Research Article

The Novel Successive Variational Mode Decomposition and Weighted Regularized Extreme Learning Machine for Fault Diagnosis of Automobile Gearbox

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1. Introduction

Gearbox is the key component of automobile, and condition monitoring and fault diagnosis for automobile gearbox are very significant [1–4]. Recently, artificial neural networks (ANNs), support vector machine (SVM), etc. have been successfully applied to diagnose the faults of gearbox. For instance, Qiu et al. presented a deep convolutional neural network model for intelligent fault diagnosis of a gearbox under different operational conditions [5]. Jedliński and Jonak presented an early fault detection method in gearboxes based on support vector machines and multilayer perceptrons with a continuous wavelet transform [6]. Extreme learning machine (ELM) is a simple and efficient single hidden layer feedforward network [7–9]. Compared with ANNs and SVM, ELM has better generalization ability [10], so ELM has a good application prospect in the field of fault diagnosis for gearbox. In order to improve the performance of ELM, weighted regularized extreme learning machine (WRELM) is the new extreme learning machine using the weight of each sample with the nonparametric kernel density estimation and can find the optimal weight for each sample. Thus, WRELM is used to classify the states of gearbox.

In addition, the feature extraction of the vibrational signal of gearbox has a great influence on the accuracy of fault diagnosis of gearbox. Recently, empirical mode decomposition (EMD), variational mode decomposition (VMD), etc. have been successfully applied to extract the features of gearbox. Hongmei Liu et al. applied empirical mode decomposition in the feature extraction of the vibrational signal of gearbox [11]. Vikas Sharma and Anand Parey applied variational mode decomposition in the feature extraction of the vibrational signal of gearbox under varying speed [12]. There are problems such as mode mixing in EMD; VMD is a new multicomponent signal decomposition method based on Wiener filtering and Hilbert transform, which aims to make decomposition of a target signal into a set of modes with sparsity properties being achievable [13–15]. In order to improve the performance of VMD,

In order to improve the diagnosis accuracies of the current diagnosis methods, a novel fault diagnosis method of automobile gearbox based on novel successive variational mode decomposition and weighted regularized extreme learning machine is presented for fault diagnosis of gearbox in this paper. The novel successive variational mode decomposition (SVMD) is presented to improve the traditional variational mode decomposition, which finds modes one after the other, and this succession helps increase convergence rate and also not extract the unwanted modes; weighted regularized extreme learning machine (WRELM) is presented to improve the traditional extreme learning machine, which uses the weight of each sample with the nonparametric kernel density estimation and can find the optimal weight for each sample. The test results indicate that the diagnosis accuracy of SVMD-WRELM for gearbox is better than that of VMD-WRELM, VMD-ELM.

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successive variational mode decomposition (SVMD) finds modes one after the other, and this succession helps increase convergence rate and also not extract the unwanted modes.

Thus, in order to improve the diagnosis accuracies of the current diagnosis methods, a novel fault diagnosis method based on successive variational mode decomposition and weighted regularized extreme learning machine (SVMD-WRELM) is presented for fault diagnosis of automobile gearbox in this paper. The four states of automobile gearbox including normal state, wear and tear, pitting fault, and snaggletooth fault are used in this experiment. The testing results indicate that the diagnosis accuracies of SVMD-WRELM for gearbox are better than those of VMD-WRELM, VMD-ELM.

\[ J([u_i],[\omega_i],\lambda) = \alpha \sum_{l=1}^L \left\| \partial_t \left[ (\rho(t) + \frac{j}{\eta t}) * u_i(t) \right] e^{-j\omega t} \right\|^2 + \left\| f(t) - \sum_{l=1}^L u_i(t) \right\|^2 + \left\langle \lambda(t), f(t) - \sum_{l=1}^L u_i(t) \right\rangle, \]

where \( \alpha \) denotes the constraint factor and \( \lambda(t) \) denotes the Lagrangian multiplier.

Successive variational mode decomposition is a method which finds modes one after the other, and this succession helps increase convergence rate and also not extract the unwanted modes. In successive variational mode decomposition, the combination of quadratic penalty term and Lagrangian multiplier can be used to establish the augmented Lagrangian function as

\[ G([u_i],[\omega_i],\lambda) = \alpha \sum_{l=1}^L \left\| \partial_t \left[ (\rho(t) + \frac{j}{\eta t}) * u_i(t) \right] e^{-j\omega t} \right\|^2 + \left\| f(t) - \sum_{l=1}^L u_i(t) \right\|^2 + \left\langle \lambda(t), f(t) - \sum_{l=1}^L u_i(t) \right\rangle + \left\langle \lambda(t), f(t) - \left( \sum_{l=1}^L u_i(t) \right) \right\rangle. \]

After using Parseval’s equality, eq (4) is transformed into

\[ G([u_i],[\omega_i],\lambda) = \alpha \left\| j(\omega - \omega_L) \left[ 1 + \text{sgn}(\omega) \overline{u}_L(\omega) \right] \right\|^2 + \left\| \overline{f}_L(\omega) - \sum_{l=1}^{L-1} \overline{u}_l(\omega) \right\|^2 + \left\| \overline{\lambda}(\omega) - \sum_{l=1}^{L-1} \overline{u}_l(\omega) \right\|^2. \]

By letting the first variation vanish for the positive frequencies by minimizing eq (5),

\[ \tilde{\overline{u}}_L^{n+1}(\omega) = \frac{\overline{f}_L(n) - \sum_{l=1}^{L-1} \overline{u}_l(\omega) + (\overline{\lambda}(\omega)/2)}{1 + 2\alpha(\omega - \omega_L)^2 + \sum_{l=1}^{L-1} (1/\alpha^2)(\omega - \omega_l)^2}. \]
By minimizing eq.(6), \( f_{\omega}^{n+1}(\omega) \) will be described as
\[
\bar{f}_{\omega}^{n+1}(\omega) = \frac{\alpha^2(\omega - \omega_{n+1}^{\omega})^4(\bar{f}(\omega) - (\bar{f}_n^{\omega}(\omega) + \sum_{l=1}^{L-1} u_l(\omega)) + (\bar{\lambda}(\omega)/2)) - \sum_{l=1}^{L-1} u_l(\omega)}{1 + \alpha^2(\omega - \omega_{n+1}^{\omega})^4}.
\]
(7)

The equation for updating the Lagrangian multiplier \( \lambda \) is achieved by the dual ascent method:
\[
\bar{\lambda}^{n+1} = \bar{\lambda}^n + \tau \left[ \bar{f}(\omega) - \left( \bar{u}_L^{n+1}(\omega) + \sum_{l=1}^{L-1} u_l(\omega) \right) \right],
\]
(8)

As shown in Figures 1 and 2, the six decomposition signals (SVMDSs) described as SVMDS1–SVMDS6 of the vibrational signal of gearbox are obtained based on SVMD. The features of the vibrational signal of gearbox are obtained by calculating the Shannon entropy of SVMDS1–SVMDS6. In Figure 1, abscissa values are the sampling data, and ordinate values are the amplitudes of the vibrational signal of gearbox; in Figure 2, abscissa values are the sampling data, and ordinate values are the amplitudes of SVMDS1–SVMDS6 of the vibrational signal of gearbox, respectively.

Figure 3 gives the comparison among the feature values of normal state of the vibrational signal of gearbox obtained by SVMD, the feature values of fault state of the vibrational signal of gearbox obtained by SVMD, the feature values of normal state of the vibrational signal of gearbox obtained by VMD, and the feature values of fault state of the vibrational signal of gearbox obtained by VMD, and abscissa values are the six features and ordinate values are the values of the six features, which indicates that there are more obvious distinctions between the feature values of normal state and fault state of gearbox by SVMD than those by VMD.

3. Weighted Regularized Extreme Learning Machine

Assume \( N \) hidden nodes in extreme learning machine and a sample pair \( \{X_i, P_i\} \), and the output of extreme learning machine can be expressed as followings:
\[
f(X_i) = \sum_{n=1}^{N} \alpha_n H(\varphi_n, X_i, b_n), \quad i = 1, 2, \ldots, N,
\]
(10)
where \( H(\cdot) \) denotes the activation function, \( \varphi_n \) denotes the input weight vector, \( \alpha_n \) denotes the \( n \)th output weight, and \( b_n \) denotes the corresponding bias.

\[
\bar{P} = H\alpha = \begin{bmatrix}
H(\varphi_1, X_1, b_1) & H(\varphi_2, X_1, b_2) & \cdots & H(\varphi_N, X_1, b_N) \\
H(\varphi_1, X_2, b_1) & H(\varphi_2, X_2, b_2) & \cdots & H(\varphi_N, X_2, b_N) \\
\vdots & \vdots & \ddots & \vdots \\
H(\varphi_1, X_N, b_1) & H(\varphi_2, X_N, b_2) & \cdots & H(\varphi_N, X_N, b_N)
\end{bmatrix} \cdot \alpha,
\]
(11)

arg min \( C\|\alpha\|^2 + \|\alpha\|^2 \),
(13)
subject to the conditions,
\[
P = H\alpha + \varepsilon,
\]
(14)
where \( \sigma \) denotes a diagonal matrix, \( \varepsilon \) denotes the vector of regression error, and \( C \) denotes a regularization term.

Lagrange multipliers are introduced to solve the above minimization problem, and the corresponding solution for \( \alpha \) is given as
Figure 1: The decomposition of the vibrational signal of gearbox based on SVMD.

Figure 2: Six SVMDs.
\[ \alpha = \left( H'\sigma^2H + \frac{I}{C} \right)^{-1} H'\sigma^2P. \]  

(15)

4. Experimental Analysis

Figure 4 gives the framework of fault diagnosis for gearbox, which includes motor, coupling, gearbox, acceleration transducer, load motor, brake, data acquisition board, and computer. The vibrational signals of gearbox are measured with acceleration transducer, and the vibrational signals of gearbox are obtained by data acquisition board. Sampling frequency is 10 KHz, and the load is 1 N.m. The common faults of gearbox are wear and tear, pitting fault, and snaggletooth fault: wear and tear indicates the loss, injury of tooth surface due to suffering from pressure in the process of operation; pitting fault indicates local corrosion of tooth surface due to fatigue of tooth surface; and snaggletooth fault indicates crack of tooth.

The four states of gearbox including normal state, wear and tear, pitting fault, and snaggletooth fault are used in this experiment, among which normal state is denoted as state 1 of gearbox, wear and tear is denoted as state 2 of gearbox, pitting fault is denoted as state 3 of gearbox, and snaggletooth fault is denoted as state 4 of gearbox. 320 training samples include 80 samples denoting state 1 of gearbox, 80 samples denoting state 2 of gearbox, 80 samples denoting state 3 of gearbox, and 80 samples denoting state 4 of gearbox. 200 testing samples include 50 samples denoting state 1 of gearbox, 50 samples denoting state 2 of gearbox, 50 samples denoting state 3 of gearbox, and 50 samples denoting state 4 of gearbox. There is no intersection between the 320 training samples and the 200 testing samples.

The flow chart of fault diagnosis method based on SVMD-WRELM is described in Figure 5. In the experiment, the running speed of VMD for the vibrational signal of a sample of gearbox is about 0.75 s, and the running speed of VMD for the vibrational signal of a sample of gearbox is about 0.35 s, which testifies the fast convergence of VMD.

Several repeated experiments were performed, and the experimental results were identical. The comparison between actual results and diagnosis results for gearbox by

Figure 3: The comparison among the feature values of normal state of the vibrational signal of gearbox obtained by SVMD, the feature values of fault state of the vibrational signal of gearbox obtained by SVMD, the feature values of normal state of the vibrational signal of gearbox obtained by VMD, and the feature values of fault state of the vibrational signal of gearbox obtained by VMD.

Figure 4: Framework of fault diagnosis for gearbox.
SVMD-WRELM are given in Figure 6, and the diagnosis accuracy of SVMD-WRELM for gearbox is 99%. The comparison between actual results and diagnosis results for gearbox by VMD-WRELM is given in Figure 7, and the diagnosis accuracy of VMD-WRELM for gearbox is 97%. The comparison between actual results and diagnosis results for gearbox by VMD-ELM is given in Figure 8, and the diagnosis accuracy of VMD-ELM for gearbox is 93.5%. In Figures 6–8, abscissa values are the sample number, and ordinate values are the four states including normal state, wear and tear, pitting fault, and snaggletooth fault, among which normal state is denoted as state 1 of gearbox, wear and tear is denoted as state 2 of gearbox, pitting fault is denoted as state 3 of gearbox, and snaggletooth fault is denoted as state 4 of gearbox.

As shown in Table 1, the diagnosis accuracies of SVMD-WRELM for gearbox are better than those of VMD-WRELM, VMD-ELM, and the diagnosis accuracies of VMD-WRELM are better than those of VMD-ELM. It can be seen that SVMD is superior to VMD, and WRELM is superior to ELM. Therefore, fault diagnosis for gearbox by SVMD-WRELM is feasible.
5. Conclusions
A novel fault diagnosis method based on SVMD and WRELM is presented for fault diagnosis of automobile gearbox in this paper. SVMD finds modes one after the other, and this succession helps increase convergence rate and also not extract the unwanted modes, and WRELM uses the weight of each sample with the nonparametric kernel density estimation and find the optimal weight for each sample. The diagnosis accuracy of SVMD-WRELM for gearbox is 99%, the diagnosis accuracy of VMD-WRELM for gearbox is 97%, and the diagnosis accuracy of VMD-ELM for gearbox is 93.5%. The testing results indicate that SVMD is superior to VMD, and WRELM is superior to ELM. It can be concluded that the diagnosis accuracies of SVMD-WRELM for gearbox are better than those of VMD-WRELM, VMD-ELM.

Data Availability
The data that support the findings of the research are available from the corresponding author.

Conflicts of Interest
The authors declare that there are no conflicts of interest regarding the publication of this article.

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References