Spatial Property of Optical Wave Propagation through Anisotropic Atmospheric Turbulence

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For the free-space optical (FSO) communication system, the spatial coherence of a laser beam is influenced obviously as it propagates through the atmosphere. This loss of spatial coherence limits the degree to which the laser beam is collimated or focused, resulting in a significant decrease in the power level of optical communication and radar systems. In this work, the analytic expressions of wave structure function for plane and spherical wave propagation through anisotropic non-Kolmogorov turbulence in a horizontal path are derived. Moreover, the new expressions for spatial coherence radius are obtained considering different scales of atmospheric turbulence. Using the newly obtained expressions for the spatial coherent radius, the effects of the inner scales and the outer scales of the turbulence, the power law exponent, and the anisotropic factor are analyzed. The analytical simulation results show that the wave structure functions are greatly influenced by the power law exponent $\alpha$, the anisotropic factor $\zeta$, the turbulence strength $\tilde{\sigma}_R$, and the turbulence scales. Moreover, the spatial coherence radii are also significantly affected by the anisotropic factor $\zeta$ and the turbulence strength $\tilde{\sigma}_R$, while they are gently influenced by the power law exponent $\alpha$ and the inner scales of the optical waves.

1. Introduction

In recent years, the traffic carried by the telecommunication network is growing significantly, especially the wireless network. The popularity of wireless data and mobile Internet is much faster than anyone imagined, and it enhances voice communication with much richer multimedia content. Mobile data traffic and mobile service spectrum have increased by many orders of magnitude from 2010 to 2020 [1]. This is an important topic of the sixth generation (6G) wireless communication. On 6G communication, optical wireless communication (OWC) technology has many advantages in frequency spectrum, security, and transmission rate, which can be used as a potential replacement and supplement of radio frequency-based wireless communication technology. OWC technology provides a basic combination of the various advantages necessary to deliver high-speed services to optical backbone networks. It provides an unlicensed spectrum, almost unlimited data rate, low-cost development, and convenient installation [2]. On the other hand, the ground-based point-to-point OWC system, also known as free-space optical (FSO) communication system, works at near-infrared frequency. Beam spreading caused by atmospheric turbulence occupies a very important position in FSO communication systems, because it determines the loss of power at the receiver plane [3]. For optical wave propagation, the classic Kolmogorov model has been widely used in theoretical researches due to its simple mathematical form [3–5]. Over the years, the Kolmogorov model is extended and several non-Kolmogorov turbulence models have been also proposed [6–13]. Toselli et al. [6] is one of them, and they analyze the angle of arrival fluctuations by using the generalized exponent factor $\alpha$ instead of the standard exponent value 11/3. The anisotropic factor is also used to describe anisotropy of the atmosphere turbulence [7], and the generalized non-Kolmogorov von Karman spectrum of...
the anisotropic atmospheric turbulence is available [8–10]. In addition, there are also numerous studies on beam wander, loss of spatial coherence, temporal frequency spread, and the angle of arrival fluctuation [14–21], which are all related to the random fluctuation of optical waves propagating through random media.

Lately, more research attention is drawn to the theoretical survey of wave structure function (WSF) for the long-exposure modulation transfer function (MTF) and spatial coherence radius (SCR) [22–29]. Based on the Rytov approximation method, a researcher like Young proposes new expressions for the WSFs of optical waves, which fit the moderate to strong fluctuation regimes [22, 23]. Lu et al. have derived new expressions for the WSFs and the SCRs for plane waves and spherical waves propagating through homogeneous and isotropic oceanic turbulence [25]. Moreover, Cui et al. consider the turbulence scales and have derived the long-exposure MTFs for plane waves and spherical waves propagating through anisotropic non-Kolmogorov atmospheric turbulence [26, 27]; Kottiang and Choi and Guan et al. also have derived a new long-exposure MTF for Gaussian waves propagating through isotropic non-Kolmogorov atmospheric turbulence and anisotropic maritime turbulence [28, 29].

In this study, we derive new WSF and SCR expressions for the plane waves and the spherical waves which propagate in the anisotropic non-Kolmogorov atmosphere turbulence. Here, the generalized von Karman model is used by incorporating the anisotropic factor \( \xi^{2-\alpha} \). In the simulation analyses, using the newly derived WSF and SCR expressions, the effects of the inner scale and the outer scale of the eddy size are investigated. In addition to the influences of the power law exponent, the turbulence strength and the anisotropic factor, which are all affecting parameters of the WSFs and SCRs, are also carefully analyzed.

### 2. Anisotropic Non-Kolmogorov Spectrum with Inner and Outer Scales

Stribling et al. [30] developed a power spectrum in non-Kolmogorov turbulence as the power law for the spectrum of the index of refraction fluctuations is varied from 3 to 4. This power spectrum, which we call the conventional isotropic non-Kolmogorov spectrum:

\[
\Phi_n(\kappa, \alpha) = A(\alpha) \xi^2 \kappa^{-\alpha} \kappa^2 + \kappa_0^2 \]

\[
A(\alpha) = \frac{\Gamma(\alpha - 1)}{4\pi^2} \cos \left( \frac{\alpha \pi}{2} \right),
\]

where \( \Gamma(\cdot) \) is the gamma function, \( \kappa \) is the spatial wave number, \( \alpha \) is the power law exponent, and \( \xi^2 \) is the generalized structure parameter with \( m^{3-\alpha} \) as its unit. The function \( A(\alpha) \) maintains the consistency between the index structure function and its power spectrum.

Tozelli in [7] proposed a new power spectrum by introducing an effective anisotropic parameter \( \xi \). When there are non-Kolmogorov power law and anisotropy along the propagation direction, it is helpful to simulate optical turbulence. Also, the concept of atmospheric turbulence anisotropy at different scales is introduced:

\[
\Phi_n(\kappa, \alpha, \xi) = A(\alpha) \xi^2 \kappa^{-\alpha} \left[ \kappa^2 + \kappa_0^2 \right]^{-\alpha/2} \cdot \exp \left( \frac{-\xi^2}{\kappa_0^2 \kappa^2} \right) (\kappa > 0, 3 < \alpha < 4),
\]

where \( \xi \) is the anisotropic factor; \( \kappa_0 = 2\pi/L_0 \) and \( L_0 \) is the outer scale parameter; \( \kappa = C(\alpha)/L_0 \) and \( L_0 \) is the inner scale parameter; \( \kappa = \sqrt{\xi^2 (\kappa_0^2 + \kappa_0^2) + \kappa^2} = \sqrt{\xi^2 \kappa_0^2 + \kappa^2} \) and \( \kappa_\alpha, \kappa_\gamma \), and \( \kappa_\rho \) are the components of \( \kappa \) in \( x, y, \) and \( z \) direction; and \( C(\alpha) = [\Gamma((5 - \alpha)/2)]A(\alpha)/2\pi^{(1/\alpha - 5)} \).

In this case, Equation (2) can be defined as the one in [6], which is formed by multiplying the generalized von Karman model with the anisotropic factor \( \xi^{2-\alpha} \). The resulting expression is then the modified anisotropic non-Kolmogorov power spectrum, and it is defined as follows [31]:

\[
\Phi_n(\kappa, \alpha, \xi) = A(\alpha) \xi^2 \kappa^{-\alpha} \left[ \kappa^2 + \kappa_0^2 \right]^{-\alpha/2} 
\cdot \exp \left( \frac{-\xi^2}{\kappa_0^2 \kappa^2} \right) (\kappa > 0, 3 < \alpha < 4),
\]

where \( \kappa_0^2 = \kappa_\alpha^2 \kappa_\rho^2 \) and \( \kappa_0^2 = \kappa_\alpha^2 / \kappa^2 \).

### 3. The Expressions for Wave Structure Functions

In order to evaluate the performance of optical wave structure function and spatial coherence radius in atmospheric turbulence, we need to derive the wave structure function of optical waves first. In this paper, we first derive the wave structure function of plane wave and spherical wave and then use these equations to derive their spatial coherence radius.

#### 3.1. The Plane Wave Structure Function

The WSF of optical waves propagating in isotropic non-Kolmogorov turbulence is proposed in [3], and it can be used to calculate the spatial coherence radius of the optical waves; the formulae are shown as follows:

\[
D_p(\rho, \alpha) = 8\pi^2 \kappa^2 L \int_0^{\infty} \kappa \Phi_n(\kappa, \alpha) [1 - J_0(\kappa \rho)] d\kappa,
\]

\[
D_p(\rho, \alpha) = 8\pi^2 \kappa^2 L \int_0^{\infty} \kappa \Phi_n(\kappa, \alpha) [1 - J_0(\kappa \rho)] d\kappa d\xi,
\]

where \( D_p(\rho, \alpha) \) is the plane wave structure function; \( D_p(\rho, \alpha) \) is the spherical wave structure function; \( \rho \) is the scalar separation distance between two points in the 2D plane; \( \kappa = 2\pi/\lambda \) is the optical wave number; \( \xi = 1 - z/L \) and \( L \) is the path length; \( z \) is the propagation distance; and \( J_0(\cdot) \) is the zero-order Bessel function of the first kind.
In this paper, Equation (3) is used as the expression for the anisotropic non-Kolmogorov power spectrum in our derivation of new wave structure function expressions for optical waves. Then, Equations (4) and (5) can be rewritten as follows:

\[
D_{pl}(\rho, \alpha, \zeta) = 8\pi^2 k^2 L \int_0^\infty \kappa \Phi_n(\kappa, \alpha, \zeta)[1 - J_0(\kappa \rho)]d\kappa, \tag{6}
\]

\[
D_{sp}(\rho, \alpha, \zeta) = 8\pi^2 k^2 L \left[ \frac{1}{0} \int_0^\infty \kappa \Phi_n(\kappa, \alpha, \zeta)[1 - J_0(\kappa \rho)]d\kappa d\xi. \tag{7}
\]

By substituting Equation (3) into Equation (6) and expanding \( J_0(\cdot) \) as a series representation, one can obtain the new WSF expression for the plane waves as follows:

\[
D_{pl}(\rho, \alpha, \zeta) = 8\pi^2 k^2 L \alpha C_n^2 \kappa^2 \alpha - \sum_{n=1}^\infty \frac{(-1)^{n-1}}{n! \Gamma(n)} \left( \frac{\rho}{2} \right)^{2n} \times \int_0^\infty \kappa^{2n+1} \left[ \kappa^2 + \kappa_0^2 \right] ^{-\alpha/2} \exp \left( -\frac{\kappa^2}{\kappa_0^2} \right) d\kappa. \tag{8}
\]

Here, the integration can be resolved by using the confluent hypergeometric function of the second kind defined as follows [32]:

\[
U(a, c, z) = \frac{1}{\Gamma(a)} \int_0^\infty e^{-zt} t^{-a-1}(1 + t)^{c-a-1} dt, \quad a > 0, \text{Re}(z) > 0, \tag{9}
\]

\[
U(a, c, z) = \frac{\Gamma(1 - c)}{\Gamma(1 + a - c)} + \frac{\Gamma(c - 1)}{\Gamma(a)} z^{-a}, \quad |z| < 1. \tag{10}
\]

Then, Equation (8) can be derived as follows:

\[
D_{pl}(\rho, \alpha, \zeta) = 4\pi^2 k^2 L \alpha C_n^2 \kappa^2 \alpha - \sum_{n=1}^\infty \frac{(-1)^{n-1}}{n! \Gamma(n)} \left( \frac{\rho}{2} \right)^{2n} \kappa^{2n+2-a} \times \left\{ n! \Gamma(n+1) (\alpha/2 - 1) + (1 - \frac{\alpha}{2}) \Gamma(1 - \frac{\alpha}{2}) \kappa_0^{2n+2-a} \right\}. \tag{11}
\]

Finally, the new expression of the wave structure function for the plane waves is defined as follows:

\[
D_{pl}(\rho, \alpha, \zeta) = 4\pi^2 k^2 L \alpha C_n^2 \kappa^2 \alpha - \sum_{n=1}^\infty \frac{(-1)^{n-1}}{n! \Gamma(n)} \left( \frac{\rho}{2} \right)^{2n} \kappa_0^{2n+2-a} \times \left\{ \frac{\kappa_0^{2n-a}}{(\alpha - 2)(\alpha - 4)} \left[ \Gamma\left(1 - \frac{\alpha}{2}\right) [1 - J(\alpha)] + \frac{\rho^2 \kappa_0^{2-a}}{(\alpha - 2)(\alpha - 4)} \right] \right\}. \tag{12}
\]

\[
J(\alpha) = \frac{1}{\Gamma(\alpha)} \left( \frac{\alpha}{2} ; \frac{\rho^2 \kappa_0^{2-a}}{4} \right), \tag{13}
\]

where \( \frac{1}{\Gamma(\cdot)} \) is the confluent hypergeometric function of the first kind [32].

3.2. The Spherical Wave Structure Function. By substituting Equation (3) into Equation (7) and expanding \( J_0(\cdot) \) as a series representation, one can obtain the new expression of the wave structure function for the spherical waves. It is expressed as follows:

\[
D_{sp}(\rho, \alpha, \zeta) = 8\pi^2 k^2 L \alpha C_n^2 \kappa^2 \alpha - \sum_{n=0}^\infty \frac{(-1)^{n-1}}{n! \Gamma(n)} \left( \frac{\rho}{2} \right)^{2n} \times \int_0^\infty \kappa^{2n+1} \left[ \kappa^2 + \kappa_0^2 \right] ^{a/2} \exp \left( -\frac{\kappa^2}{\kappa_0^2} \right) d\kappa d\xi. \tag{14}
\]

Using Equations (9) and (10), the final expression of the WSF for the spherical waves can be derived and it is rewritten as follows:

\[
D_{sp}(\rho, \alpha, \zeta) = 4\pi^2 k^2 L \alpha C_n^2 \kappa^2 \alpha - \sum_{n=0}^\infty \frac{(-1)^{n-1}}{n! \Gamma(n)} \left( \frac{\rho}{2} \right)^{2n} \times \int_0^\infty \kappa^{2n+1} \left[ \kappa^2 + \kappa_0^2 \right] ^{a/2} \exp \left( -\frac{\kappa^2}{\kappa_0^2} \right) d\kappa d\xi. \tag{15}
\]

\[
K(\alpha) = \Gamma \left( \frac{1}{2} \right) ; 1; \frac{\rho^2 \kappa_0^{2-a}}{4} \right), \tag{16}
\]

where \( \frac{1}{\Gamma(q)} \) is the generalized hypergeometric function and \( p \) and \( q \) are nonnegative integers [32].

4. New Expressions for Spatial Coherence Radius

The main purpose of this section is to calculate the spatial coherence radius of the optical waves. It is used to determine the spatial coherence radius of the wave at the receiver pupil plane. As we know, the spatial coherence radius defines the effective receiver aperture size in a heterodyne detection system. The new expressions for SCRs of the plane waves and the spherical waves are derived in this section. The SCR derivations begin with the new WSFs derived in the previous section. Those WSFs need to be approximated and simplified to be used effectively in numerical computations when one performs computer simulations.

Consider the WSFs in Equations (12) and (15). Those equations involve the confluent hypergeometric functions \( _1 F_1(\cdot) \) and \( _2 F_2(\cdot) \). Those hypergeometric function can be approximately expressed as follows [32]:

\[
_1 F_1(a; c; z) = \begin{cases} 
1 - \frac{az}{c}, & |z| < 1, \\
\Gamma(c) \left( \frac{\Gamma(c - a)}{\Gamma(c - a)} \right) \left( \frac{z^a}{c} \right), & \text{Re}(z) > 1,
\end{cases} \tag{17}
\]

wireless communications and mobile computing
Equations (17) and (18) can be substituted into Equations (12) and (15), respectively. The WSFs of the optical waves can be rewritten as follows:

\[ D_{\rho}(\rho, \alpha, \xi) = \begin{cases} 
R(a)\sigma^2_{\alpha}(a)\sqrt{2^{a}r_{\alpha}}(1 - \frac{a}{2}) - \frac{1}{2} \Gamma(1 - \frac{a}{2}) \left[ \Gamma\left(1 - \frac{a}{2}\right)\right]^{-1}, & \rho \gg l_0, \\
R(a)\sigma^2_{\alpha}(a)\sqrt{2^{a}r_{\alpha}}(1 - \frac{a}{2}) - \frac{1}{2} \Gamma(1 - \frac{a}{2}) \left[ \Gamma\left(1 - \frac{a}{2}\right)\right]^{-1}, & \rho < c_{l0}, 
\end{cases} \]

(19)

and the result of Equations (25) and (26) is consistent with the research in [3].

5. Evaluations Using Numerical Analysis

Based on the above derived new analytic expressions, we analyze the wave structure function and spatial coherence radius for the plane and spherical wave propagation in anisotropic non-Kolmogorov turbulence. There are two sets of new expressions derived, and they are set for evaluation with respect to various characterizing parameters. Those are WSFs defined in Equations (12) and (15) and SCRs defined in Equations (23) and (24), respectively. We have made some general assumptions in the numerical simulations: the optical waves propagate with the generalized structure parameter \( C_n^2 = 1.4 \times 10^{-14} m^{-3/2} \); the wavelength \( \lambda = 1.65 \times 10^{-6} m \); the scalar separation distance is \( \rho = 3 \) cm, the inner scale of the eddy size is \( 1 \) mm, and the outer scale of the eddy size is \( 10 \) m; the optical path lengths vary from \( 100 \) m to \( 8 \) km; the power law exponent \( \alpha \) varies from 3 to 4; and the case of \( l_0 < < \rho < < L_0 \) is used for the SCR simulations.

5.1. Evaluations on WSFs. The first set of simulations are performed using the new expressions of wave structure function defined in Equations (12) and (14). The focus of the evaluation is to analyze the behaviors of the WSFs in terms of various characterizing parameters. Those include the power law exponent \( \alpha \), the turbulence strength \( \sigma_{\alpha}^2 \), and the anisotropic factor \( \xi \).

Figure 1(a) shows the behavior of the WSF with respect to the increasing power law exponent \( \alpha \), when the anisotropic factor \( \xi = 1 \), which actually makes the turbulence isotropic. The WSFs increase when \( \alpha \) varies from 3 to 3.3 and then decrease gently afterwards. One can see the smooth bumps that the WSFs get to their maximum when \( \alpha = 3.3 \). On the other hand, Figure 1(b) shows the behaviors of the WSF with respect to the turbulence strength \( \sigma_{\alpha}^2 \). The WSFs monotonically increase as the turbulence strength increases. One can observe that the values of WSF for the plane waves are always bigger than those of spherical waves in both figures.
Figure 2 shows the behavior of the WSF with respect to the increasing turbulence strength $\tilde{\sigma}_R^2$ and the increasing anisotropic factor $\zeta$. Figure 2(a) is for the plane waves, and Figure 2(b) is for the spherical waves. In both cases, the WSFs increase as the turbulence strength gets stronger. Also, it is also important to note that the WSFs are significantly influenced by the anisotropic factor $\zeta$ that the strength of the WSFs gets as much as 400 times weaker as the anisotropy increases from 1 to 50.

Figure 3 shows the behavior of the WSF with respect to the scales of the eddy sizes. In these simulations, we have set that the anisotropic factor $\zeta = 1$ and the power law exponent $\alpha = 11/3$. In Figure 3(a), one can observe that the WSFs for both optical waves slowly decrease as the inner scale of the eddy size $l_0$ increases. On the other hand, in Figure 3(b), the WSFs increase asymptotically as the outer scale of the eddy size $L_0$ increases. Note that the WSFs increase sheer over the outer scale of the eddy size up to 20 meters.
6. Evaluation on SCRs

The second set of simulations is performed using the new expressions of spatial coherence radiuses defined in Equations (23) and (24). Similar to the simulations using the WSFs, the focus of the evaluation is also to analyze the behaviors of SCRs in terms of various characterization parameters. Those include the power law exponent \( \alpha \), the turbulence strength \( \sim \sigma^2_R \), and the anisotropic factor \( \zeta \).

Figure 4(a) shows the behavior of the SCR with respect to the increasing power law exponent \( \alpha \) when the anisotropic factor \( \zeta = 1 \), which actually makes the turbulence isotropic. Power law exponent \( \alpha \) is related to altitude of the propagation path of optical waves [34]. It is clear that the height will influence the atmosphere condition and the curves change when the atmosphere changes. The SCRs decrease sheer when \( \alpha \) varies from 3 to 3.2 and increase gently when \( \alpha \) varies from 3.3 to 3.8 and finally decrease sheer afterwards as \( \alpha \) goes to 4. On the other hand, Figure 4(b) shows the behavior of the SCR with respect to the turbulence strength \( \sim \sigma^2_R \). The SCRs also monotonically decrease as the turbulence strength increases. It is notable that the strengths of SCRs for two optical waves become almost the same when the turbulence strength gets moderate to strong, i.e., \( \sim \sigma^2_R > 1 \). The physical
reason for this phenomenon is that the strong turbulence will weaken the optical wave signals; thus, the SCR will reduce when the turbulence strength increases. Moreover, as in the simulations using the SCRs, the magnitudes of the plane waves are always smaller than those of the spherical waves.

Figure 5 shows the behavior of the SCR with respect to the increasing turbulence strength $\tilde{\sigma}_R^2$ and the increasing anisotropic factor $\zeta$. Figure 5(a) is for the plane waves, and Figure 5(b) is for the spherical waves. On the contrary to the WSF cases, the SCRs decrease as the turbulence strength gets stronger. Also, it is important to note that the SCRs are
also significantly influenced by the anisotropic factor $\zeta$ that 
the strength of the SCRs gets as much as 40 times stronger 
as the anisotropy increases from 1 to 50. The physical reason 
for this can be found in the anisotropic property of eddies; 
the eddies work as lenses with a larger radius of curvature 
in anisotropic turbulence than in isotropic turbulence, and 
the larger curvature lenses can focus an optical wave better 
than in isotropic turbulence [35].

Finally, Figure 6 shows the behavior of the SCR with 
respect to the inner scale of the eddy size $l_0$. In these simulations, 
we have set that the anisotropic factor $\zeta = 1$ and the 
power law exponent $\alpha$ equals to 3.2, 10/3, and 3.8, respectively. 
The simulation results show that the SRCs for both 
of the optical waves are significantly influenced by the inner 
scale of the eddy size; the curves increase monotonically as $l_0$ increases. Moreover, the plane waves are more affected by 
the power exponent factor $\alpha$ at the fixed inner scale of the 
eddy size; its magnitude increases as much as 50 percent as 
varies from 3.2 to 3.8. As the SCR gets smaller, it means 
the receiver needs more work to equalize the channel 
distortion.

7. Conclusion

In this work, we have presented new sets of expressions 
for the wave structure functions and also for the spatial 
coherence radiiuses of the free-space optical waves such 
as the plane waves and the spherical waves propagating 
in a horizontal path of a free space, which is disturbed 
by anisotropic turbulence. Those newly derived analytic 
expressions of WSFs and SCRs are evaluated, and their 
behaviors are observed by varying five major characteriz-
ing parameters, which are the power law exponent $\alpha$, the 
turbulence strength $\sigma_u^2$, the anisotropic factor $\zeta$, and the 
inner scale and the outer scale of the eddy size, $l_0$ and $L_0$, respectively.

Those five parameters individually or in their combina-
tions have extensive impacts on the magnitudes of the WSFs 
and SCRs. The behaviors of the WSFs and the SCRs come 
out differently with respect to the power law exponent. Also, 
with respect to the increasing turbulence strength, the WSFs 
and SCRs show an inverse relation that the WSFs increase 
while the SCRs decrease. Similarly, the anisotropic factor 
affects the WSFs and the SCRs inversely. In other words, 
the WSFs increase as the anisotropy increases while the 
SCRs decrease on the contrary. Finally, the scales of the eddy 
size gently affect the WSFs and the SCRs that both of them 
monotonically increase as the scales of the eddy sizes 
increase regardless of the inner scale or the outer scale. 
Particularly, for the SCRs, the plane waves are more signifi-
cantly affected by the turbulence power than the spherical 
waves. Moreover, the bigger power law exponents shrink 
the size of SCRs more than those of the smaller ones; the 
plane waves are also more affected than the spherical waves 
in this case as well.

We have also found that the wave structure function can 
be used to analyze the temporal frequency spreads of optical 
waves and MTF of an imaging system. In the optical com-
unication system, in order to recognize the target effec-
tively, it is necessary to evaluate the micro-Doppler shift 
caused by the background noise. This kind of noise also 
includes the wave caused by optical wave propagation in tur-
bulent atmosphere. These random changes cause frequency 
spread in the spectrum of laser signal, which is manifested 
as additional Doppler frequency shift. In addition, the signif-
ificant frequency spread can eliminate the micro-Doppler 
shift caused by the target. Therefore, the temporal frequency 
spread of optical waves can be used in lidar system, optical 
detection, ranging system, and other target detection and 
recognition fields. In conjunction with the current work pre-
sented in this paper, we are also looking at the effects of 
short-exposure MTFs on imaging systems of optical waves 
propagating in a free space with anisotropic maritime tur-
bulence; the propagation paths can be slant and horizontal. 
Our results have important theoretical and practical signifi-
cance for optical communication and imaging and sensing 
systems involving turbulent atmospheric channels on 6G 
communication. Also, our research has some limitations; 
the work is mainly based on the power-law spectrum derived 
from the mathematical formula and no outdoor experi-
ments. In future work, we will try to compare the results 
with the measured data from the outdoor experiment, 
because the outdoor results can better represent the actual 
atmospheric conditions.

Data Availability

The data used to support the findings of this study are avail-
able from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest.

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