

Research Article

Fatigue Properties of Plain Concrete under Triaxial Tension-Compression-Compression Cyclic Loading

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Fatigue tests were performed on plain concrete under triaxial tension-compression-compression (T-C-C) cyclic loading with constant and variable amplitude using a large multiaxial machine. Experimental results show that, under constant amplitude fatigue loads, the development of residual strain in the fatigue loading direction depends mostly on the lateral compressive stress ratio and is nearly independent of stress level. Under variable amplitude fatigue loads, the fatigue residual strain is related to the relative fatigue cycle and lateral compressive stress ratio but has little relationship with the loading process. To model this system, the relative residual strain was defined as the damage variant. Damage evolutions for plain concrete were established. In addition, fatigue damage analysis and predictions of fatigue remaining life were conducted. This work provides a reference for multistage fatigue testing and fatigue damage evaluation of plain concrete under multiaxial loads.

1. Introduction

In practice, many concrete structures such as offshore platforms, nuclear reactor pressure containers, and bridges are subjected to repeated loading amplitudes in complex multiaxial stress states during normal use. Thus, it is important to understand fatigue damage accumulation in concrete under multiaxial variable amplitude stresses and various stress ratios. In the last few decades, many researches have been carried out to study the fatigue properties of plain concrete (PC) under uniaxial and multiaxial compressive loads. Because the development of multiaxial fatigue test system technology is difficult and with high cost and several key technical problems exist in the experiment, to date, a few works have been dedicated to investigating multiaxial tension and compression fatigue properties. Park et al. [1] used thin fire-damaged concrete discs to evaluate tensile strength and found that the tensile strength could be effectively estimated from the HNP without consideration of the

mix proportion. He et al. [2, 3] focused on the multiaxial mechanical properties of plain recycled aggregate concrete (RAC) and found that the ratio of triaxial fatigue strength to the corresponding uniaxial compressive strength for the three strength grades of RAC was higher than that of conventional concrete. Mun et al. [4] examined the fatigue stress-strain response of different concrete mixtures under compressive cyclic loadings with maximum and minimum stress levels. Shi et al. [5] reported that the tensile strength and secant modulus of large aggregate concrete under triaxial T-C-C increase with the increase of strain rate but decrease with the increase of lateral compressive stress. Subramaniam et al. [6] studied the fatigue behavior of concrete subjected to combined stresses in the T-C region of the biaxial stress space and found that the decrease in rotational stiffness at failure for the constant amplitude fatigue loading was comparable to the corresponding load in the postpeak part of the quasistatic response. Shiming and Yupu [7] studied on biaxial T-C strength and found that tensile compressive strength

increases with the increase of strain rate when the lateral tensile stress is constant and the tensile compressive strength decreases with the increase of lateral tensile stress. Yan et al. [8] tested the dynamic properties of concrete materials under both high strain rates and triaxial stress states. It was pointed out that the strain rate effects on maximum strength under triaxial stress states decrease with an increase in confining stress. Only Yang et al. [9] investigated the fatigue properties of concrete in tension under single and bilateral pressure of variable amplitude, determining fatigue life and residual strain. Based on the cyclic stress-strain curve, fatigue deformation modulus was defined. Accordingly, a damage model was established through the relationship between the ratios of fatigue deformation modulus and the number of cycles. Above all, we can see that the researches on plain concrete for fatigue properties under triaxial T-C-C loading are rare, so it has a realistic significance for us.

Fatigue cumulative damage is one of the main concerns when using PC, and the P-M linear fatigue cumulative damage criterion is still the most widely used model. On this basis, most studies have included research on the linear damage of PC. Studies have validated and discussed the damage variant $D = \sum(n_i/N_i)$. Subramaniam et al. [6] recommended that damage in concrete subjected to biaxial fatigue loading in the T-C region through torsion is localized, the damage localizes to a single crack, and the observed overall response is governed by crack growth. The load-deformation response obtained from quasistatic loading acts as the envelope failure curve for fatigue loading considering decrease in rotational stiffness. Peiyin et al. [10] discussed the laws and characteristics of fatigue residual strain, defined the damage variable, and carried out damage accumulation and evolution rules. In addition, a model of fatigue damage was established and verified using experimental results. These investigations focused on the nonlinear cumulative fatigue damage to concrete. The fatigue damage evolution equations were defined using other parameters such as strain, strength, and elastic modulus as part of the damage variant. Chen et al. [11] reported the effects of stress state on the dynamic compressive strength and the dynamic damage evolution process of concrete using a split Hopkinson pressure bar and ultrasonic technique. Results showed that dynamic damage evolutions are accelerated with an increase in strain rate and are delayed significantly under confined pressure. Byung [12] introduced the cumulative damage theory of concrete under variable amplitude fatigue loading condition. Yang et al. [9] investigated the properties of concrete in tension under single and bilateral pressure of variable amplitude fatigue, working out fatigue life and residual strain. Based on the cyclic stress-strain curve, fatigue deformation modulus was defined. Accordingly, a damage model was established through the relationship between the ratios of fatigue deformation modulus and the number of cycles. Cao et al. [13] considered more than the fatigue residual strain of concrete when determining the damage variant. Steady deformations and smaller discreteness at the ultimate residual strain were observed when considering residual strain on the concrete fatigue loading direction. Thus, the unrecoverable degree of microplastic deformation and microcracks can be

determined. This model better reflects the properties of the material than the method of maximum strain for concrete in the fatigue loading direction.

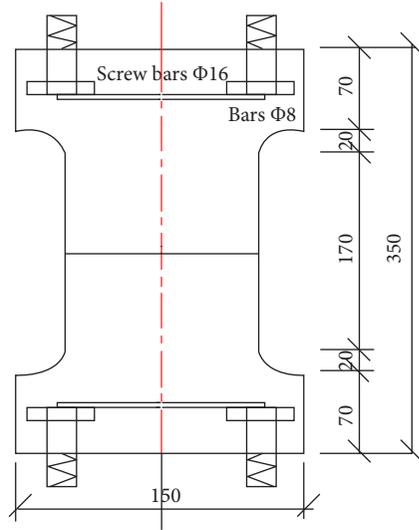
Testing of the triaxial T-C-C fatigue properties was performed using a triaxial testing machine capable of developing three independent compressive or tensile forces at Dalian University of Technology. Fatigue residual strain was recorded during both constant and varying amplitude fatigue processes. The relative residual strain was defined as the damage variant, updates were proposed to the corresponding fatigue damage equation, and the multistage fatigue damage model under triaxial T-C-C loading was established. This work provides a reference for multistage fatigue testing and fatigue damage evaluation of concrete under multiaxial loads.

2. Materials and Experimental Procedures

2.1. Casting and Curing of Specimens. The constituent proportions within the mix used experimentally were cement : sand : stone : water = 383 : 663 : 1154 : 193 (kg/m³). During testing, the ends of the specimen bulk and the testing machine load head were connected by tightening nuts. This transmitted the tensile strength of the machine through the screw, which was then passed to the specimen in order to test volatility in tension fatigue loading. Specimens were created by casting in wooden molds and compacted slightly by a vibrating table. After 24 hours, specimens were removed from molds and then cured at 20 ± 3°C and 95% relative humidity for 28 days covered with grass. Specimens were tested 90 days after cure by the test method of Chinese standard GB/T 17671-1999 [14].

Variable cross-section prism specimens were used for testing based on experimental requirements, fatigue performance, specimen installation, and references available at home and abroad. As shown in Figure 1, lateral pressure can be applied to two pairs of sides when testing a prism shaped specimen. The specimens tested measured 150 mm × 150 mm × 350 mm. In order to reduce stress concentrations, both ends of the specimen were embedded with four Φ16 steel screws, and the end of the screw was embedded within the specimen by Φ8 steel welded connections. The same batch of concrete was used to create six or more 150 mm × 150 mm × 150 mm standard cubes, which were used to measure the strength for multiaxial tests and determine strength class [15].

2.2. Testing Load Patterns. Fatigue tests were performed on plain concrete subjected to constant and variable amplitude triaxial T-C-C cyclic loading, and the lateral pressure stresses S_{\max} are 0.25 f_t and 0.50 f_t . S is the stress level of fatigue, $S_{\max} = \sigma_{\max}/f_t$, $S_{\min} = \sigma_{\min}/f_t = 0.10$, and f_t is the uniaxial tensile strength of 150 mm × 150 mm × 300 mm prism. Constant amplitude fatigue of maximum stress was varied from 0.25 f_t to 0.75 f_t , and variable amplitude fatigue procedures included tests with two and three stages. The loading mode is shown in Figure 2, where loading frequency was 5 Hz. Cyclic loading was applied using a sine wave waveform and the minimum stress level. Load patterns are shown in Table 1.



(a) Specimen size and shape



(b) The large-scale static and dynamic multiaxial testing machine



(c) Specimens under multiaxial loads

FIGURE 1: Machine and specimen.

TABLE 1: Test results for constant-amplitude cyclic loading.

Lateral stress ratio		S_{\max}	Fatigue life					
σ_2/f_c	σ_3/f_c		N_f			\bar{N}_f		
0.25	0.25	0.75	210	121	89	75	43	108
		0.65	16188	8903	5117	1547	369	6425
		0.55	950477	783912	361760	137334	32729	453242
0.25	0.50	0.60	171	102	72	46	21	82
		0.50	20387	9753	7415	1110	336	7800
		0.40	1453275	1150119	785733			1129709
0.50	0.50	0.45	1276	871	625	389	207	674
		0.35	348663	150744	98146	51405	17592	133310
		0.25						

Note. \bar{N}_f is the average fatigue life.

2.3. Testing Methods. Deformation of the specimen was recorded within a range of ± 5 mm using displacement sensors. Three layers of plastic membrane with Mobil lubricants were placed between the compressive loading plate and the specimen as friction-reducing pads [2, 3]. After the specimen was placed in the appropriate position, first execute visual

alignment and preload 10 kN static load in the vertical direction. Moreover, a larger static load was applied on specimens to complete the horizontal direction centering controlling. Then, preload the same proportion more than three times repeatedly in three directions, so that specimen with the loading plate contact surface compaction and load

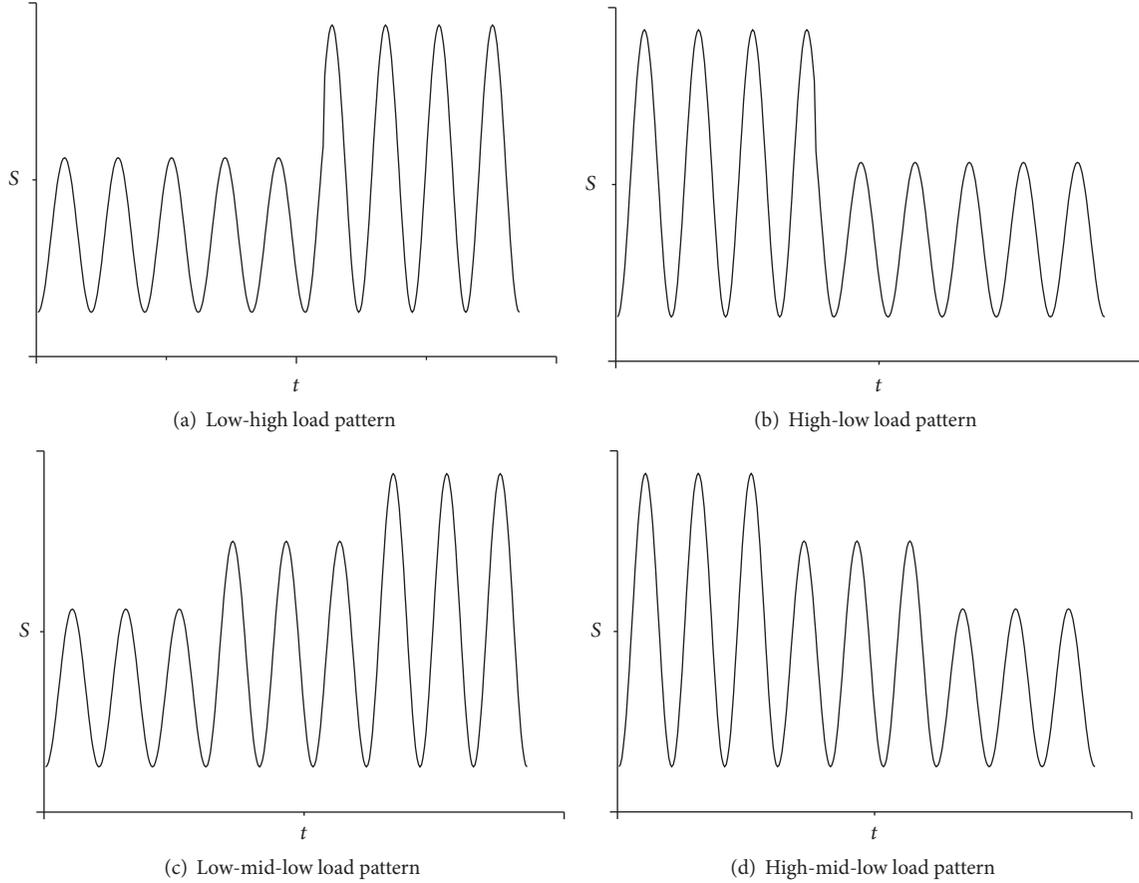


FIGURE 2: Load patterns of variable amplitude multistage fatigue tests.

can be appropriately increased to 20~30 kN. Complete the specimen in the geometric centering controlling and fix it with moderate force, gradually tightening evenly eight screws at the upper and lower edges of the specimen. Finally, use a small hammer to tap specimen or load head, through the rotation of globe hinge to adjust mechanical alignment of specimen [16].

3. Test Results and Discussions

3.1. Fatigue Life. Fatigue life was measured on plain concrete and results are shown in Tables 1 and 2. A large number of studies have shown that the fatigue strength of concrete is usually attributed to the establishment of $S-N$ curve equation (also known as Wöhler equation). The $S-N$ curve quantitatively describes the relationship between stress level S and fatigue life N , and the mathematical expression is

$$S_{\max} = A - B \lg N, \quad (1a)$$

where A and B are coefficients. And fatigue $S-N$ equations under T-C-C constant amplitude loading at various lateral

pressures were analyzed using the linear regression method proposed below:

$$S_{\max} = -0.0519 \lg N + 0.8388 \quad \left(\frac{\sigma_2}{f_c} = 0.25; \frac{\sigma_3}{f_c} = 0.25 \right), \quad (1b)$$

$$S_{\max} = -0.0427 \lg N + 0.6642 \quad \left(\frac{\sigma_2}{f_c} = 0.25; \frac{\sigma_3}{f_c} = 0.50 \right), \quad (1c)$$

$$S_{\max} = -0.0412 \lg N + 0.5582 \quad \left(\frac{\sigma_2}{f_c} = 0.50; \frac{\sigma_3}{f_c} = 0.50 \right), \quad (1d)$$

where S_{\max} is the maximum stress level of fatigue, N is fatigue life, f_c is uniaxial compressive strength of a concrete prism, σ_1 is the cyclic tensile stress, σ_2 and σ_3 are lateral compressive stresses, $\sigma_3 < \sigma_2 < \sigma_1$, and the compressive stress is negative but tensile stress is positive. The correlation coefficients R^2 of the above equations are 0.945, 0.965, and 0.948, respectively. Figure 3 shows the corresponding $S-N$ scattergram.

TABLE 2: Test data of fatigue for variable amplitude.

Specimen number	Fatigue life		D	ϵ_0 $\mu\epsilon$	Specimen number	Fatigue life			D	ϵ_0 $\mu\epsilon$
	n_1	n_2				n_1	n_2	n_3		
25250101	52203	24	0.45	215	25250301	52203	1004	121	1.79	255
25250102	52203	308	3.48	234	25250302	52203	1004	75	1.30	248
25250103	52203	272	3.09	238	25250303	52203	1004	13	0.64	192
25250104	52203	43	0.66	247	25250304	52203	1004	360	4.33	244
25250105	52203	640	7.01	204	25250305	52203	1004	29	0.81	232
25250201	19	816980	3.33	217	25250401	19	1004	1498232	6.24	234
25250202	19	185321	0.91	213	25250402	19	1004	300168	1.65	229
25250203	19	114847	0.64	225	25250403	19	1004	70474	0.77	203
25250204	19	91356	0.55	199	25250404	19	1004	49593	0.69	237
25250205	19	1934129	7.61	243	25250405	19	1004	109627	0.92	226
25500101	304705	110	1.86	327	25500301	304705	1060	67	1.52	308
25500102	304705	17	0.45	319	25500302	304705	1060	315	5.27	314
25500103	304705	43	0.85	313	25500303	304705	1060	16	0.74	301
25500104	304705	233	3.73	306	25500304	304705	1060	32	0.99	335
25500105	304705	59	1.09	286	25500305	304705	1060	143	2.67	327
25500201	13	2559519	1.88	310	25500401	13	1060	594174	0.89	334
25500202	13	700821	0.66	302	25500402	13	1060	1218818	130	305
25500203	13	594174	0.59	275	25500403	13	1060	289469	0.69	307
25500204	13	1767287	1.36	293	25500404	13	1060	319940	0.71	320
25500205	13	>2500000	>1.88	319	25500405	13	1060	>2500000	>2.14	261
50500101	17171	1057	2.08		50500201	112		340844	4.17	400

Note. $D = \sum(n_i/N_i)$, ϵ_0 is the ultimate strain of specimen damage. Specimen numbering methods xxyzztt: xxyy means the two directions of lateral compressive stress ratio, where 2550 indicates that one direction of lateral compressive stress ratio σ_2/f_c is 0.25, another σ_3/f_c is 0.50; zz represents the amplitude loading condition; 01, 02, 03, and 04 are four testing loading conditions for low-high, high-low, low-medium-high, and high-medium-low, respectively; tt represents the sample number to each operating mode.

3.2. *Linear Fatigue Damage Analysis.* Miner [17] performed pioneering work on the amplitude fatigue linear cumulative damage rule, the P-M criterion as shown below:

$$D = \sum_{i=1}^k D_i = \sum_{i=1}^k \frac{n_i}{N_i} = 1. \quad (2)$$

In this paper, Miner experimentally verified the P-M criterion. Table 3 shows the values obtained by this work.

As shown in Table 3, our experimental result for the value of D is higher than predicted. However, considering factors that influence multiaxial fatigue, the values of D obtained can be considered within the normal range. Moreover, results indicate that the P-M criterion for multiaxial amplitude fatigue has certain limitations. These limitations are mainly caused by difficulty in satisfying the prerequisites of the principle, which are as follows: each cycle of the energy dissipation is equal under constant amplitude stress level, cumulative damage cannot be influenced by the past loading process, and the fatigue life of concrete would not be affected by variable amplitude loading order.

4. Nonlinear Damage Analysis

4.1. *Residual Strain.* Residual strains were measured during strain development along the fatigue loading direction, and

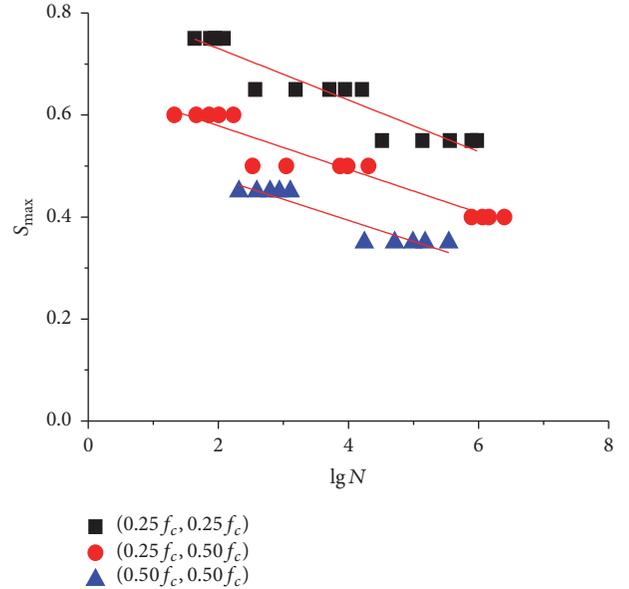


FIGURE 3: S-N Scatter-gram.

results are shown in Figures 4 and 5. As shown, under triaxial T-C-C constant amplitude cyclic loading, the development of residual strain of plain concrete in the fatigue

TABLE 3: Value D .

	[10]	[20]	[21]	[12]	This paper
Max	2.94	95.72	1.11	3.26	7.61
Min	0.36	0.01	0.21	0.38	0.31
Avg.	1.20	8.32	0.53	1.27	1.87

direction depends mainly on lateral compressive stress and is not significantly related to the stress level. The maximum strain development of constant amplitude fatigue follows an obvious three-stage rule, which is defined by the crack initiation, crack stable expansion, and crack propagation. The ratio of these three stages has a great correlation with the lateral pressure level, especially at a high lateral pressure, and the second stage of the maximum strain development is obviously longer, while the third stage becomes shorter and the specimen rapidly deteriorates. The strain development law [18, 19] follows the same pattern for uniaxial fatigue residual strain, but the value of the fatigue residual strain is larger than uniaxial. Under variable amplitude fatigue loads, the fatigue residual strain is not associated with the loading process. Development of fatigue residual strain is stable whether under variable amplitude loading or constant amplitude loading. The same is true for specimens loaded in the uniaxial direction.

Based on Figure 4, regression equations under different lateral stress ratios were analyzed using a nonlinear regression method for residual strain ε_r and relative fatigue cycle n/N as shown:

$$\varepsilon_r = 109.0 \left(\frac{n}{N}\right)^3 - 220.0 \left(\frac{n}{N}\right)^2 + 164.6 \left(\frac{n}{N}\right) \quad (3a)$$

$$\frac{\sigma_2}{f_c} = 0.25, \quad \frac{\sigma_3}{f_c} = 0.25,$$

$$\varepsilon_r = 173.9 \left(\frac{n}{N}\right)^3 - 328.1 \left(\frac{n}{N}\right)^2 + 236.0 \left(\frac{n}{N}\right) \quad (3b)$$

$$\frac{\sigma_2}{f_c} = 0.25, \quad \frac{\sigma_3}{f_c} = 0.50,$$

$$\varepsilon_r = 246.7 \left(\frac{n}{N}\right)^3 - 442.9 \left(\frac{n}{N}\right)^2 + 302.7 \left(\frac{n}{N}\right) \quad (3c)$$

$$\frac{\sigma_2}{f_c} = 0.50, \quad \frac{\sigma_3}{f_c} = 0.50.$$

Correlation coefficients R^2 of the above equations are, respectively, 0.976, 0.976, and 0.943, all the values of R^2 are greater than 0.90, and it indicates that Formulas (3a), (3b), and (3c) are suitable to express the fatigue T-C-C failure criterion. If relative fatigue cycle $n/N = 1$, the extreme fatigue residual strain ε_r^0 of concrete is, respectively, 53.6μ , 81.8μ , and 106.5μ . The extreme residual strain ε_r^0 can be used as a criterion to judge the fatigue damage of plain concrete in corresponding lateral stress ratio.

4.2. Fatigue Damage Model and Validation. According to the basic concepts of damage mechanics and the development

laws of residual strain on PC under T-C-C and uniaxial fatigue loading, the fatigue damage was defined as the ratio between the residual strain of concrete ε_r and the extreme fatigue residual strain ε_r^0 , $\varepsilon_r/\varepsilon_r^0$. The damage equation is given by

$$D = \frac{\varepsilon_r}{\varepsilon_r^0} = a \left(\frac{n}{N}\right)^3 + b \left(\frac{n}{N}\right)^2 + c \left(\frac{n}{N}\right), \quad (4)$$

where a , b , c are coefficients of the damage equation and relate to fatigue loading method and extreme fatigue residual strain. The relationships between the fatigue damage D and relative number n/N of plain concrete under T-C-C loading are shown in Figure 6. Above all, the proposed fatigue damage model can be used for multistage fatigue cumulative damage analysis of plain concrete in uniaxial and T-C-C loading. This analysis can also be used to predict remaining fatigue life of the sample.

The equivalent damage value D_e and residual fatigue life prediction value N_{2e} or N_{3e} of PC at the lateral compressive stress ratio of 0.50 under T-C-C loading are shown in Table 4; n_{20} is the fatigue life of the residual strain under two-stage loading; n_{10}/N_{1e} and n_{20}/N_{2e} are the corresponding relatively equivalent fatigue life of ε_{r1} and ε_{r2} ; N_{2e} (N_{3e}) is the remaining fatigue life prediction value (including n_{20}); D_e is the equivalent damage value, $D_e = n_1/N_{1e} + n_2/N_{2e}$ is the remaining fatigue life.

As shown in Table 4, samples tested with variable amplitude fatigue loading had a maximum equivalent damage value D_e of 1.92, a minimum of 0.65, and an average of 1.08. In comparison, the maximum damage value D of the P-M criterion (Table 3) is 7.61, the minimum is 0.31, and the average is 1.87 (not including the residual fatigue life of specimens with more than 2.5 million cycles). Meanwhile, the remaining fatigue life prediction values N_{2e} (two-grade fatigue) or N_{3e} (three-grade fatigue) are relatively close to the actual remaining fatigue life n_2 or n_3 in Table 2. Figure 7 takes N_{2e} , N_{3e} and n_2 , n_3 logarithmic, makes $\lg N_{2e}(\lg N_{3e})$ ordinate, makes $\lg n_2(\lg n_3)$ an abscissa, and converts the remaining fatigue life prediction values and the corresponding actual values into a scatter plot. If the scatter points are near the diagonal line on both sides, the forecast and experiment values of theory are satisfactory. As shown, the damage model proposed here is sufficiently accurate.

Based on the residual strain ε_r and relative fatigue cycles n/N of (3a), (3b), and (3c), the regression equation under

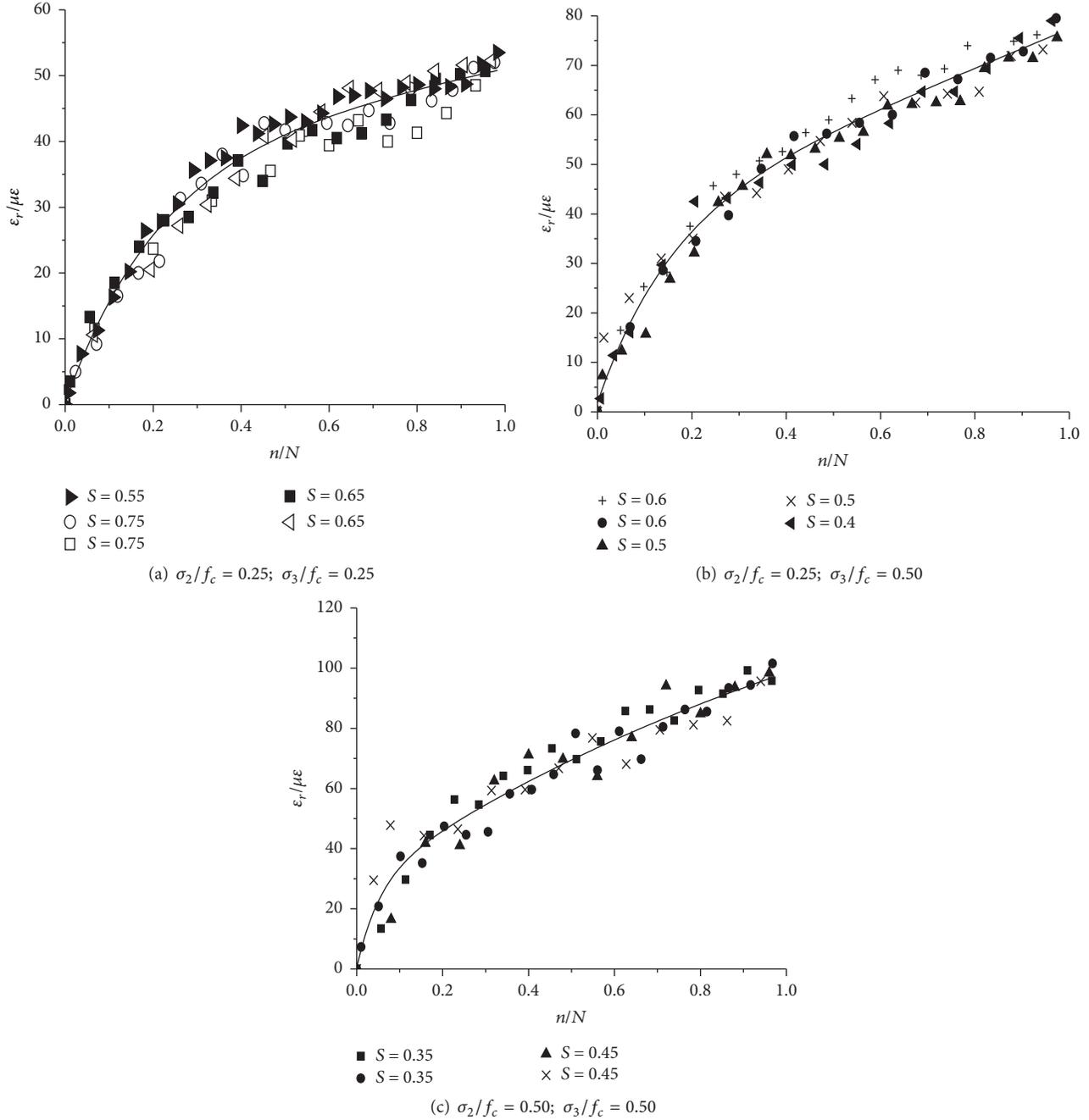


FIGURE 4: Relationship of residual strain and relative fatigue cycle in T-C-C constant amplitude loading.

different lateral stress ratios was analyzed using nonlinear regression as shown below:

$$\begin{aligned}
 D = & \left\{ \left(-\frac{1.24\sigma_2}{f_c} + \frac{0.04\sigma_3}{f_c} + 2.60 \right) \left(\frac{n}{N} \right)^3 \right. \\
 & + \left(\frac{1.82\sigma_2}{f_c} + \frac{1.34\sigma_3}{f_c} - 5.32 \right) \left(\frac{n}{N} \right)^2 \\
 & \left. + \left(-\frac{0.58\sigma_2}{f_c} - \frac{1.39\sigma_3}{f_c} + 3.72 \right) \left(\frac{n}{N} \right) \right\}. \quad (5)
 \end{aligned}$$

Using (5), Figure 8 shows the relationships between the damage variable D and lateral compressive stress of σ_2/f_c , σ_3/f_c as well as the spatial relationships in different relative cycle ratios of fatigue ($n/N = 0.2, 0.4, 0.6, 0.8$). The figure axes are the damage variable D and the lateral compressive stress ratios σ_2/f_c , σ_3/f_c , respectively.

5. Discussion

So far, there have been a lot of researches on uniaxial and multiaxial fatigue of concrete subjected to variable amplitude

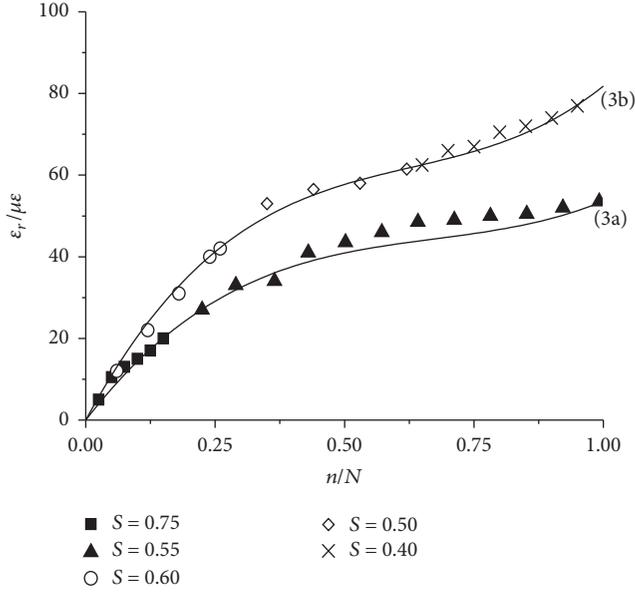


FIGURE 5: Relationship of residual strain and relative fatigue cycle in T-C-C variable amplitude loading.

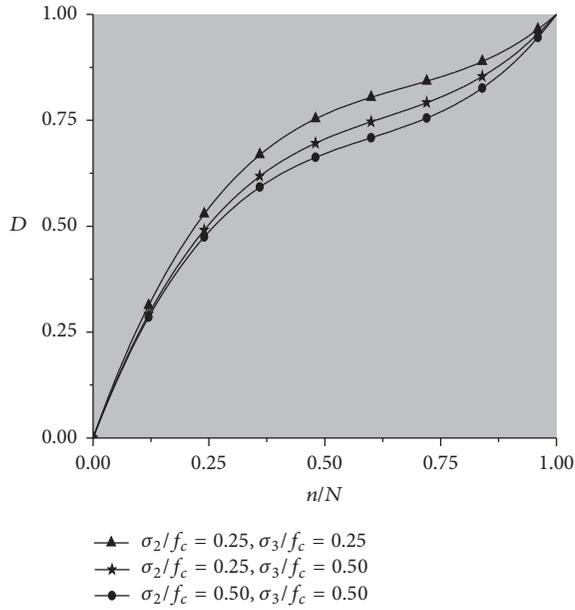


FIGURE 6: Relationship between damage and relative fatigue cycles n/N in T-C-C loading case.

compression, while little attention has been paid to biaxial and triaxial tension and compression fatigue. The main reason is that the concrete specimen is difficult to achieve repeated tension-compression loading, and the testing key technology is not complete.

- (1) For the multiaxial fatigue test, the physical centering of the sample is very important in the process of installation and testing and is more difficult than in a triaxial fatigue test. Poor alignment will result

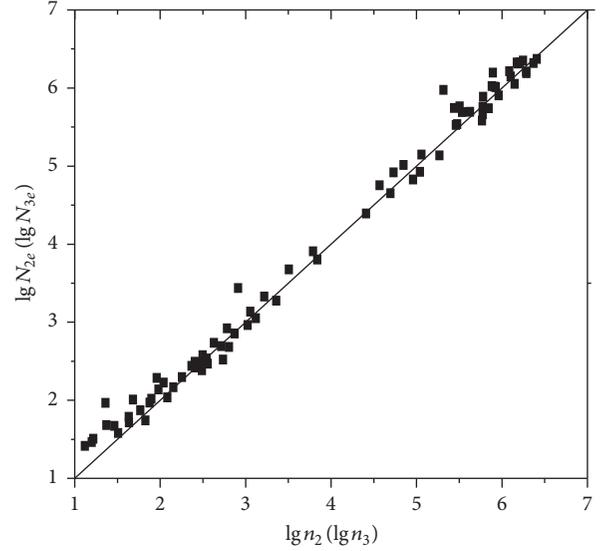


FIGURE 7: Comparison between predicted residual fatigue life and observed ones.

TABLE 4: Variable amplitude fatigue life of prediction.

Specimen number	D_e	N_{2e}	Specimen number	D_e	N_{3e}
25250101	0.88	48	25250301	1.44	109
25250102	1.37	241	25250302	0.94	93
25250103	0.88	303	25250303	0.93	26
25250104	0.91	52	25250304	1.29	293
25250105	1.09	479	25250305	1.06	47
25250201	0.89	1037225	25250401	1.51	2113472
25250202	0.91	136286	25250402	0.76	343910
25250203	0.87	140203	25250403	1.11	102601
25250204	1.01	67159	25250404	1.00	44838
25250205	1.36	1548276	25250405	0.72	84152
25500101	0.80	168	25250301	0.84	55
25500102	0.91	32	25250302	1.27	376
25500103	0.98	61	25250303	1.53	29
25500104	1.29	274	25250304	0.85	38
25500105	0.82	74	25250305	1.28	146
25500201	0.97	2350852	25250401	1.09	572043
25500202	1.13	549963	25250402	1.45	1635711
25500203	0.78	458977	25250403	1.22	335639
25500204	1.33	2245031	25250404	0.97	579068
25500205			25250405		
50500101	1.55	916	50500201	0.98	490733
50500102	1.76	330	50500201	1.92	382615
50500103	0.67	137	50500201	1.35	24700
50500104	0.65	542	50500201	0.77	82501
50500105	1.04	2134	50500201	0.63	56662

Note. D_e is equivalent damage value; N_{2e}/N_{3e} is the residual fatigue life prediction values.

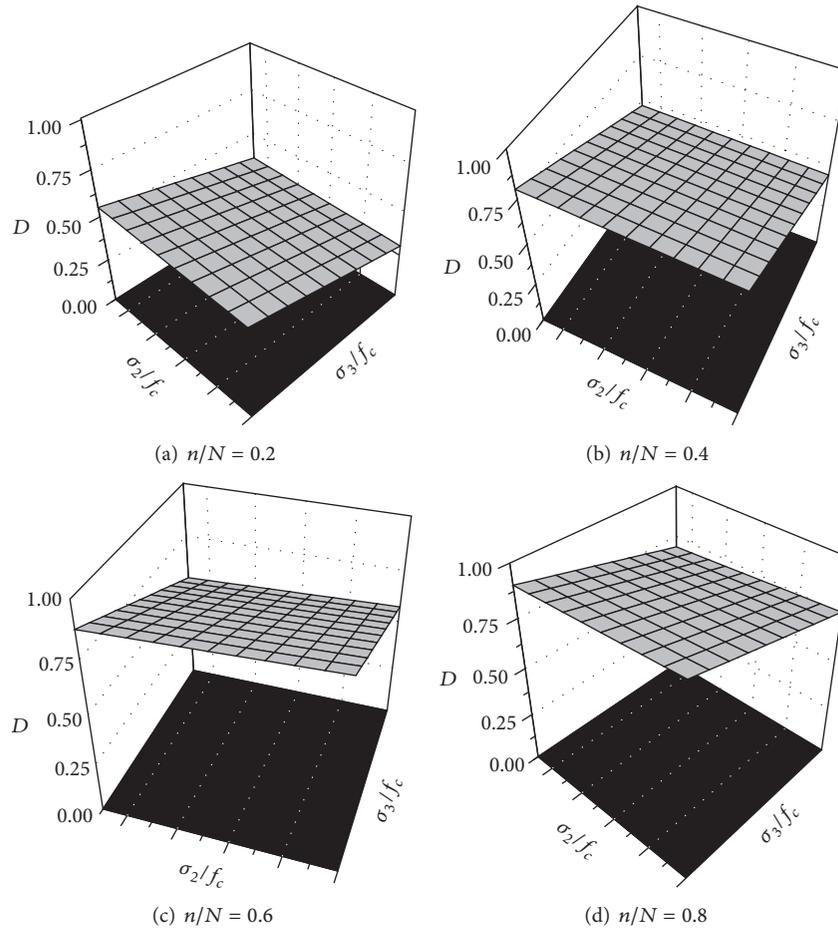


FIGURE 8: Relationship between damage D and σ_2/f_c , σ_3/f_c .

in specimen failure and consequently failure of the experiment. During testing, specimens were placed in the appropriate position and visually aligned before applying a 10 kN static preload in the vertical direction. Moreover, a larger static load was applied to the specimens to center the samples horizontally. Finally, the sample was preloaded in the same proportions more than three times in three directions to verify centering in the test apparatus. Preload levels were then increased to 20~30 kN to ensure contact between the loading plate and the specimen. Next, specimens were held in this centered position by gradually and evenly tightening eight screws at the upper and lower edges of the specimen. Fatigue tests were suspended after a dozen cyclic loads, to analyze the output of the deformation data in each direction and verify consistency. Finally, a small hammer was used to tap specimens or load heads as needed to adjust mechanical alignment through rotation of the globe hinge of the specimen in order to obtain valid data.

- (2) As the testing system uses electrohydraulic servo control technology, the system is easily self-excited. Even the original MTS single-axis fatigue testing machine can appear self-excited during testing. Here,

self-excitation refers to the system suddenly operating at a different frequency compared to the load frequency during normal operation or the ability to adjust the loading frequency to produce substantial vibration. To avoid mechanical resonance, the experiment should begin at a lower frequency running for a period of time, so that the direction of the installation of the specimen can be verified. The frequency can be smoothly increased to the ideal test frequency. The system has load control and displacement control in two directions; thus, each direction should be treated similarly to avoid self-excitation. Finally, the test system must be completely independent of the power supply to eliminate interference with other electrical equipment.

6. Conclusions

Based on analysis of experimental results from the development of fatigue strain, the following conclusions can be drawn below.

- (1) The development of fatigue residual strain in the fatigue loading direction of PC under triaxial T-C-C

constant amplitude cyclic loading is mainly dependent on the lateral compressive stress ratio and is mostly independent of stress level. The fatigue residual strain under variable amplitude fatigue loading was found to be associated with the relative fatigue cycle and lateral compressive stress ratio but is independent of the loading process. Strain development is as stable as the constant loading amplitude.

- (2) The residual strain ε_r and fatigue relative cycle n/N were used to develop a nonlinear regression model. The ultimate residual strains ε_r^0 of concrete fatigue damage are, respectively, 53.6μ , 81.8μ , and 106.5μ . This can be used as a criterion to judge the fatigue damage of plain concrete in corresponding lateral stress ratios.
- (3) Relative residual strain was defined as the damage variant, a damage evolution for plain concrete was proposed, and models for damage analysis and prediction of fatigue life were executed. The failure models developed can be used to predict the residual remaining life of plain concrete under multiaxial fatigue loads. Model predictions and the measured results are in good agreement.
- (4) It is proved that Miner's rule is not applicable to multiaxial loading of plain concrete and has certain limitations for calculating multiaxial amplitude fatigue.

Competing Interests

The authors declare that they have no competing interests.

Acknowledgments

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