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 $\alpha = 1.383;$ 
 $\beta = 3;$ 
 $n = 10\,000;$ 
 $k = 3;$ 
 $t = 0.7;$ 
 $a = 2;$ 
 $b = 1;$ 
 $c = 0.5;$ 
 $z = 3;$ 
 $s1 = 0;$ 
 $s2 = 0;$ 
 $s3 = 0;$ 
 $s4 = 0;$ 
 $s5 = 0;$ 
 $s6 = 0;$ 
 $s7 = 0;$ 
 $s8 = 0;$ 
 $s9 = 0;$ 
 $s10 = 0;$ 
 $s11 = 0;$ 
 $s12 = 0;$ 
 $s13 = 0;$ 
 $s14 = 0;$ 
 $s15 = 0;$ 
 $s16 = 0;$ 
 $s17 = 0;$ 
 $s18 = 0;$ 
 $s19 = 0;$ 
 $s20 = 0;$ 
 $w = 0.2;$ 

IT = 10 000;
R = 1 - Exp[- $\alpha * t^{-\beta}$ ];
For[i = 1, i ≤ IT, i++,
  x = Table[ $\left(-\frac{1}{\alpha} \log[\text{Random}[]]\right)^{-\frac{1}{\beta}}$ , {n}];
  maxima[x_] := Union[Rest[FoldList[Min, x[[1]], x]]];
  tt = maxima[x];
  g = Length[tt];
  ttt = Sort[tt, Greater];
  If[g ≥ k, d = ttt[[k]], d = Min[{ttt}]];
  V = b + d $^{-\beta}$ ;
  αmL = k * d $^{\beta}$ ;
  s1 += (αmL - α) $^2$ ;
  αSE =  $\frac{a+k}{V}$ ;
  s2 += (αSE - α) $^2$ ;
  αLinex =  $\frac{k+a}{c} \log\left(\frac{c+V}{V}\right)$ ; s3 += (αLinex - α) $^2$ ;
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I1 =  $\left( \frac{z+v}{v} \right) ^{-k-a};$ 
I2 =  $\left( \frac{(c+z)+v}{v} \right) ^{-k-a};$ 
 $\alpha wLinex = \frac{1}{c} \text{Log} \left[ \left( \frac{\left( \frac{z+v}{v} \right) ^{-k-a}}{\left( \frac{(c+z)+v}{v} \right) ^{-k-a}} \right) \right]; s4 += (\alpha wLinex - \alpha)^2;$ 
mle1 =
Minimize[{{(\alpha mL * h1 + \alpha SE * h2 - \alpha)^2, h1 + h2 == 1, 0 < h1 < 1, 0 < h2 < 1}, {h1, h2}}];
d1 = mle1[[1]]; dr1 = h1 /. mle1[[2, 1]];
dr2 = h2 /. mle1[[2, 2]]; \alpha seLP = \alpha mL * dr1 + \alpha SE * dr2;
s5 += (\alpha seLP - \alpha)^2;
mle2 = Minimize[{{\left( -\frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * h3 + h4 * \left( 1 + \frac{c}{v} \right) ^{-a-k} \right] \right) - \alpha}^2,
h3 + h4 == 1, 0 < h3 < 1, 0 < h4 < 1}, {h3, h4}];
d2 = mle2[[1]]; dr3 = h3 /. mle2[[2, 1]];
dr4 = h4 /. mle2[[2, 2]];
 $\alpha LinexLP = -\frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * dr3 + dr4 * \left( 1 + \frac{c}{v} \right) ^{-a-k} \right];$ 
s6 += (\alpha LinexLP - \alpha)^2;

mle3 = Minimize[{{\left( \frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * h5 + h6 * \left( \frac{\left( 1 + \frac{z}{v} \right) ^{-a-k}}{\left( 1 + \frac{z+c}{v} \right) ^{-a-k}} \right) \right] \right) - \alpha}^2,
h5 + h6 == 1, 0 < h5 < 1, 0 < h6 < 1}, {h5, h6}];
d3 = mle3[[1]]; dr5 = h5 /. mle3[[2, 1]];
dr6 = h6 /. mle3[[2, 2]];
 $\alpha WLInexLP = \frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * dr5 + dr6 * \left( \frac{\left( 1 + \frac{z}{v} \right) ^{-a-k}}{\left( 1 + \frac{z+c}{v} \right) ^{-a-k}} \right) \right];$ 
s7 += (\alpha WLInexLP - \alpha)^2;
\alpha seW = \alpha mL * w + \alpha SE * (1-w);
s8 += (\alpha seW - \alpha)^2;
 $\alpha INEXW = -\frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * w + (1-w) * \left( 1 + \frac{c}{v} \right) ^{-a-k} \right];$ 
s9 += (\alpha INEXW - \alpha)^2;
 $\alpha WINEXW = \frac{1}{c} \text{Log} \left[ (\text{Exp}[-\alpha mL * c]) * w + (1-w) * \left( \frac{\left( \frac{z+v}{v} \right) ^{-k-a}}{\left( \frac{(c+z)+v}{v} \right) ^{-k-a}} \right) \right];$ 
s10 += (\alpha WINEXW - \alpha)^2;

RML = 1 - \text{Exp}[-\alpha mL * t^{-\beta}]; s11 += (RML - R)^2;

RSE = 1 -  $\left( \frac{v}{v + t^{-\beta}} \right) ^{a+k}; s12 += (RSE - R)^2;$ 
f = Log[E^{-c} + E^{-c} * v^{a+k} * Sum[(c)^i / Gamma[i+1], {i, 1, Infinity}]];

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Rlinex =  $\frac{-1}{c} * f;$ 
s13 += (Rlinex - R)^2;
RWINEX =
 $\frac{1}{c} * \text{Log}\left[\left(\frac{(z)^i}{\text{Gamma}[i+1]} (V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right)\right] /$ 
 $\left(\frac{(c+z)^i}{\text{Gamma}[i+1]} (V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right)$ 
];
s14 += (RWINEX - R)^2;
mle4 =
Minimize[{\{(RML * h7 + RSE * h8 - R)^2, h7 + h8 == 1, 0 < h7 < 1, 0 < h8 < 1\}, {h7, h8}};
d4 = mle4[[1]]; dr7 = h7 /. mle4[[2, 1]];
dr8 = h8 /. mle4[[2, 2]]; RSELP = RML * dr7 + RSE * dr8;
s15 += (RSELP - R)^2;

mle5 =
Minimize[{\left(\left(-\frac{1}{c} \text{Log}\left[\left(\text{Exp}[-RML * c] * h9 + h10 * E^{-c} + E^{-c} * V^i * (a+k) * \text{Sum}\left[\frac{(c)^i}{\text{Gamma}[i+1]}
 $(V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right]\right]\right)^2 - R\right)^2,
h9 + h10 == 1, 0 < h9 < 1, 0 < h10 < 1\}, {h9, h10}];
d5 = mle5[[1]]; dr9 = h9 /. mle5[[2, 1]];
dr10 = h10 /. mle5[[2, 2]];

RLinexLP = - $\frac{1}{c} \text{Log}\left[\left(\text{Exp}[-RML * c] * dr9 + dr10 * E^{-c} + E^{-c} * V^i * (a+k) * \text{Sum}\left[\frac{(c)^i}{\text{Gamma}[i+1]} (V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right]\right)\right]$ ;
s16 += (RLinexLP - R)^2;

mle6 = Minimize[
{\left(\left(\frac{1}{c} \text{Log}\left[\left(\text{Exp}[-RML * c] * h11 + h12 * \left(\left(\frac{(z)^i}{\text{Gamma}[i+1]} (V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right)\right) / \left(\frac{(c+z)^i}{\text{Gamma}[i+1]} (V + i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\}\right)\right]\right) - R\right)^2,
h11 + h12 == 1, 0 < h11 < 1, 0 < h12 < 1\}, {h11, h12}]];
d6 = mle6[[1]]; dr11 = h11 /. mle6[[2, 1]];
dr12 = h12 /. mle6[[2, 2]];

RWLinexLP =  $\frac{1}{c} \text{Log}\left[\left(\text{Exp}[-RML * c] * dr11 + dr12 * \right.\right.$$ 
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$$\left( \left( E^{-z} + E^{-z} * V^a * (a+k) * \text{Sum} \left[ \frac{(z)^i}{\text{Gamma}[i+1]} (V+i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\} \right] \right) / \left( E^{-(c+z)} + E^{-(c+z)} * V^a * (a+k) * \text{Sum} \left[ \frac{(c+z)^i}{\text{Gamma}[i+1]} (V+i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\} \right] \right) \right) ];$$

s17 += (RWLinexLP - R)^2;

RseW = RML * w + RSE * (1 - w);
s18 += (RseW - R)^2;
RLIenxw = -  $\frac{1}{c} \text{Log} \left[ (\text{Exp}[-RML * c]) * w + (1-w) * E^{-c} + E^{-c} * V^a * (a+k) * \text{Sum} \left[ \frac{(c)^i}{\text{Gamma}[i+1]} (V+i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\} \right] \right]$ ;
s19 += (RLIenxw - R)^2;

RWLinexLPw =  $\frac{1}{c} \text{Log} \left[ (\text{Exp}[-RML * c]) * w + (1-w) * \left( \left( E^{-z} + E^{-z} * V^a * (a+k) * \text{Sum} \left[ \frac{(z)^i}{\text{Gamma}[i+1]} (V+i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\} \right] \right) / \left( E^{-(c+z)} + E^{-(c+z)} * V^a * (a+k) * \text{Sum} \left[ \frac{(c+z)^i}{\text{Gamma}[i+1]} (V+i t^{-\beta})^{-k-a}, \{i, 1, \text{Infinity}\} \right] \right) \right) \right] ;$ 
s20 += (RWLinexLPw - R)^2;

Print["k =", k];
Print["c =", c];
Print["w =", w];
Print["z =", z];
Print["α ml =", s1 / IT];
Print["α se =", s2 / IT];
Print["α linex =", s3 / IT];
Print["α wlinex =", s4 / IT];
Print["α selp=", s5 / IT];
Print["α LINUXlp=", s6 / IT];
Print["α wLINUXlp=", s7 / IT];
Print["α sew=", s8 / IT];
Print["α linex w=", s9 / IT];
Print["α wlinex w=", s10 / IT];

Print["reliability =", reliability];
Print["R ml =", s11 / IT];
Print["R se =", s12 / IT];
Print["R linex =", s13 / IT];
Print["R wlinex =", s14 / IT];
Print["R selp=", s15 / IT];
Print["R LINUXlp=", s16 / IT];
Print["R wLINUXlp=", s17 / IT];

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Print[" R sew=", s18 / IT];
Print[" R linewidth=", s19 / IT];
Print[" R wlinex w=", s20 / IT];
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