are still dominated by radial (Charnes, Cooper, and Rhodes model, abbreviation as CCR model; Banker, Charnes, and Cooper model, abbreviation as BCC model), nonradial (slack-based measure, abbreviation as SBM), two-stage DEA analysis, and directional distance function. However, these models employ static analysis, lack dynamic considerations, and cannot understand the changes in efficiency of energy and environmental pollutants. Thus, this study employs the modified dynamic SBM to evaluate the situation for each county and city. We utilize 19 counties and cities in Taiwan from 2012 to 2015 with data on the number of employed people, motor vehicles, and electricity consumption and take the average disposable income per household as output, PM_{2.5}, nitrogen oxide emissions (NO₂), and sulfur oxide emissions (SO_2) as undesirable outputs (recently, the problem of air pollution has drawn the attention of many scholars; because the issue of CO₂ emission has been analyzed by many researches, this study focuses on the other air pollutants (SO₂, NO₂, and PM_{2.5} in Taiwan), and fixed assets as the carry-over variable). By above input and output variables, this study evaluates the economic performance, electricity consumption efficiency, and air pollutant emission efficiency of Taiwan.

2. Research Methods

2.1. DEA. Farrell [32] proposes the efficiency frontier, but the model is only for a single input and a single output. Charnes et al. [33] extend Farrell's theory for multiple inputs and multiple outputs, naming it the CCR model. Banker et al. [34] propose their BCC model, which can determine variable returns to scale. For the first time, Tone [35] proposes nonradial and nonoriented estimation methods through slacks, calling it the SBM model. Many efficiency assessment methods have been subsequently proposed, such as super DEA, hybrid DEA, network DEA, two-stage DEA, fuzzy DEA, and three-stage DEA.

2.2. Dynamic DEA. Many research studies utilize static analysis, with dynamic DEA window analysis to analyze dynamic models. Färe et al. [36] offer the Malmquist index, but during two periods, the researchers do not analyze the impact of carry-over. Färe and Grosskopf [37] then offer a new analysis of the dynamic impact of consecutive activities. Chen [38] and K. S. Park and K. Park [39] subsequently present SBM studies of several dynamics, with the dynamic analysis model extended into a slack-based measure by Tone and Tsutsui [40]. In order to carry-over activities as a form of connectivity, they propose the SBM (slack-based measures) dynamic DEA model. Tone and Tsutsui [40] develop the model into SBM dynamic analysis, with carry-over activities as a link, and the existence of activities divided into a four-model analysis: (1) desirable (Z^{good}); (2) undesirable (Z^{bad}); (3) discretionary (Z^{free}); (4) nondiscretionary (Z^{fix}), with carry-over variables from period t to period t+1.

The following is the nonoriented model:

$$\rho_{0}^{*} = \min \frac{(1/T)\sum_{t=1}^{T} W^{t} \left[1 - (1/m + n \text{bad}) \left(\sum_{i=1}^{m} \left(w_{i}^{-} s_{it}^{-} / x_{iot} \right) + \sum_{r=1}^{n \text{bad}} \left(s_{it}^{\text{bad}} / z_{rot}^{\text{bad}} \right) \right) \right]}{(1/T)\sum_{t=1}^{T} W^{t} \left[1 + (1/s + n \text{good}) \left(\sum_{l=1}^{s} \left(w_{i}^{+} s_{it}^{+} / y_{iot} \right) + \sum_{r=1}^{n \text{good}} \left(s_{it}^{\text{good}} / z_{rot}^{\text{good}} \right) \right) \right]},$$
(1)

$$\sum_{r=1}^{n} z_{rjt}^{\alpha} \lambda_{j}^{t} = \sum_{j=1}^{n} z_{rjt}^{\alpha} \lambda_{j}^{t+1}, \quad (\forall i; t = 1, \dots, T-1).$$
(2)

Equation (2) is the connection equation between t and t + 1.

$$\begin{aligned} x_{iot} &= \sum_{j=1}^{n} x_{ijl} \lambda_{j}^{t} + s_{it}^{-}, \quad (i = 1, \dots, m; t = 1, \dots, T), \\ x_{iot}^{fix} &= \sum_{j=1}^{n} x_{iol}^{fix} \lambda_{j}^{t}, \quad (i = 1, \dots, p; t = 1, \dots, T), \\ y_{lot} &= \sum_{l=1}^{n} y_{ljl} \lambda_{j}^{t} - s_{lt}^{+}, \quad (l = 1, \dots, s; t = 1, \dots, T), \\ y_{lot}^{fix} &= \sum_{l=1}^{n} y_{lol}^{fix} \lambda_{j}^{t}, \quad (l = 1, \dots, r; t = 1, \dots, T), \\ z_{rot}^{good} &= \sum_{r=1}^{n} z_{rot}^{good} \lambda_{j}^{t} - s_{rt}^{good}, \quad (r = 1, \dots, n \text{good}; t = 1, \dots, T), \\ z_{rot}^{fix} &= \sum_{r=1}^{n} z_{rjt}^{had} \lambda_{j}^{t} + s_{rt}^{had}, \quad (r = 1, \dots, n \text{good}; t = 1, \dots, T), \\ z_{rot}^{fix} &= \sum_{r=1}^{n} z_{rjt}^{fix} \lambda_{j}^{t} + s_{rt}^{fice}, \quad (r = 1, \dots, n \text{fix}; t = 1, \dots, T), \\ z_{rot}^{fix} &= \sum_{r=1}^{n} z_{rjt}^{fix} \lambda_{j}^{t}, \quad (r = 1, \dots, n \text{firee}; t = 1, \dots, T), \\ z_{rot}^{fix} &= \sum_{r=1}^{n} z_{rjt}^{fix} \lambda_{j}^{t}, \quad (r = 1, \dots, n \text{fire}; t = 1, \dots, T), \\ \sum_{j=1}^{n} \lambda_{j}^{t} &= 1 \quad (t = 1, \dots, T), \\ \lambda_{j}^{t} &\geq 0, s_{rt}^{-1} \geq 0, s_{rt}^{t} \geq 0, s_{rt}^{good} \geq 0 \text{ and } s_{rt}^{free} : \text{ free} (\forall i, t). \end{aligned}$$

The most efficient solution is

$$\rho_{0t} = \frac{1 - (1/m + n\text{bad}) \left(\sum_{i=1}^{m} \left(w_i^- s_{iot}^{-*} / x_{iot} \right) + \sum_{r=1}^{n\text{bad}} \left(s_{rot}^{\text{bad}} * / z_{rot}^{\text{bad}} \right) \right)}{1 + (1/s + n\text{good}) \left(\sum_{l=1}^{s} \left(w_i^+ s_{it}^{+*} / y_{lot} \right) + \sum_{r=1}^{n\text{good}} \left(s_{rot}^{\text{good}} * / z_{rot}^{\text{good}} \right) \right)},$$

$$(i = 1, \dots, T).$$

$$(4)$$

2.3. The Modified Dynamic SBM Model. Since this study considers the undesirable output in the dynamic SBM

model, Tone and Tsutsui's [40] dynamic SBM model can be modified to be the undesirable output in the dynamic SBM model. Suppose the observation is a J (J=1, ..., n) dimension decision-making unit (DMU) set in which the DMU under evaluation is represented by DMU_O and subject to DMU_O \in J. The input and output used to compute the efficiency are labeled as m inputs x_{ijt} (i=1, ..., m) and soutputs Y_{ljt} , respectively. Let output Y be divided into (Y^g , Y^b), where Y^g is the desirable output, Y^b is the undesirable output, and Z^{good} is carried over from period t to period t+1. The following is the nonoriented model:

$$\theta_0^* = \min \frac{(1/T)\sum_{t=1}^T W^t \left[1 - (1/m)\sum_{i=1}^m s_{it}^- / x_{iot}\right]}{(1/T)\sum_{t=1}^T W^t \left[1 + (1/s_1 + s_2 + ngood) \left[\sum_{l=1}^{s_1} s_{jt}^{+g} / y_{lot}^g + \sum_{l=1}^{s_2} s_{jt}^{-b} / y_{lot}^b + \sum_{r=1}^{ngood} s_{rt}^{good} / z_{rot}^{good}\right]\right]}.$$
(5)

The following six equations show the connection equation between t and t + 1:

$$\sum_{j=1}^{n} z_{ijt}^{\alpha} \lambda_{j}^{t} = \sum_{j=1}^{n} z_{ijt}^{\alpha} \lambda_{j}^{t+1}, \quad (\forall i; t = 1, \dots, T - 1),$$

$$x_{iot} = \sum_{i=1}^{m} x_{ijt} \lambda_{i}^{t} + s_{it}^{-}, \quad (i = 1, \dots, m; t = 1, \dots, T),$$

$$y_{lot} = \sum_{l=1}^{s1} y_{lot}^{+g} \lambda_{j}^{t} - s_{lt}^{+g}, \quad (l = 1, \dots, s1; t = 1, \dots, T),$$

$$y_{lot} = \sum_{l=1}^{s2} y_{lot}^{-b} \lambda_{j}^{t} - s_{lt}^{-b}, \quad (l = 1, \dots, s2; t = 1, \dots, T),$$

$$z_{rot}^{good} = \sum_{r=1}^{rgood} z_{rot}^{good} \lambda_{j}^{t} - s_{rt}^{good}, \quad (R = 1, \dots, ngood; t = 1, \dots, T),$$

$$\sum_{j=1}^{n} \lambda_{j}^{t} = 1 \quad (t = 1, \dots, T),$$

$$\lambda_{j}^{t} \ge 0, s_{it}^{-t} \ge 0, \ s_{lt}^{-b} \ge 0, \ s_{rt}^{good} \ge 0.$$

The most efficient solution is

$$\rho_{0t} = \frac{1 - (1/m) \left(\sum_{i=1}^{m} \left(s_{iot}^{-*} / x_{iot} \right) \right)}{1 + (1/s1 + s2 + ngood) \left(\sum_{l=1}^{s1} \left(s_{jt}^{+g*} / y_{lot} \right) + \sum_{l=1}^{s2} \left(s_{jt}^{-b*} / y_{lot} \right) + \sum_{r=1}^{ngood} \left(s_{rot}^{good*} / z_{rot}^{good} \right) \right)}, \quad (i = 1, \dots, T).$$
(7)

In equation (5), W^t denotes the weight of time and the range of time of this model is from 2012 to 2015. x_{iot} indicates outputs, which are labor, motor vehicle number, and electricity consumption. y_{iot}^{+g} denotes desirable output which is disposable income. y_{iot}^{-b} denotes undesirable outputs, which are PM_{2.5}, NO_{x3} and SO₂. Z_{rot}^{good} is carry over, which is fixed assets. s_{it}^{-} indicates input slack. s_{jt}^{+g} indicates desirable output slack. s_{rot}^{good} indicates undesirable output slack. s_{rot}^{good} indicates undesirable output slack. s_{rot}^{good} indicates undesirable output slack.

This study lists labor, motor vehicle number, and electricity consumption as inputs. Suspended particulate emissions (PM_{2.5}), nitrogen oxide emissions (NO₂), and sulfur oxide emissions (SO_2) are undesirable outputs. Fixed assets are a carry-over variable. Table 1 lists the details.

The number of motor vehicles, electricity consumption, average disposable income, and NO_2 , SO_2 , and $PM_{2.5}$ efficiency indices.

Hu and Wang [19] total-factor energy efficiency index is used to overcome any possible bias in the traditional energy efficiency indicator. For each specific evaluated country, we calculate the number of motor vehicles, electricity consumption, average disposable income, and NO₂, SO₂, and PM_{2.5} efficiencies from the following equations:

the number of motor vehicles' efficiency =
$$\frac{\text{target motor vehicles' efficiency input }(i, t)}{\text{actual motor vehicles' efficiency input }(i, t)}$$
, (8)
electricity consumption efficiency = $\frac{\text{target electricity consumption input }(i, t)}{\text{actual electricity consumption input }(i, t)}$, (9)

average disposable efficiency =
$$\frac{\text{actual average disposible income output}(i, t)}{\text{target average disposible output}(i, t)}$$
, (10)

$$NO_2 \text{ efficiency} = \frac{\text{target } NO_2 \text{ undesirable output}(i, t)}{\text{actual } NO_2 \text{ undesirable output}(i, t)},$$
(11)

$$PM_{2.5} \text{ efficiency} = \frac{\text{target } PM_{2.5} \text{ undesirable output } (i, t)}{\text{actual } PM_{2.5} \text{ undesirable output } (i, t)}$$
(12)

$$SO_2 \text{ efficiency} = \frac{\text{target } SO_2 \text{ undesirable output}(i, t)}{\text{actual } SO_2 \text{ undesirable output}(i, t)}.$$
(13)

The efficiency index indicates the ratio of target value and actual value. The target value indicates the most efficient value. Thus, the efficiency index denotes the difference of actual vale and target value. The index (ratio) equals to 1 when the actual value reaches the target value, and the actual value is most efficient. The index is more efficient when the value is close to 1.

If the target motor vehicle number and electricity consumption input equal the actual inputs and the NO₂, PM_{2.5}, and SO₂ outputs equal the actual undesirable outputs, then the motor vehicle number, electricity consumption, and NO₂, PM_{2.5}, and SO₂ efficiencies equal 1, indicating no room for improvement on their efficiency. The actual value reaches the target. If the target motor vehicle number and electricity consumption inputs are less than the actual input and the NO₂, PM_{2.5}, and SO₂ outputs are less than the actual undesirable outputs, then the motor vehicle number, electricity consumption" and NO₂, PM_{2.5}, and SO₂ efficiencies are less than 1, indicating the actual value is inefficiency. There is room for improvement on actual value.

If the target average disposable income output is equal to the actual average disposable income output, then the average disposable income efficiency equals 1, indicating overall efficiency. If the actual average disposable income output is less than the target average disposable income output, then the average disposable income efficiency is less than 1, indicating overall inefficiency.

3. Empirical Results and Analysis

3.1. Sources and Variables

3.1.1. Data Source. This research takes Taiwan as a case study from 2012 to 2015, including New Taipei City, Taipei City, Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Yilan County, Hsinchu County, Miaoli County, Changhua County, Nantou County, Yunlin County, Chiayi County, Pingtung County, Taitung County, Hualien County, Keelung City, Hsinchu City, and Chiayi City. The source is from Taiwan Statistics Department, Taiwan Power Company, and the Environmental Protection Agency of the Executive Yuan. The software used by this research is MaxDEA. This software is a benefit for DEA analysis, especially for model with undesirable output. 3.1.2. Variable and the Structure of Model. This is a dynamic model with several periods, such as period t and period t + 1. The inputs are labor, motor vehicle number, and electricity consumption. Labor and electricity consumption are used for economic development. Electricity is the main energy consumption of Taiwan. A large amount of air pollutants are generated during the production of electricity (ex: thermal power). Vehicles are a source of air pollutants in daily life.

There are two kinds of output. The desirable output is average disposable income which is an indicator of economic performance. The undesirable outputs are air pollutant which is generated by economic development and citizen's daily life. The carry-over factor which continues to each period (ex: period t to period t+1) is fixed assets. The linkage of variables is shown in Figure 1.

3.2. Statistics of Input and Output Variables. Table 2 summarizes the statistics of Taiwan's counties and cities from 2012 to 2015. In 2012, the average number of laborers is 569,474, the maximum is 1,892,000 in New Taipei City, and the minimum is 103,000 in Taitung County, with a standard deviation of 523,758. The average number of motor vehicles is 1,166,673, with a maximum of 3,309,078 units in New Taipei City, a minimum of 246,208 units in Taitung County, and a standard deviation of 1,013,652 units. The average electricity consumption is 7.819 billion, the maximum is 22.399 billion in New Taipei City, the minimum is 485.1 million in Taitung County, and the standard deviation is 7.529 billion degrees. The average yearly disposable income is NT\$874,514, the maximum is NT\$1,278,278 in Taipei City, the minimum is NT\$670,017 in Taitung County, and the standard deviation is NT\$158,827. The average amount of suspended particulate emissions is 3,941 metric tons, the maximum is 10,696 metric tons in Kaohsiung City, the minimum is 514 metric tons in Chiavi City, and the standard deviation of 2,631. The average sulfur oxide emissions are 6,397 metric tons, with a maximum of 42,929 metric tons in Kaohsiung City, a minimum of 60 metric tons in Chiayi City, and a standard deviation of 10,594 metric tons. The average NOx emissions are 20,213 metric tons, with a maximum of 76,826 metric tons in Kaohsiung City, a minimum of 2,281 metric tons in Chiayi City, and a standard deviation of 19,626 metric tons. The average fixed asset investment for a factory is NT\$56,753,880 thousand, the maximum value is TABLE 1: Definitions of variables.

	Variable	Definition
	Labor	Above fifteen-year-old paid worker or engaged in unpaid family work for more than 15 hours (unit: person)
Input	Motor vehicle number	Number of motor vehicles with uniform licenses to the supervision authorities at the end of the year (unit: vehicle)
	Electricity consumption	Electricity sold to the service industry, government schools, agriculture, forestry, fisheries, and industrial sales (unit: degree)
Desirable output	Average disposable income	Disposable income/total number of households (unit: NT\$)
Undooirable	Suspended particulate emissions	Total emissions of suspended particulates (PM _{2.5}) (unit: metric tons)
output	NOx emissions	Total emissions of nitrogen oxides (including nitrogen monoxide and nitrogen dioxide) (unit: metric tons)
	Sulfur oxide emissions	Total emissions of sulfur oxides (including sulfur dioxide) (unit: metric tons)
Carry-over	Fixed assets	The amount of fixed assets newly added by the factory in normal operations, including equipment investment (antipollution equipment, machinery and equipment, transportation vehicles, and other equipment), land acquisition, dormitory, factory warehouse office, and other construction projects (unit: NT\$1,000)



FIGURE 1: The structure of the model.

NT\$199,155,007 thousand in Tainan City, the minimum is NT\$324,609 thousand in Chiayi City, and the standard deviation is NT\$66,919,221 thousand (Figure 2).

According to Table 2, regardless of the amount of labor, motor vehicles, and electricity consumption, the maximum values are mainly concentrated in New Taipei City and Tainan City. The minimum values are mainly concentrated in Taitung County and Chiayi City. For average disposable income, the maximum value in the 4 years is in Taipei City. The minimum values are mainly concentrated in Taitung County and Chiayi City. The maximum emission of suspended particulates is mainly in Kaohsiung City, and the minimum emissions are in Chiayi City. The maximum emissions of sulfur oxides are in Kaohsiung City, and the minimum emissions are in Chiayi City. The maximum fixed asset investment for a factory is in Tainan City, and the minimum value is in Taitung County. 3.3. *Empirical Analysis*. This study explore the overall efficiency of Taiwan's counties and cities from 2012 to 2015.

3.3.1. Overall Efficiency. As shown in Table 3, the overall efficiency average is 0.8215, and the average efficiency for each year from 2012 to 2015 is, respectively, 0.8360, 0.7984, 0.8199, and 0.8370. The room for improvement is still between 16.3% and 20.2%. The four-year average efficiency maximum is 1 in Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. The lowest 4-year average efficiency is in Tainan City. The bottom three rankings are Yunlin County, Changhua County, and Tainan City.

The average efficiency in 2012 is 0.8360, and the most efficient regions are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. The bottom three are Taichung City, Yunlin County, and Tainan City. The average efficiency in 2013 is 0.7984, and the most efficient are Taipei

Variable		2012	2013	2014	2015
I <i>nputs</i> Labor (people)	Maximum Minimum Average Standard	1,892,000 (New Taipei City) 103,000 (Taitung County) 569,474 523,758	1,910,000 (New Taipei City) 104,000 (Taitung County) 574,947 529,741	1,927,000 (New Taipei City) 104,000 (Taitung County) 580,736 534,914	1,945,000 (New Taipei City) 104,000 (Taitung County) 586,947 541,477
Motor vehicles	deviation Maximum Minimum Average Standard deviation	3,309,078 (New Taipei City) 246,208 (Taitung County) 1,166,673 1,013,652	3,233,275 (New Taipei City) 233,394 (Taitung County) 1,125,181 979,776	3,178,499 (New Taipei City) 230,890 (Taitung County) 1,110,507 966,127	3,183,551 (New Taipei City) 230,954 (Taitung County) 1,115,854 971,184
Electricity consumption (degrees)	Maximum Minimum Average Standard	22,399,088,277 (New Taipei City) 485,166,744 (Taitung County) 7,819,496,456 7,529,994,233	22,850,473,858 (Taoyuan City) 488,240,891 (Taitung County) 7,988,861,231 7,694,682,886	23,045,858,780 (Taoyuan City) 496,469,053 (Taitung County) 8,102,790,831 7,811,168,091	22,801,815,338 (Taoyuan City) 520,574,022 (Taitung County) 8,121,363,829 7,826,312,606
<i>Desirable output</i> Average disposable income (NT\$)	Maximum Minimum Average Standard deviation	1,278,278 (Taipei City) 670,017 (Taitung County) 874,514 158,827	1,279,195 (Taipei City) 676,390 (Taitung County) 889,033 171,147	1,292,604 (Taipei City) 667,933 (Chiayi City) 896,941 182,797	1,314,031 (Taipei City) 636,162 (Taitung County) 895,059 167,073
<i>Undesirable output</i> Suspended particulate emissions (PM _{2.5}) (metric tons)	Maximum Minimum Average Standard deviation	10,696 (Kaohsiung City) 514 (Chiayi City) 3,941 2,631	10,336 (Kaohsiung City) 491 (Chiayi City) 3,901 2,606	10,174 (Kaohsiung City) 479 (Chiayi City) 3,825 2,557	9,893 (Kaohsiung City) 471 (Chiayi City) 3,742 2,487
Sulfur oxide emissions (SO_2) (metric tons)	Maximum Minimum Average Standard deviation	42,929 (Kaohsiung City) 60 (Chiayi City) 6,397 10,594	37,849 (Kaohsiung City) 44 (Chiayi City) 5,960 9,614	37,132 (Kaohsiung City) 44 (Chiayi City) 5,845 9,428	35,667 (Kaohsiung City) 43 (Chiayi City) 5,638 9,051
Nitrogen oxide emissions (NO ₂) (metric tons)	Maximum Minimum Average Standard deviation	76,826 (Kaohsiung City) 2,281 (Chiayi City) 20,213 19,626	74,061 (Kaohsiung City) 2,283 (Chiayi City) 20,321 19,228	 69,934 (Kaohsiung City) 2,101 (Chiayi City) 19,250 18,167 	65,068 (Kaohsiung City) 1,944 (Chiayi City) 18,120 16,922
<i>Carry over</i> Fixed assets (NT\$1,000)	Maximum Minimum Average Standard deviation	199,155,007 (Tainan City) 324,609 (Chiayi City) 56,753,880 66,919,221	199,637,849 (Taichung City) 264,800 (Taitung County) 55,750,421 68,137,797	213,953,949 (Tainan City) 773,560 (Taitung County) 62,653,275 75,504,497	232,090,820 (Taoyuan City) 903,929 (Taitung County) 65,734,355 74,984,091

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TABLE 2: Description of statistics.

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FIGURE 2: Description of statistics.

City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. The bottom three are Tainan City, Changhua County, and Yunlin County. The average efficiency in 2014 is 0.8199, with the most efficient being Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. The average efficiency in 2015 is 0.8370, with the most efficient being Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. The bottom three are Yunlin County, Changhua County, and Tainan City. In 2012, the average efficiency of 0.8360 is the highest. In 2013, the average efficiency is 0.7984, the average efficiency in 2014 is 0.8199, and the average efficiency in 2015 is 0.8370. The most efficient are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City; the worst are Tainan County, Changhua County, and Yunlin County.

3.3.2. Annual Input and Output Variable Efficiencies. From electricity consumption in Table 4, the four-year efficiency value of 1 covers Taipei City, Hsinchu County, Nantou County, Yunlin County, Chiayi County, Pingtung County, Taitung County, Hsinchu City, and Chiayi City.

TABLE 3: Overall efficiency of Taiwan's counties and cities from 2012 to 2015.

DMU	2012	2013	2014	2015	Average	Rank
New Taipei City	0.7134	0.7280	0.7331	0.7302	0.7261	13
Taipei City	1	1	1	1	1	1
Taoyuan City	0.8140	0.8134	0.8509	0.8482	0.8312	8
Taichung City	0.6937	0.7262	0.7393	0.7383	0.7239	14
Tainan City	0.6242	0.6579	0.6497	0.6649	0.6488	19
Kaohsiung City	0.6995	0.7155	0.7099	0.7206	0.7113	15
Yilan County	0.9381	0.7687	0.9077	0.9944	0.8940	7
Hsinchu County	0.9952	0.9048	0.9348	0.93	0.9401	6
Miaoli County	0.7982	0.7312	0.8411	0.7948	0.7893	9
Changhua County	0.7037	0.6566	0.6611	0.6671	0.6716	18
Nantou County	0.8736	0.7083	0.7808	0.7647	0.7775	11
Yunlin County	0.6761	0.6365	0.6824	0.7115	0.6756	17
Chiayi County	0.7870	0.6899	0.6712	0.7818	0.7287	12
Pingtung County	0.7424	0.6687	0.6764	0.7312	0.7032	16
Taitung County	1	1	1	1	1	1
Hualien County	0.8255	0.7640	0.7398	0.8251	0.7868	10
Keelung City	1	1	1	1	1	1
Hsinchu City	1	1	1	1	1	1
Chiayi City	1	1	1	1	1	1
Average value	0.8360	0.7984	0.8199	0.8370	0.8215	
Standard deviation	0.1347	0.1377	0.1363	0.1284	1	
Maximum	1	1	1	1	0.6488	
Minimum	0.6242	0.6365	0.6497	0.6649	0.1312	

TABLE 4: Electricity consumption efficiency of counties and cities inTaiwan from 2012 to 2015.

	Electricity co	onsumptior	ı	
DMU	2012	2013	2014	2015
New Taipei City	0.879	0.8759	0.8672	0.8676
Taipei City	1	1	1	1
Taoyuan City	0.4376	0.4312	0.4279	0.4312
Taichung City	0.5447	0.5229	0.5147	0.5093
Tainan City	0.4993	0.4856	0.4589	0.4463
Kaohsiung City	0.4741	0.469	0.4716	0.4791
Yilan County	0.7851	0.8123	0.7012	0.8878
Hsinchu County	1	1	1	1
Miaoli County	0.8566	0.9567	0.7435	0.8359
Changhua County	0.9485	1	0.9369	1
Nantou County	1	1	1	1
Yunlin County	1	1	1	1
Chiayi County	1	1	1	1
Pingtung County	1	1	1	1
Taitung County	1	1	1	1
Hualien County	0.5506	0.5268	0.508	0.5954
Keelung City	1	1	1	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.8408	0.8463	0.8226	0.8449
Standard deviation	0.2122	0.2207	0.2243	0.2183

Those with efficiency values below the four-year average of 0.8387 are Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Yilan County, and Hualien County. In 2012, there are 9 counties and cities that need to be adjusted. Among them, Taoyuan City, Kaohsiung City, and Tainan City need the greatest improvement, as their efficiency values are 0.4376, 0.4741, and 0.4376. The remaining 10 counties and cities have an efficiency value of 1 and do not

need to adjust. In 2013, there are 8 counties and cities that need to be adjusted. Among them, Taoyuan City, Kaohsiung City, and Tainan City need the greatest improvement, as their efficiency values are 0.4312, 0.4690, and 0.4586. The remaining 11 counties and cities have an efficiency value of 1. In 2014, there are 9 counties and cities that need to be adjusted. Among them, Taoyuan City, Kaohsiung City, and Tainan City need the greatest improvement, as their efficiency values are 0.4279, 0.4589, and 0.4716. The remaining 10 counties and cities have an efficiency value of 1. In 2015, there are 9 counties and cities that need to be adjusted. Among them, Taoyuan City, Kaohsiung City, and Tainan City need the greatest improvement, as their efficiency values are 0.4312, 0.4791, and 0.4463. The remaining 10 counties and cities have an efficiency value of 1.

From Table 5 on motor vehicles, the cities with a fouryear efficiency value of 1 are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Those with efficiency values below the four-year average of 0.8351 are New Taipei City, Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Changhua County, Yunlin County, Chiayi County, and Pingtung County. In 2012, there are 14 counties and cities with motor vehicles that need to be adjusted. Among them, New Taipei City, Kaohsiung City, and Pingtung County need the greatest improvement, as their efficiency values are 0.5610, 0.5963, and 0.6503. The remaining 5 counties and cities have an efficiency value of 1. In 2013, there are 14 counties and cities with motor vehicles that need to be adjusted. Among them, New Taipei City, Kaohsiung City, and Pingtung County need the greatest improvement, as their efficiency values are 0.5576, 0.6143, and 0.6587. The remaining 5 counties and cities have an efficiency value of 1. In 2014, there are 14 counties and cities with motor vehicles that need to be adjusted. Among them,

TABLE 5: Motor vehicle efficiency in counties and cities of Taiwanfrom 2012 to 2015.

	Motor	vehicle		
DMU	2012	2013	2014	2015
New Taipei City	0.5610	0.5576	0.5563	0.5535
Taipei City	1	1	1	1
Taoyuan City	0.7954	0.7811	0.7759	0.7609
Taichung City	0.6809	0.6755	0.6640	0.6542
Tainan City	0.6901	0.7083	0.6974	0.6949
Kaohsiung City	0.5963	0.6143	0.6156	0.6127
Yilan County	0.9602	0.9530	0.9365	0.9359
Hsinchu County	0.9584	0.9424	0.9330	0.9222
Miaoli County	0.8804	0.8748	0.8673	0.8708
Changhua County	0.7211	0.7271	0.7215	0.7187
Nantou County	0.8385	0.8425	0.8417	0.8426
Yunlin County	0.7965	0.8094	0.8045	0.8051
Chiayi County	0.8267	0.8368	0.8312	0.8342
Pingtung County	0.6503	0.6587	0.6652	0.6622
Taitung County	1	1	1	1
Hualien County	0.9281	0.9189	0.9424	0.9599
Keelung City	1	1	1	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.8360	0.8369	0.8343	0.8330
Standard deviation	0.1460	0.1421	0.1430	0.1454

New Taipei City, Kaohsiung City, and Taichung City need the greatest improvement, as their efficiency values are 0.5563, 0.6156, and 0.6640. The remaining 5 counties and cities have an efficiency value of 1. In 2015, there are 14 counties and cities with motor vehicles that need to be adjusted. Among them, New Taipei City, Kaohsiung City, and Taichung City need the greatest improvement, as their efficiency values are 0.5535, 0.6127, and 0.6542. The remaining 5 counties and cities have an efficiency value of 1.

From the average disposable income of Table 6, the cities with a four-year efficiency value of 1 are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Those with efficiency values below the four-year average of 0.8228 are New Taipei City, Taichung City, Tainan City, Kaohsiung City, Miaoli County, Changhua County, Nantou County, Yunlin County, Chiayi County, Pingtung County, and Hualien County. In 2012, there are 14 counties and cities that need to be adjusted. Among them, Taichung City, Kaohsiung City, and New Taipei City need the most improvement, as their efficiency values are 0.6937, 0.6995, and 0.7134. The remaining 5 counties and cities have an efficiency value of 1. In 2013, there are 14 counties and cities that need to be adjusted. Among them, Changhua County, Pingtung County, and Chiayi County need the most improvement, as their efficiency values are 0.6566, 0.6687, and 0.6899. The remaining 5 counties and cities have an efficiency value of 1. In 2014, there are 14 counties and cities that need to be adjusted. Among them, Tainan City, Changhua County, and Chiavi County need the most improvement, as their efficiency values are 0.6497, 0.6611, and 0.6712. The remaining 5 counties and cities have an efficiency value of 1. In 2015, there are 14 counties and cities that need to be adjusted. Among them, Tainan City, Changhua County, and Yunlin

Fable	6:	Average	e dis	sposable	income	efficiency	of	counties	and
cities i	nТ	Taiwan f	rom	2012 to	2015.				

	Average disp	osable inco	me	
DMU	2012	2013	2014	2015
New Taipei City	0.7134	0.728	0.7331	0.7302
Taipei City	1	1	1	1
Taoyuan City	0.814	0.8134	0.8509	0.8482
Taichung City	0.6937	0.7262	0.7393	0.7383
Tainan City	0.6242	0.6579	0.6497	0.6649
Kaohsiung City	0.6995	0.7155	0.7099	0.7206
Yilan County	0.9381	0.7687	0.9077	0.9944
Hsinchu County	0.9952	0.9048	0.9348	0.93
Miaoli County	0.7982	0.7312	0.8411	0.7948
Changhua County	0.7037	0.6566	0.6611	0.6671
Nantou County	0.8736	0.7083	0.7808	0.7647
Yunlin County	0.6761	0.6365	0.6824	0.7115
Chiayi County	0.787	0.6899	0.6712	0.7818
Pingtung County	0.7424	0.6687	0.6764	0.7312
Taitung County	1	1	1	1
Hualien County	0.8255	0.764	0.7398	0.8251
Keelung City	1	1	1	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.836	0.7984	0.8199	0.837
Standard deviation	0.1311	0.134	0.1327	0.125

County need the most improvement, as their efficiency values are 0.6649, 0.6671, and 0.7115. The remaining 5 counties and cities have an efficiency value of 1.

3.3.3. Annual PM_{2.5}, SO₂, and NO₂ Efficiencies. From Table 7 on $PM_{2.5}$, the cities with a four-year efficiency value of 1 are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Those with efficiency values below the fouryear average 0.4362 are Taipei City, Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Yilan County, Hsinchu County, Miaoli County, Changhua County, Nantou County, Yunlin County, Chiayi County, Pingtung County, and Hualien County. In 2012, there are 14 counties and cities that need to make adjustments for suspended particulate emissions. Hualien County, Kaohsiung City, and Yilan County need the greatest improvement, as their efficiency values are 0.0874, 0.1609, and 0.1969. The remaining 5 counties and cities have an efficiency value of 1. In 2013, there are 14 counties and cities that need to make adjustments for suspended particulate emissions. Hualien County, Kaohsiung City, and Yilan County need the greatest improvement, as their efficiency values are 0.0852, 0.1615, and 0.1644. The remaining 5 counties and cities have an efficiency value of 1. In 2014, there are 14 counties and cities that need to make adjustments for suspended particulate emissions. Hualien County, Kaohsiung City, and Yilan County need the greatest improvement, as their efficiency values are 0.0840, 0.1616, and 0.1673. The remaining 5 counties and cities have an efficiency value of 1. In 2015, there are 14 counties and cities that need to make adjustments for suspended particulate emissions. Hualien County, Kaohsiung City, and Yilan County need the greatest improvement, as their

TABLE 7: $PM_{2.5}$ emission efficiency in counties and cities of Taiwan from 2012 to 2015.

	PI	M _{2.5}		
DMU	2012	2013	2014	2015
New Taipei City	0.3001	0.2960	0.2970	0.2981
Taipei City	1	1	1	1
Taoyuan City	0.2493	0.2475	0.2535	0.2568
Taichung City	0.2111	0.1964	0.1981	0.2016
Tainan City	0.2585	0.2499	0.2504	0.2534
Kaohsiung City	0.1609	0.1615	0.1616	0.1635
Yilan County	0.1969	0.1644	0.1673	0.1671
Hsinchu County	0.4408	0.4068	0.4029	0.4078
Miaoli County	0.2752	0.2552	0.2526	0.2545
Changhua County	0.2788	0.2940	0.3004	0.3034
Nantou County	0.2243	0.2224	0.2214	0.2211
Yunlin County	0.2175	0.2028	0.2032	0.2068
Chiayi County	0.2818	0.2788	0.2785	0.2806
Pingtung County	0.1992	0.1803	0.1800	0.1800
Taitung County	1	1	1	1
Hualien County	0.0874	0.0852	0.0840	0.0829
Keelung City	1	1	1	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.4411	0.4337	0.4343	0.4357
Standard deviation	0.3405	0.3444	0.3441	0.3434

efficiency values are 0.0829, 0.1635, and 0.1671. The remaining 5 counties and cities have an efficiency value of 1.

From Table 8 on SO₂, the cities with a four-year efficiency value of 1 are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Those with efficiency values below the four-year average of 0.3288 are New Taipei City, Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Yilan County, Hsinchu County, Miaoli County, Changhua County, Nantou County, Yunlin County, Chiayi County, Pingtung County, and Hualien County. In 2012, 14 counties and cities need to make adjustments for sulfur oxide emissions. Hualien County, Yunlin County, and Taichung City need the greatest improvement, as their efficiency values are 0.0188, 0.0209, and 0.0207. The remaining 5 counties and cities have an efficiency value of 1. In 2013, 14 counties and cities need to make adjustments for sulfur oxide emissions. Kaohsiung City, Hualien County, and Yunlin County need the greatest improvement, as their efficiency values are 0.0108, 0.0125, and 0.0145. The remaining 5 counties and cities have an efficiency value of 1. In 2014, 14 counties and cities need to make adjustments for sulfur oxide emissions. Kaohsiung City, Hualien County, and Yunlin County need the greatest improvement, as their efficiency values are 0.0109, 0.0128, and 0.0144. The remaining 5 counties and cities have an efficiency value of 1. In 2015, 14 counties and cities need to make adjustments for sulfur oxide emissions. Kaohsiung City, Hualien County, and Yunlin County need the greatest improvement, as their efficiency values are 0.0112, 0.0131, and 0.0145. The remaining 5 counties and cities have an efficiency value of 1.

From Table 9 on NO_2 , the cities with a four-year efficiency value of 1 are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Those with efficiency

TABLE 8: SO_2 emission efficiency in counties and cities of Taiwan from 2012 to 2015.

	S	O ₂		
DMU	2012	2013	2014	2015
New Taipei City	0.1582	0.1034	0.1083	0.1070
Taipei City	1	1	1	1
Taoyuan City	0.0691	0.0512	0.0499	0.0487
Taichung City	0.0270	0.0174	0.0176	0.0179
Tainan City	0.1424	0.1029	0.1007	0.0990
Kaohsiung City	0.0152	0.0108	0.0109	0.0112
Yilan County	0.1061	0.0845	0.0836	0.0811
Hsinchu County	0.2572	0.2355	0.2234	0.2141
Miaoli County	0.1495	0.1469	0.1418	0.1385
Changhua County	0.1616	0.1238	0.1200	0.1170
Nantou County	0.3198	0.2534	0.2480	0.2452
Yunlin County	0.0209	0.0145	0.0144	0.0145
Chiayi County	0.0755	0.0505	0.0506	0.0509
Pingtung County	0.2748	0.2190	0.2150	0.2120
Taitung County	1	1	1	1
Hualien County	0.0188	0.0125	0.0128	0.0131
Keelung City	1	1	0.0010	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.3577	0.3382	0.2841	0.3353
Standard deviation	0.3927	0.4017	0.3765	0.4027

TABLE 9: NO_2 emission efficiency of counties and cities in Taiwan from 2012 to 2015.

	NC	D_2		
DMU	2012	2013	2014	2015
New Taipei City	0.3447	0.3223	0.3229	0.3280
Taipei City	1	1	1	1
Taoyuan City	0.2440	0.2026	0.1996	0.2018
Taichung City	0.1934	0.1663	0.1664	0.1721
Tainan City	0.4033	0.3424	0.3432	0.3508
Kaohsiung City	0.1483	0.1329	0.1324	0.1365
Yilan County	0.2522	0.2310	0.2213	0.2131
Hsinchu County	0.4329	0.4256	0.2981	0.4148
Miaoli County	0.2550	0.2330	0.2255	0.2228
Changhua County	0.0004	0.3497	0.3463	0.3502
Nantou County	0.5437	0.4853	0.4846	0.4895
Yunlin County	0.1582	0.1450	0.1383	0.1352
Chiayi County	0.3021	0.2584	0.2527	0.2521
Pingtung County	0.3970	0.3575	0.3545	0.3558
Taitung County	1	1	1	1
Hualien County	0.1322	0.1289	0.1225	0.1166
Keelung City	1	1	1	1
Hsinchu City	1	1	1	1
Chiayi City	1	1	1	1
Average value	0.4635	0.4622	0.4531	0.4600
Standard deviation	0.3419	0.3347	0.3383	0.3365

values below the four-year average 0.4597 are New Taipei City, Taoyuan City, Taichung City, Tainan City, Kaohsiung City, Yilan County, Hsinchu County, Miaoli County, Changhua County, Nantou County, Yunlin County, Chiayi County, Pingtung County, and Hualien County. In 2012, there are 14 counties and cities that need to make adjustments in NOx emissions. Hualien County, Kaohsiung City, and Yunlin County need the greatest improvement, as their

TABLE 10: O disposable in	verall score, electricity come efficiency analysi	consumption, motor v s.	ehicle emissions, su	spended particles emis	ssions, sulfur oxide emiss	sions, nitrogen oxide emissio	ons, and average household
DMU	Overall efficiency	Electricity consumption	Motor vehicles	Suspended particles	SOx	NOx	Average household distributable income
New Taipei City	Dropped from 11 th place in 2013 to 15 th place in 2015	Maintained 12 th or 13 th place	In last place all 4 years (19 th)	$7^{\rm th}$ in 2012 and 2013 and dropped to $8^{\rm th}$ place in 2014 and 2015	10 th in 2012 and 2014 and dropped to 11 th place in 2013 and 2015	10 th in 2012 and 2014 and dropped to 11 th place in 2013 and 2015	14 th in 2012, progressed to 11 th place in 2013, retired to 13 th place in 2014, and regressed to 15^{th} place in 2015
Taipei City	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1^{st} place in the 4 years	1^{st} place in the 4 years
Taoyuan City	Continued to improve slightly from 10 th in 2012 to 8 th in 2015	Last place in the 4 years (19 th place)	13 th place in the 4 years	12 th in 2012 and 2013 and progressed to 10 th place in 2014 and 2015	15 th in 2012 and 2015 and progressed to 14 th in 2013 and 2014	14 th in 2012 and regressed to 15 th place in 2013, 2014, and 2015	10^{th} place in 2012, progressed to 7^{th} place in 2013 and regressed to 8^{th} place in 2014 and 2015
Taichung City	Continued improving from 17 th in 2012 to 13 th in 2015	4 th in 2012, 2013, and 2015	$16^{\text{th}} \text{ in } 2012 \text{ and}$ $2013 \text{ and to } 17^{\text{th}}$ place in 2014 and 2015	15 th place in the 4 years	16 th in 2012, 2013, and 2015 and progressed to 15 th in 2014	15 th place in 2012, while 2013, 2014, and 2015 all regressed to 16 th place	17^{cn} in 2012 (3^{4c} last), progressed to 12^{th} place in 2013 and 2014, and regressed to 13^{th} place in 2015
Tainan City	Last place in 2012, 2014, and 2015	Third to last place in 2012, 2013, and 2014 and second to last in 2015	15 th in the 4 years	11 th in 2012 and 2013 and 12 th in 2014 and 2015	12 th in 2012, 2013, and 2015 and 11 th in 2014	<pre>8th place in 2012, 10th place in 2013, and 9th place in 2014 and 2015</pre>	Last (19 th place) in 2012, 2014, and 2015 and 17 th in 2013
Kaohsiung City	In 2013 it slipped from 13 th	Last in 2012, 2013, and 2014 and progressed to third from last in 2015	18^{th} in the 4 years	18^{th} in the 4 years	19 th in 2012, 2013 and 2015, progressing to 18 th place in 2014	17 th in 2012 and 2015 and 18 th place in 2013 and 2014	16 th in 2012 and 2015, 13 th in 2013, and 14 th in 2014
Yilan County	Average 6 th place.	14 th in 2012, 2013, and 2014, progressing to 12 th place in 2015	6^{th} in 2012 and 2013 and 7^{th} in 2014 and 2015	17 th place in the 4 years	13 th in 2012, 2013, and 2015 and to 12 th in 2014	13 th in 2012 and 14 th in 2013, 2014, and 2015	Average 7 th place
Hsinchu County	Average 7 th place	1 st place in the 4 years	7^{th} in 2012 and 2013 and 8^{th} in 2014 and 2015	6 th place in the 4 years	Average 7 th place	7 th place in 2012, 2013, and 2015 and 11 th place in 2014	$6^{\rm th}$ in 2012, 2013, and 2014 and $7^{\rm th}$ in 2015
Miaoli County	Continued improvement from 11 th in 2012 to 9 th in 2014	Average 13 th place	9 th place in the 4 years	10 th in 2012 and 2013 and 11 th in 2014 and 2015	$\begin{array}{l} 11^{\rm th} \mbox{ in 2012, progressed} \\ to 9^{\rm th} \mbox{ in 2013,} \\ progressed to 8^{\rm th} \mbox{ in 2014, and returned to} \\ 9^{\rm th} \mbox{ in 2015} \end{array}$	12 th in 2012, while 2013, 2014, and 2015 all regressed to 13 th	Average 10 th place
Changhua County	Second to last place in 2013, 2014, and 2015	1 st in 2013 and 2015, but 11 th in 2012 and 2014	14 th in the 4 years	9^{th} in 2012, progressed to 8^{th} in 2013, and progressed to 7^{th} in 2014 and 2015	9 th in 2012 and 2014, but regressed to 10 th in 2013 and 2015	Last place in 2012 (19^{th}), progressed to 9^{th} in 2013, progressed to 8^{th} in 2014, and backtracked to 10^{th} in 2015	15 th in 2012, while 2013, 2014, and 2015 all regressed to 18 th

DMU	Overall efficiency	Electricity consumption	Motor vehicles	Suspended particles	SOx	NOx	Average household distributable income
Nantou County	11 th on average	1 st place in the 4 years	10 th in the 4 years	13 th in the 4 years	6 th in 2012, 2013, and 2015 and progressed to 5 th in 2014	6 th in the 4 years	11 th on average
Yunlin County	17 th on average	1 st place in the 4 years	12 th in the 4 years	14 th in the 4 years	17 th in 2012, 2013, and 2015 and progressed to 16 th in 2014	16 th in 2012, 17 th in 2013 and 2014, and 18 th in 2015	18 th in 2012, retraced to 19 th (last) in 2013, progressed to 15^{th} in 2014, and regressed to 17^{th} in 2015,
Chiayi County	12 th on average	1 st place in the 4 years	11 th in 4 years	11 th place in 2012 and 9 th in 2013, 2014, and 2015	14 th on average	11 th in 2012 and 12 th in 2013, 2014, and 2015	12^{th} in 2012, 15^{th} in 2013, 17^{th} in 2014, and 11^{th} in 2015
Pingtung County	16 th on average	1 st place in the 4 years	17 th in 2012 and 2013 and 16 th in 2014 and 2015	16 th place in the 4 years	7 th in 2012 and 2014 and regressed to 8 th in 2013 and 2015	8 th on average	$13^{\rm th}$ in 2012, $16^{\rm th}$ in 2013 and 2014, and $14^{\rm th}$ in 2015
Taitung County	1 st place in the 4 years	$1^{ m st}$ place in the 4 years	1^{st} place in the 4	1 st place in the 4	1 st place in the 4	1 st place in the 4	1 st place in the 4
Hualien County	10 th on average	15 th in 2012, 2013, and 2014	8 th in 2012 and 2013 and progressed to 6 th in 2014 and 2015	Last place in the 4 years (19 th)	18 th place in 2012, 2013, and 2015 and 17 th place in 2014	18 th in 2012 and 19 th in 2013, 2014, and 2015	9 th in 2012, 2013, and 2015 and 11 th in 2014
Keelung City	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1^{st} place in 2012, 2013, and 2015, but regressed to 19^{th} (last) in 2014	1 st place in the 4 years	1 st place in the 4 years
Hsinchu City	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1 st place in the 4 years
Chiayi City	1 st place in the 4 years	$1^{\rm st}$ place in the 4 years	1 st place in the 4 years	1 st place in the 4 years	1^{st} place in the 4 years	1^{st} place in the 4 years	1 st place in the 4 years

Continued.	
10:	
TABLE	

efficiency values are 0.1322, 0.1483, and 0.1582. The remaining 5 counties and cities have an efficiency value of 1. In 2013, there are 14 counties and cities that need to make adjustments in NOx emissions. Hualien County, Kaohsiung City, and Yunlin County need the greatest improvement, as their efficiency values are 0.1289, 0.1329, and 0.1450. The remaining 5 counties and cities have an efficiency value of 1. In 2014, there are 14 counties and cities that need to make adjustments in NOx emissions. Hualien County, Kaohsiung City, and Yunlin County need the greatest improvement, as their efficiency values are 0.1225, 0.1324, and 0.2213. The remaining 5 counties and cities have an efficiency value of 1. In 2015, there are 14 counties and cities that need to make adjustments in NOx emissions. Hualien County, Yunlin County, and Kaohsiung City need the greatest improvement, as their efficiency values are 0.1166, 0.1352, and 0.1365. The remaining 5 counties and cities have an efficiency value of 1.

In order to further understand the counties' and cities' electricity consumption, motor vehicles, aerosol emissions, sulfur oxide emissions, nitrogen oxide emissions, and average disposable income per household, this research offers Table 10 for illustration. From Table 10, Taipei City, Taitung County, Hsinchu City, Chiayi City, and Keelung City maintain the highest efficiency values in the 4 years, regardless of overall score, electricity consumption, motor vehicles, fine aerosol emissions, nitrogen oxide emissions, and average per efficiency analysis of household disposable income. From the efficiency analysis of sulfur oxide emissions, Taipei City, Taitung County, Hsinchu City, and Chiayi City still rank first in 4 years. Keelung City also maintains first place in 2012, 2013, and 2015, but in 2014, it ranks 19th (last). In 2014, the Keelung Port Art Exhibition attracted a large number of people from other counties and cities, and the air pollution was serious.

The 19th overall score (last place) is Tainan City. The electricity efficiency value of Tainan City is also in second to last place or third from last place. Its value for motor vehicle efficiency remains in 15th place in the 4 years (5th from last). For its efficiencies of suspended particulate emissions and sulfur oxide emissions, it maintains 11th or 12th place in the 4 years. The average efficiency of each household's disposable income is last place in 2012, 2014, and 2015 (19th place). In 2013, it improves slightly to 17th (third from last place).

Among the six municipalities, only Taipei City and Taoyuan City rank first and eighth. The remaining 4 municipalities have poor overall scores. In last place (19th) is Tainan City, 15th is Kaohsiung City, 14th is Taichung City, and 13th is New Taipei City.

Among the 13 nonmunicipalities with low overall scores, 18th is Changhua County (second lowest), 17th is Yunlin County (third lowest), 16th is Pingtung County, and 12th is Chiayi County. For nonmunicipalities with middle overall scores, 6th is Hsinchu County, 7th is Yilan County, 9th is Miaoli County, 10th is Hualien County, and 11th is Nantou County.

For the efficiency of electricity consumption, in last place is Taoyuan City for all 4 years. For the efficiency of motor vehicles, in last place is New Taipei City and in 18th is Kaohsiung City for the 4 years (second to last place). For the efficiency of suspended matter emissions, in last place is Hualien County, in 18th is Kaohsiung City (second lowest), in 17th is Yilan County (third from last), and Pingtung County is in 16th place in the 4 years. The undesirable output and desirable output of each county and city have different degrees of progress or regression in the 4 years.

We note that Taipei City, Taitung County, Hsinchu City, Chiayi City, and Keelung City have the best performances. The rest of the counties and cities have a lot of room for improvement. Taiwan's local governments thus should formulate strong policy interventions in air pollution.

4. Conclusions

During the current situation of global warming and deteriorating environmental conditions, countries around the world are thinking about how to balance economic growth, reduce environmental pollution, and move forward in the direction of sustainable development. Therefore, this article collects data from 19 counties and cities in Taiwan from 2012 to 2015, using the modified dynamic SBM model to explore the change in efficiency of air pollutants in various regions of the country from the economic perspective. The results are as follows:

- (1) From 2012 to 2015, the counties with the best overall efficiency performance are Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City. Their average overall efficiency value is 1. The average overall efficiency performances are poor in Tainan City, Changhua County, Yunlin County, Pingtung County, and Kaohsiung City, with efficiency values of 0.6488, 0.6716, 0.6756, 0.7032, and 0.7113. In counties and cities with the best overall performance and poor performance, the average disposable income per household has no significant relationship with air pollutant emissions.
- (2) In the counties and cities with better overall efficiency from 2012 to 2015, the efficiency values of motor vehicles, average household disposable income, and three air pollutant emissions are all 1. Counties and cities with poor performance have large room for improvement in average disposable income per household.
- (3) Regarding the undesirable output of suspended particulate emissions, sulfur oxide emissions, and nitrogen oxide emissions, the efficiency values of Taipei City, Taitung County, Keelung City, Hsinchu City, and Chiayi City are all 1. The efficiency values of the three air pollutants in the remaining 14 counties and cities are far below 0.5, indicating that the air pollution situation there is in urgent need of improvement.
- (4) The five counties and cities with the lowest electricity consumption efficiency are Taoyuan City, Kaohsiung City, Tainan City, Taichung City, and Hualien County. The cement industry, mining industry, and tourism industry are concentrated in Hualien

County and need to improve their efficiency. Due to the high demand for industrial electricity, Taoyuan City accounts for more than half of all electricity in Taiwan. The authority must increase the utilization rate of energy use.

Compared with advanced countries, Taiwan has fallen far behind in air pollution control. The prevention of air pollution still only focuses on propaganda and should change to enforcement as soon as possible. More detailed regulations of pollution reduction in different industries are also necessary. This study has pointed out that the efficiency values of the three air pollutants in fourteen counties and cities are far below 0.5. Among the six municipalities directly under the central government with relatively high financial autonomy, only Taipei City and Taoyuan City have higher overall scores. The remaining 4 municipalities of Tainan City, Kaohsiung City, Taichung City, and New Taipei City have poor overall scores. Taiwan must pay attention to the future adjustment of its energy structure such as the use of coal and petrochemical energy and renewable energy development policies. Lastly, Taiwan should face the problem of air pollution without dividing the political parties in order to achieve a steady economy and sustainable development for all involved.

By above results, this research provides the following policy recommendation:

- (1) Air pollutants move with air flow; thus, the issue of air pollution should be jointly treated with surrounding countries
- (2) Local governments reduce coal use to generate electricity to reduce air pollution
- (3) Public sector and private sector should replace petrochemical energy with renewable energy to reduce air pollution
- (4) The government encourages the public sector and the private sector to use electric vehicles to reduce air pollutant emission by vehicle

Data Availability

The data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that there are no conflicts of interest.

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