

Research Article Sum-Throughput Maximization in Backscatter Communication-Based Cognitive Networks

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In this paper, we consider a backscatter communication (BackCom) based cognitive network that consists of one primary transmitter, one primary receiver, multiple secondary transmitters (STs), and one secondary receiver (SR). Each ST operates in the BackCom or energy harvesting model. Our goal is to jointly optimize the energy harvesting and backscatter time, the transmit power of the primary transmitter, and the power reflection coefficient of each ST to maximize the sum throughput of all the STs under a nonlinear energy harvesting model while satisfying multiple constraints, i.e., the energy causality of each ST, the Quality of Service of the primary transmitter, etc. The formulated problem is nonconvex due to the coupled variables and hard to solve. In order to address this problem, we decouple partial coupled variables by using the properties of the objective function and constructing auxiliary variables, and the remaining coupled variables are decoupled via successive convex approximation (SCA). On this basis, a SCA based iterative algorithm is developed to solve the formulated problem. Simulation results are provided to support our work.

1. Introduction

Internet of Things (IoT) is expected to deploy massive smart sensor nodes in the future communications to seamlessly connect the physical environment and the cyberspace for providing intelligent services [1]. However, such an approach requires huge spectrum resources, and this motivates us to consider high spectrum-efficient communication paradigms for IoT. In this context, cognitive radio has been proposed, whose key idea is to allow sensor nodes sharing spectrum with primary uses without causing any harmful factors to the primary transmission [2]. In cognitive radio, the smart sensor node (also called secondary user) transmits its own information by active radios that need the powerconsuming components and consume a lot of energy, greatly shortening their lifespan and leading to an energy-constrained problem for smart sensor nodes.

In addition to the cognitive radio that improves the spectrum efficiency, backscatter communication (BackCom) is another key technology, and its main purpose is to overcome the energy-constrained problem [3–5]. BackCom allows a smart sensor node modulating its information on the incident signals and backscattering the modulated signals to its associated receiver by changing the power reflection coefficient so that the power-consuming components can be avoided, while harvesting energy from the incident signal for realizing energy self-sustainability [3-5]. Despite these superiorities, the communication performance of BackCom is limited as it uses the ambient signals as the incident signals, and the ambient signals introduce serious cochannel interference to the BackCom receiver [4]. Accordingly, researchers proposed to use the controllable signals as the incident signals, but such an approach requires an extra cost to deploy RF sources. Recall that cognitive radio is able to provide controllable signals for the BackCom transmitter (also referred to as the secondary transmitter (ST) in this paper). Recent works have integrated BackCom into cognitive radio, yielding a spectrum- and energy-efficiency paradigm, called BackCom based cognitive networks.

In [6], the authors formulated a problem to maximize the throughput of a BackCom link in a BackCom based cognitive network with a single ST by jointly optimizing the transmit

power of the primary user and the power reflection coefficient of the ST. In [7], the authors proposed to maximize the energy efficiency of the secondary link by jointly optimizing the transmit power of the primary transmitter (PT), the power reflection coefficient of the ST, and the time for energy harvesting and BackCom. Extending the single ST scenario [6, 7] into multiple STs [8], the authors maximized the sum rate of STs by jointly optimizing the PT's transmit power and the power reflection coefficient of each ST. The authors of [9] considered a full-duplex-enabled BackCom based cognitive network and proposed a joint time, transmit power, and power reflection coefficient scheduling to maximize the throughput of the BackCom system. In addition to the above works, the harvest-then-transmit (HTT) protocol has also been integrated into BackCom based cognitive networks, and various resource allocation schemes have been studied [10–12], where the main focus is to balance the time for energy harvesting, HTT, and backscattering.

After carefully examining the existing resource allocation schemes, we note that all of them were based on a linear energy harvesting model. As pointed out by existing works, the linear energy harvesting model does not match the behavior of a practical energy harvester. More specifically, the harvest power is a nonlinear function with respect to the input power. The previous works [13-15] (in which Back-Com based cognitive network has not been considered) have proved that the mismatch of energy harvesting models will lead to performance degradation. Accordingly, it is necessary to design resource allocation for BackCom based cognitive networks with nonlinear energy harvesting model. Motivated by this, in this paper, we consider a BackCom based cognitive network with multiple STs and aim to maximize the total throughput of STs by jointly optimizing the energy harvesting time, BackCom time, power reflection coefficient, and PT's transmit power under a nonlinear energy harvesting model. Meanwhile, the energy-causality constraint of each ST and the Quality of Service (QoS) of both the primary link and the secondary links are considered. The main contributions of this paper are summarized as below.

We formulate an optimization problem to maximize the sum throughput of STs, and propose an efficient iterative algorithm to solve the problem. Since the formulated problem is nonconvex, the main challenge is how to transform the original problem into a convex one. Towards this end, we firstly determine the optimal transmit power of the PT by using the properties of the objective function, then introduce some auxiliary variables to decouple coupled variables, and lastly employ the successive convex approximation (SCA) to transform a nonconvex constraint into a linear one. We also provide computer simulation results to verify the proposed iterative algorithm and show the advantages of the proposed scheme over the baseline schemes.

2. System Model and Working Flow

As shown in Figure 1, we consider a BackCom based cognitive network, which consists of one PT, one PR, *K* energy-constrained STs, and one SR. In this network, the PT



FIGURE 1: BackCom based cognitive network and its frame structure.

transmits its own information to the PR, while the RF signals transmitted by the PT can also be exploited by the K STs for energy harvesting (EH) and information transmission. Assume that all the devices are equipped with a single antenna and work in the half-duplex mode. Suppose that each ST is equipped with both the EH circuit and the BackCom circuit so that it can harvest energy from the received RF signals and backscatter the received signals for information transmission. In order to prolong the operation time of each energy-constrained ST, we assume that each ST only uses its harvested energy instead of the energy early stored in its battery to cover the energy consumption during information backscattering. All channels including the PT-PR link and the ST-SR links are assumed to follow quasi-static fading. In the beginning of each transmission block, the channel state information (CSI) of all links can be perfectly achieved by the PT via the existing advanced channel estimation methods, so that the PT can determine the optimal resource allocation scheme based on the obtained CSI and feed the optimal scheme back to all the STs.

Let T denote the duration of the whole transmission block. For the PT-PR link, the PT may transmit its signals in the whole transmission block. For the ST-SR links, the whole transmission can be divided into two phases, which are the EH phase and the BackCom phase, respectively. In the EH phase, the PT broadcasts its signals to the PR while all the STs will perform EH. In the BackCom phase, the PT keeps broadcasting while all the STs take turns to perform BackCom in order to avoid the cochannel interference among STs.

2.1. EH Phase. Let t_e denote the duration of the EH phase. Denote P_t as the transmit power of the PT. Then, the received signal at the *k*-th ($k \in \mathcal{K} = \{1, 2, ..., K\}$) ST is given by

$$y_{\rm ST}^k = \sqrt{P_{\rm t} h_k} x_p + N_{\rm ST},\tag{1}$$

where h_k denotes the channel gain of the PT-*k*-th ST link, x_p with $\mathbb{E}[|x_p|^2] = 1$ is the information transmitted by the PT to the PR, and N_{ST} is the thermal noise at the *k*-th ST. Since the backscatter communication circuit consists only of passive components and takes few signal processing operations, the thermal noise is usually very small and can be ignored, i.e., $N_{ST=0}$ [7].

For EH, we consider a more practical nonlinear EH model since the linear EH model cannot characterize the nonlinearity of the practical EH circuit [16]. The reasons of considering the above nonlinear EH model instead of the one considered in [17, 18] are as follows. Firstly, the nonlinear EH model proposed in [16] is accurate enough for characterizing the nonlinearity of practical EH circuits. Secondly, the use of the nonlinear EH model proposed in [16] can simplify the difficulty and reduce the complexity of solving the formulated optimization problem. Accordingly, we compute the harvested energy of the k-th as

$$E_{\rm e}^{k} = t_{\rm e} \left(\frac{a_k P_{\rm t} h_k + d_k}{P_{\rm t} h_k + v_k} - \frac{d_k}{v_k} \right), \tag{2}$$

where a_k , d_k , and v_k are the parameters of the nonlinear EH model.

For the PT-PR link, the received signal at the PR is expressed as

$$y_{\rm PR}^e = \sqrt{P_{\rm t} f_p} x_p + N_{\rm PR},\tag{3}$$

where f_p denotes the channel gain of the PT-PR link and $N_{\rm PR}$ is the additive white Gaussian noise (AWGN) at the PR with mean zero and variance σ^2 . Accordingly, the achievable throughput at the PR in this phase can be computed as

$$R_{\rm e}^p = t_{\rm e} B \, \log_2 \left(1 + \frac{P_{\rm t} f_p}{\sigma^2} \right),\tag{4}$$

where B is the system bandwidth.

2.2. BackCom Phase. The whole BackCom phase can be divided into K subphases. In each subphase, each ST performs BackCom to transmitted information. Let t_k denote the duration of the k-th subphase. Denote α_k with $0 \le \alpha_k \le 1$ as the power reflection coefficient of the k-th ST based on which the received RF signal at the k-th ST can be split into two parts: one part is used for BackCom and the other part is flowed into the EH circuit. Then, in the subphase t_k , the received signal at the SR is given by

$$y_{\rm SR}^k = \sqrt{\alpha_k P_{\rm t} h_k g_k} x_p x_{s,k} + \sqrt{P_{\rm t} f_s} x_p + N_{\rm SR}, \qquad (5)$$

where g_k denotes the channel gain between the *k*-th ST and the SR, f_s is the channel gain of the PT-SR link, $x_{s,k}$ with $\mathbb{E}[|x_{s,k}|^2] = 1$ is the transmitted information of the *k*-th ST, and N_{SR} is the AWGN at the SR with mean zero and variance σ^2 .

From (5), it can be observed that the cochannel interference from the PT-SR link always exists, which degrades the throughput achieved by the *k*-th ST via BackCom. In order to decode the transmitted information of the *k*-th ST correctly, the SR performs the successive interference cancellation (SIC) technology. Specifically, the SR first decodes the PT's transmitted information x_p by treating $\sqrt{\alpha_k P_t h_k g_k} x_p x_{s,k}$ as the cochannel interference and then uses the SIC technology to cancel the interference from the PT as well as decoding the transmitted information of the *k*-th ST $x_{s,k}$. Therefore, the signal to interference plus noise ratio (SINR) at the SR for decoding x_p is given by

$$\gamma_{s,k}^{p} = \frac{P_{t}f_{s}}{\alpha_{k}P_{t}h_{k}g_{k} + \sigma^{2}}.$$
(6)

After using SIC technology, the signal to noise ratio (SNR) at the SR for decoding $x_{s,k}$ is expressed as

$$\gamma_{s,k} = \frac{\alpha_k P_t h_k g_k}{\eta P_t f_s + \sigma^2},\tag{7}$$

where η with $0 \le \eta \le 1$ is the interference cancellation factor.

Accordingly, the achievable throughput of the k-th ST-SR link can be computed as

$$R_{s,k} = t_k B \log_2(1 + \xi \gamma_{s,k}), \tag{8}$$

where ξ expresses the performance gap reflecting the real modulation [19–21]. In this subphase, the harvested energy of the *k*-th ST is determined by

$$E_{k}^{b} = t_{k} \left(\frac{a_{k} (1 - \alpha_{k}) P_{t} h_{k} + d_{k}}{(1 - \alpha_{k}) P_{t} h_{k} + v_{k}} - \frac{d_{k}}{v_{k}} \right).$$
(9)

At the end of the BackCom phase, the total harvested energy of the k-th ST is given by

$$E_{\text{tot}}^{k} = E_{k}^{b} + \left(t_{e} + \sum_{i=1}^{K} t_{i} - t_{k}\right) \left(\frac{a_{k}P_{t}h_{k} + d_{k}}{P_{t}h_{k} + \nu_{k}} - \frac{d_{k}}{\nu_{k}}\right).$$
(10)

For the PT-PR link, it also suffers from the cochannel interference from the k-th ST, and the received signal at the PR is given by

$$y_{\rm PR}^k = \sqrt{P_{\rm t}f_p} x_p + \sqrt{\alpha_k P_{\rm t}h_k f_k} x_p x_{s,k} + N_{\rm PR}, \qquad (11)$$

where f_k denotes the channel gain from the *k*-th ST to the PR. Then, the SINR at the PR for decoding x_p is computed as

$$\gamma_k^p = \frac{P_{\rm t} f_p}{\alpha_k P_{\rm t} h_k f_k + \sigma^2}.$$
 (12)

Correspondingly, the achievable throughput of the PT-PR link in this subphase is given by $R_k^p = t_k B \log_2(1 + \gamma_k^p)$.

3. Throughput Maximization for BackCom-Based Cognitive Networks

In this section, we design an optimal resource allocation scheme to maximize the total throughput of all the STs for the BackCom based cognitive network. In particular, we formulate a throughput maximization problem by jointly optimizing the transmit power of the PT, BackCom time, and power reflection coefficients of STs, as well as the EH time, subject to QoS, energy causality, latency, transmit power, and power reflection coefficient constraints, and then use the existing convex tools to solve it.

3.1. *Problem Formulation*. Before formulating the throughput maximization problem, we should determine the optimization objective and constraints.

3.1.1. Optimization Objective. The optimization objective is to maximize the total throughput of the STs which can be computed as

$$R_{\text{tot}}^{s} = \sum_{k=1}^{K} R_{s,k} = \sum_{k=1}^{K} t_{k} B \log_{2} \left(1 + \frac{\xi \alpha_{k} P_{t} h_{k} g_{k}}{\eta P_{t} f_{s} + \sigma^{2}} \right).$$
(13)

3.1.2. QoS Constraints. There are two QoS constraints to constrain the throughput of the PT and each ST, respectively. For the QoS constraint of each ST, we should guarantee that the achievable throughput of each ST is not less than its minimum required throughput. Let $C_{\min,k}$ denote the minimum required throughput of the *k*-th ST. Then, the QoS constraint of the *k*-th ST can be expressed as

$$R_{s,k} \ge C_{\min,k}, \quad \forall k,$$

$$\longleftrightarrow t_k B \log_2 \left(1 + \frac{\xi \alpha_k P_t h_k g_k}{\eta P_t f_s + \sigma^2} \right) \ge C_{\min,k}, \quad \forall k.$$
(14)

For the QoS constraint of the PT, the total achievable throughput of the PT should not be less than the PT's minimum required throughput, denoted by C_{\min} . Therefore, the QoS constraint of the PT can be expressed as

$$R_e^p + \sum_{k=1}^K R_k^p = t_e B \log_2 \left(1 + \frac{P_t f_p}{\sigma^2} \right)$$
$$+ \sum_{k=1}^K t_k B \log_2 \left(1 + \frac{P_t f_p}{\alpha_k P_t h_k f_k + \sigma^2} \right) \ge C_{\min}.$$
(15)

3.1.3. Energy-Causality Constraint. The energy-causality constraint states that the energy consumption of each ST should not be larger than its harvested energy during the

whole transmission block. Note that a rechargeable battery is equipped in each ST and that each ST may first use the energy stored in its battery to support BackCom and then use the harvested energy to power the battery. The energy-causality constraint ensures that the energy early stored in the battery is not reduced. Here, we consider fixed power consumption for BackCom by following [19–21]. Let $P_{b,k}$ denote the power consumption for the *k*-th ST when performing BackCom. Therefore, the energy-causality constraint for the *k*-th ST is given by

$$P_{b,k}t_k \leq E_{tot}^{\kappa} = t_k f_k \left((1 - \alpha_k) P_t h_k \right) + \left(t_e + \sum_{i=1}^{K} t_i - t_k \right) f_k \left(P_t h_k \right), \quad \forall k,$$

$$(16)$$

where $f_k(x) = (a_k x + d_k/x + v_k) - (d_k/v_k)$. Please note that the power consumption for the EH circuit has been included in the EH model and thus has not been considered in (16).

3.1.4. Transmit Power Constraint. Let P_{max} denote the maximum allowed transmit power of the PT. Then, the PT's transmit power constraint can be expressed as

$$0 \le P_{t} \le P_{\max}.$$
(17)

Based on (13), (14), (15), (16), and (17), the throughput maximization problem can be formulated as

$$P_{1}: \max_{P_{t},t_{e},\{t_{k}\}_{k=1}^{K},\{\alpha_{k}\}_{k=1}^{K}} R_{tot}^{*},$$

s.t. C1: (14), (15),
C2: (16),
C3: (17),
C4: $(\gamma_{s,k}^{P} \ge \gamma_{th}, \forall k),$
C5: $t_{e} + \sum_{k=1}^{K} t_{k} \le T, t_{e}, t_{k} \ge 0, \forall k,$
C6: $0 \le \alpha_{k} \le, \forall k,$

where C1 denotes the QoS constraints for each ST and the PT, C2 is the energy-causality constraint for each ST, C3 constrains the maximum transmit power of the PT, C4 ensures that each ST can decode x_p successfully and γ_{th} is the threshold required for decoding x_p , C5 is the latency constraint, and C6 is the constraint for the power reflection coefficient of each ST.

It can be observed that \mathbf{P}_1 is a highly nonconvex optimization problem and is difficult to solve due to the following reasons. Firstly, there exist several coupled relationships between multiple optimization variables, i.e., P_t , t_k , α_k , etc., leading to the nonconvex objective function and constraints, i.e., C1, C2, etc. Secondly, the cochannel interference causes the difference of convex (DC) structures in the objective function and C1, bringing new challenges to solving \mathbf{P}_1 . Thirdly, the consideration of the nonlinear EH model is another difficulty for solving \mathbf{P}_1 since the nonlinear EH model makes C1 more complex. Therefore, it is hard to solve \mathbf{P}_1 . 3.2. Solution. In order to remove DC structures existing in the objective function and C1 and simplify P_1 , the following lemma is introduced to determine the optimal transmit power of the PT.

Lemma 1. The maximum throughput of all the STs for the considered network is achieved when the PT transmits its signals with its maximum transmit power, i.e., $P_t^* = P_{max}$.

Proof. Please see Appendix A.

By substituting $P_t = P_{max}$ into \mathbf{P}_1 , \mathbf{P}_1 can be reformulated as

$$P_{2}: \max_{t_{e},\{t_{k}\}_{k=1}^{K},\{\alpha_{k}\}_{k=1}^{K}}\sum_{k=1}^{K}t_{k}B\log_{2}\left(1+\frac{\zeta\alpha kP_{\max}h_{k}g_{k}}{\eta P_{\max}f_{s}+\sigma^{2}}\right),$$

$$s.t. C1': t_{k}B\log_{2}\left(1+\frac{\zeta\alpha kP_{\max}h_{k}g_{k}}{\eta P_{\max}f_{s}+\sigma^{2}}\right) \ge C_{\min,k}, \forall k,$$

$$\sum_{k=1}^{K}t_{k}B\log_{2}\left(1+\frac{P_{\max}f_{p}}{\alpha_{k}P_{\max}h_{k}f_{k}+\sigma^{2}}\right)+t_{e}B\log_{2}\left(1+\frac{P_{\max}f_{p}}{\sigma^{2}}\right) \ge C_{\min},$$

$$C2': P_{b,k}t_{k} \le \left(t_{e}+\sum_{i=1}^{K}t_{i}-t_{k}\right)f_{k}(P_{\max}h_{k})+t_{k}f_{k}((1-\alpha_{k})P_{\max}h_{k}), \forall k,$$

$$C5, C7: 0 \le \alpha_{k} \le \min\left(\frac{P_{\max}f_{s}-\gamma_{th}\sigma^{2}}{P_{\max}h_{k}g_{k}\gamma_{th}},1\right), \forall k,$$

$$(19)$$

where C7 is the combination of C4 and C6.

 \mathbf{P}_2 is still nonconvex since the coupled relationships between different variables, e.g., α_k and t_k , still exist in the objective function and several constraints. To address this issue, we introduce the following auxiliary variables: $z_k = \alpha_k t_k, \forall k$, to replace the variables $\alpha_k, \forall k$, and rewrite \mathbf{P}_2 as

$$P_{2}: \max_{t_{e},\{t_{k}\}_{k=1}^{K},\{z_{k}\}_{k=1}^{K}}\sum_{k=1}^{K}t_{k}B\log_{2}\left(1+\frac{\zeta z_{k}P_{\max}h_{k}g_{k}}{t_{k}(\eta P_{\max}f_{s}+\sigma^{2})}\right),$$

$$s.t. C1'': t_{k}B\log_{2}\left(1+\frac{\zeta z_{k}P_{\max}h_{k}g_{k}}{t_{k}(\eta P_{\max}f_{s}+\sigma^{2})}\right) \ge C_{\min,k}, \forall k,$$

$$\sum_{k=1}^{K}t_{k}B\log_{2}\left(1+\frac{P_{\max}f_{p}}{z_{k}P_{\max}h_{k}f_{k}+\sigma^{2}}\right)+t_{e}B\log_{2}\left(1+\frac{P_{\max}f_{p}}{\sigma^{2}}\right) \ge C_{\min},$$

$$C2'': P_{b,k}t_{k} \le t_{k}f_{k}\left(\frac{(t_{k}-z_{k})P_{\max}h_{k}}{t_{k}}\right)\left(t_{e}+\sum_{i=1}^{K}t_{i}-t_{k}\right)f_{k}(P_{\max}h_{k}), \forall k,$$

$$C5, C7': 0 \le z_{k} \le t_{k} \times \min\left(\frac{P_{\max}f_{s}-\gamma_{th}\sigma^{2}}{P_{\max}h_{k}g_{k}\gamma_{th}}, 1\right),$$

$$(20)$$

Proposition 1. In P_3 , the objective function and all the constraints except C1'' are convex.

Proof. Please see Appendix B.

where $\alpha_k = (z_k/t_k), \forall k$.

In order to handle the nonconvex constraint C1^{''} and solve \mathbf{P}_3 , the SCA method is used, where the first-order Taylor expression is used to approximate the function $t_k B \log_2 (1 + (t_k P_{\max} f_p / z_k P_{\max} h_k f_k + \sigma^2 t_k))$ in C1^{''} and turn this nonconvex function into a linear function. Specifically, let $F_k(\alpha_k) = t_k B \log_2(1 + (P_{\max}f_p/\alpha_k P_{\max}h_k f_k + \sigma^2))$. By taking the first-order derivative of $F_k(\alpha_k)$ with respect to α_k , we have

$$\frac{\partial F_k(\alpha_k)}{\partial \alpha_k} = \frac{-P_{\max^2} f_p h_k f_k B t_k}{\left(\alpha_k P_{\max} h_k f_k + \sigma^2 + P_{\max} f_p\right) \left(\alpha_k P_{\max} h_k f_k + \sigma^2\right) In2}.$$
(21)

Using the first-order Taylor expression, $F_k(\alpha_k)$ can be approximated as

$$F_{k}(\alpha_{k}) \approx \frac{\partial F_{k}(\alpha_{k}^{0})}{\partial \alpha_{k}^{0}} (\alpha_{k} - \alpha_{k}^{0}) + F_{k}(\alpha_{k}^{0}) = \frac{-P_{\max^{2}}f_{p}h_{k}f_{k}Bt_{k}(\alpha_{k} - \alpha_{k}^{0})}{(\alpha_{k}^{0}P_{\max}h_{k}f_{k} + \sigma^{2} + P_{\max}f_{p})(\alpha_{k}^{0}P_{\max}h_{k}f_{k} + \sigma^{2})In2} + F_{k}(\alpha_{k}^{0}),$$

$$= \frac{-P_{\max^{2}}f_{p}h_{k}f_{k}B(z_{k} - \alpha_{k}^{0}t_{k})}{(\alpha_{k}^{0}P_{\max}h_{k}f_{k} + \sigma^{2} + P_{\max}f_{p})(\alpha_{k}^{0}P_{\max}h_{k}f_{k} + \sigma^{2})In2} + F_{k}(\alpha_{k}^{0}),$$
(22)

where α_k^0 is the given value for α_k and can be updated iteration by iteration.

By substituting (22) into C1^{''}, the QoS constraint for the PT's transmission can be rewritten as

$$\sum_{k=1}^{K} \left(\frac{-P_{\max^{2}} f_{p} h_{k} f_{k} B(z_{k} - \alpha_{k}^{0} t_{k})}{(\alpha_{k}^{0} P_{\max} h_{k} f_{k} + \sigma^{2} + P_{\max} f_{p})(\alpha_{k}^{0} P_{\max} h_{k} f_{k} + \sigma^{2}) \ln 2} + F_{k}(\alpha_{k}^{0}) \right) + t_{e} B \log_{2} \left(1 + \frac{P_{\max} f_{p}}{\sigma^{2}} \right) \ge C_{\min}.$$
(23)

Accordingly, \mathbf{P}_3 can be transformed into the following subproblem, given by

$$P_{4}: \max_{t_{e},\{t_{k}\}_{k=1}^{K},\{z_{k}\}_{k=1}^{K}} \sum_{k=1}^{K} t_{k} B \log_{2} \left(1 + \frac{\zeta z_{k} P_{\max} h_{k} g_{k}}{t_{k} (\eta P_{\max} f_{s} + \sigma^{2})} \right),$$

$$s.t. C1''': t_{k} B \log_{2} \left(1 + \frac{\zeta z_{k} P_{\max} h_{k} g_{k}}{t_{k} (\eta P_{\max} f_{s} + \sigma^{2})} \right) \ge C_{\min,k}, \forall k,$$

$$\sum_{k=1}^{K} t_{k} B \log_{2} \left(1 + \frac{-P_{\max}^{2} f_{p} h_{k} f_{k} B (z_{k} - \alpha_{k}^{0} t_{k})}{(\alpha_{k}^{0} P_{\max} h_{k} f_{k} + \sigma^{2} + P_{\max} f_{p}) (\alpha_{k}^{0} P_{\max} h_{k} f_{k} + \sigma^{2})} + F_{k} (\alpha_{k}^{0}) \right) + t_{e} B \log_{2} \left(1 + \frac{P_{\max} f_{p}}{\sigma^{2}} \right) \ge C_{\min},$$

$$C2''', C5, C7'.$$

$$(24)$$

Proposition 2. P_4 is proved to be convex, which can be efficiently solved by using the existing convex optimization tools.

Proposition 1, \mathbf{P}_4 can be proved to be convex and can be efficiently solved by using the existing convex optimization tools.

Proof. After using the first-order Taylor expression, the nonconvex QoS constraint for the PT's transmission in C1''' can be turned into a linear constraint. Combining with

(1) Set the maximum tolerance ε and the maximum number of iterations I_{max} ; (2)Set the iteration index i = 1 and the initial given values $\alpha_k^0, \forall k$; Based on Lemma 1, the optimal transmit power of the PT P_t^* is set as P_{max} ; (3) (4)repeat (5)Solve the optimization problem \mathbf{P}_4 with given $\alpha_k^0, \forall k$, to obtain the optimal solutions, denoted by $t_e^*, \{t_k^*\}_{k=1}^K, \{z_k^*\}_{k=1}^K$ (6)Compute α_k^* as $(z_k^*/t_k^*), \forall k$; Compute the value of R_{tot}^s based on (13); (7)if $|\alpha_k^* - \alpha_k^0| \le \varepsilon$ then (8)Set Flag = 1; (9)(10)else Set Flag = 0 and i = i + 1; (11)Update α_k^0 as $\alpha_k^0 = \alpha_k^*, \forall k$; (12)(13) end if (14) until Flag = 1 or $i = I_{max}$. (15) Output $P_t^*, t_e^*, \{t_k^*\}_{k=1}^K, \{\alpha_k^*\}_{k=1}^K$ and R_{tot}^s .

ALGORITHM 1: SCA based iterative algorithm.

3.3. Design of a SCA Based Iterative Algorithm. In this subsection, we propose a SCA based iterative algorithm to solve P_3 efficiently. The detailed process of the proposed algorithm is shown in Algorithm 1.

As shown in Algorithm 1, in each iteration, we should use the existing convex tools, i.e., CVX, to optimally solve the subproblem \mathbf{P}_4 with given $\alpha_k^0, \forall k$. Then the optimal solutions to \mathbf{P}_4 are obtained, denoted by $t_e^*, \{t_k^*\}_{k=1}^K, \{\alpha_k^*\}_{k=1}^K$, where α_k^* is computed as $(z_k^*/t_k^*), \forall k$. If the stop condition, namely, $|\alpha_k^* - \alpha_k^0| \le \varepsilon$ with the maximum tolerance ε , is satisfied, then the solution to \mathbf{P}_3 is $t_e^*, \{t_k^*\}_{k=1}^K, \{\alpha_k^*\}_{k=1}^K$. Otherwise, we should update the value of α_k^0 as α_k^* and repeat the above steps until the stop condition is satisfied.

4. Numerical Results

In this section, both the effectiveness and the superiority of the proposed algorithm are verified via computer simulations. The key simulation parameters, unless otherwise specified, are provided in Table 1. Following [16], the parameters of the considered nonlinear EH model at the k-th ST are set as $a_k = 2.463$, $d_k = 1.635$, and $v_k = 0.826$, $\forall k$. For the settings of all channels, we consider a standard channel fading model. Specifically, the channel gain of the PT-PR link is modeled by $f_p = f_p' D_p^{-\beta}$, where f_p' denotes the smallscale fading of the PT-PR link, D_p is the distance from the PT to the PR, and β denotes the path loss exponent. The channel gain of the PT-k-th ST link is given by $g_k = g'_k D_{1,k}^{-p}, \forall k$, where g'_k and $D_{1,k}$ are the small-scale fading and the distance from the PT to the k-th ST, respectively. The channel gain of the k-th ST-SR link is modeled by $h_k = h'_k D_{2,k}^{-p}, \forall k$, where h'_k and $D_{2,k}$ are the small-scale fading and the distance from the k-th ST to the SR, respectively. The channel gain of the k-th ST–PR link is $f_k = f'_k D_{3,k}^{-\beta}, \forall k$ with the small-scale fading f'_k and the distance $D_{3,k}$. The channel gain of the PT-SR link is modeled by $f_s = f'_s D_s^{-\beta}, \forall k$, with the small-scale fading f'_s and the distance D_s . In the simulations, we set $\beta = 2.7$, $D_p = 30$ m, $D_s = 30$ m, $D_{1,1} = 12$ m, $D_{1,2} = 10 \text{ m}, D_{1,3} = 15 \text{ m}, D_{1,4} = 13 \text{ m}, D_{2,1} = 20 \text{ m}, D_{2,2} =$

15 m, $D_{2,3} = 20$ m, $D_{2,4} = 15$ m, $D_{3,1} = 25$ m, $D_{3,2} = 30$ m, $D_{3,3} = 30$ m, and $D_{3,4} = 30$ m.

Figure 2 demonstrates the convergence of Algorithm 1, where different settings of $C_{s,\min}$ are considered and $C_{\min^1} = C_{\min^2} = C_{\min^3} = C_{\min^4} = C_{s,\min}$. We set $C_{s,\min}$ as 10 bits, 20 bits, and 30 bits. It can be observed that the proposed algorithm in Algorithm 1 can always converge to a certain value after only a few iterations, i.e., 3 iterations. This indicates that the proposed algorithm is convergent and computationally efficient. Besides, it can also be seen that a larger $C_{s,\min}$ brings a lower total throughput of all STs. This is because a larger $C_{s,\min}$ means a higher QoS requirement for the ST's transmission, and more resources will be allocated to the STs with worse channels, leading to a reduction in the total throughput of all STs.

Figure 3 plots the total throughput of all STs versus the minimum required throughput for each ST C_{s.min}, and $C_{s,\min}$ is varied from 5 bits to 30 bits. In order to illustrate the advantages of the proposed scheme, we compare the performance achieved by the proposed scheme with the fixed scheme, where the power reflection coefficient of each ST is fixed as 0.5, 0.8, and 0.9, respectively. As shown in this figure, the total throughput of all STs decreases with the increase of $C_{s,\min}$, since a larger $C_{s,\min}$ brings a higher QoS requirement for the ST's transmission, and more resources will be allocated to the STs with worse channels, leading to a reduction in the total throughput of all STs. By comparisons, we can see that the total throughput of all STs under the proposed scheme is higher than that under the fixed scheme, as the proposed scheme provides more flexibilities to utilize resources efficiently for maximizing the total throughput of all STs. This also demonstrates the superiority of the proposed scheme.

Figure 4 shows total throughput of all STs versus the minimum SINR threshold required for decoding x_p , γ_{th} , where γ_{th} ranges from 20 to 100. The power reflection coefficient of each SN under the fixed scheme is set as 0.5, 0.8, and 0.9. It can be observed from this figure that the total throughput of all STs decreases when γ_{th} increases. This is because a higher γ_{th} brings a higher requirement for

Parameter	Notation	Value
The entire time block	T	1 second
The communication bandwidth	В	100 kHz
The constant circuit power consumption for BackCom at the k-th ST	$P_{\mathrm{b},k}$	10μ W
The maximum transmit power at the PT	P_{\max}	1 W
The performance gap reflecting the real modulation for BackCom	ξ	-15 dB
The noise power	σ^2	-60 dBm
The number of STs	K	4
The minimum required throughput of the k-th ST	$C_{\min,k}$	10 bits
The minimum required throughput of the PT	C_{\min}	100 bits
The threshold required for decoding x_p	$\gamma_{ m th}$	20



FIGURE 2: The convergence of Algorithm 1 under different settings of $C_{s,\min}$, where $C_{\min^1} = C_{\min^2} = C_{\min^3} = C_{\min^4} = C_{s,\min}$.



FIGURE 3: Total throughput of all STs versus the minimum required throughput for each ST.



FIGURE 4: Total throughput of all STs versus the minimum SINR threshold required for decoding x_p .



FIGURE 5: Total throughput of all STs versus the maximum allowed transmit power at the PT.

decoding x_p , leading to a reduction in the total throughput of all STs. By comparisons, we can observe that the proposed scheme outperforms the other schemes in terms of the total throughput of all STs, which illustrates the advantages of the proposed scheme.

Figure 5 shows the total throughput of all STs versus the maximum allowed transmit power at the PT P_{max} under different schemes. Here, P_{max} varies from 1 W to 3 W. It can be observed that the total throughput of all STs under all the schemes increase with the increase of P_{max} . Based on Lemma 1, the optimal transmit power of the PT is determined by

 P_{max} , and a higher transmit power of the PT allows STs to harvest more energy for supporting the energy consumption of BackCom and to backscatter signals with a higher power, resulting in an improvement for the total throughput of all STs. Besides, we also observe that the total throughput of all STs under the proposed scheme is the highest among these schemes, which also demonstrates the superiority of the proposed scheme in terms of total throughput of all STs.

5. Conclusions

In this paper, we have studied the throughput maximization for the BackCom based cognitive network while considering a nonlinear EH model. Specifically, we have formulated an optimization problem to maximize the total throughput of all STs by jointly optimizing the EH time, the transmit power of the PT, the BackCom time, and the power reflection coefficient of each ST under the QoS, energy causality, latency, transmit power, and power reflection coefficient constraints. In order to solve the nonconvex problem, we first determined the optimal transmit power of the PT by using the properties of the objective function and then proposed a SCA based iterative algorithm to obtain the proposed scheme. The simulation results verified the quick convergence of the proposed algorithm and showed that the proposed scheme outperforms the other schemes in terms of total throughput of all STs.

Appendix

A. Proof of Lemma 1

Let $C_k(P_t) = t_k B \log_2(1 + (\xi \alpha_k P_t h_k g_k / \eta P_t f_s + \sigma^2))$ and $R_{\text{tot}}^s = \sum_{k=1}^{K} C_k(P_t)$. By taking the first-order derivative of R_{tot}^s with respect to P_t , we have

$$\frac{\partial R_{tot}^s}{\partial P_t} = \sum_{k=1}^{K} \frac{\partial C_k(P_t)}{\partial P_t} = \sum_{k=1}^{K} \frac{t_k B \xi \alpha_k h_k g_k \sigma^2}{\left(\eta P_t f_s + \sigma^2\right) \left(\eta P_t f_s + \sigma^2 + \xi \alpha_k h_k g_k P_t\right) In2}.$$
(A.1)

Since $(\partial R_{tot}^s/\partial P_t) > 0$ always holds, R_{tot}^s is a monotone increasing function with respect to P_t . That is to say, a larger P_t brings a larger R_{tot}^s . In order to maximize R_{tot}^s , the optimal transmit power of the PT, denoted by P_t^* , should equal the maximum within its feasible region.

By observing the constraints C1, C2, C3, and C4, we can find that the lower bound of P_t is determined by C1, C2, and C4 while the upper bound of P_t is always P_{max} . The reasons are as follows. As for C1, similar to R_{tot}^s , we can prove that the functions $C_k(P_t)$ and $\sum_{k=1}^{K} t_k B \log_2(1 + (P_t f_p / \alpha_k P_t h_k f_k + \sigma^2)) + t_e B \log_2(1 + (P_t f_p / \sigma^2))$ are monotone increasing functions with respect to P_t . The proof process is omitted here for brevity. Therefore, C1 determines a lower bound of P_t .

As for C2, since the harvested power of the EH circuit increases with the increase of the input power and then converges to the maximum value when the input power is large enough, $f_k(x)$ is a monotone increasing function with respect to x. That is, the right side of C2 is also a monotone increasing function with respect to P_t , and P_t determines another lower bound of P_t .

As for C4, based on (6), we can transform C4 as $P_t \ge (\gamma_{th}\sigma^2/f_s - \gamma_{th}\alpha_k h_k g_k)$, $\forall k$, which is also a lower bound of P_t .

Therefore, the upper bound of P_t is only determined by P_{max} , and the optimal transmit power of the PT is given by $P_t^* = P_{\text{max}}$. Then, the proof of Lemma 1 is complete.

B. Proof of Proposition 1

After carefully analyzing P_3 , it is not hard to conclude that both constraints C5 and C7' are linear constraints. Thus, P_3 is convex if and only if the objective function is a concave function and constraints C1'' and C2'' are convex.

For the objective function, using the fact that the perspective function can preserve convexity, we can find that the convexity of the function $t_k B \log_2(1 + (\xi z_k P_{\max} f_s + \sigma^2)))$ is the same as that of the function $\begin{array}{l} \log_2\left(1+\left(\xi z_k P_{\max} h_k g_k / \eta P_{\max} f_s + \sigma^2\right)\right). & \text{Since } \log_2\left(1+\left(\xi z_k P_{\max} h_k g_k / \eta P_{\max} f_s + \sigma^2\right)\right) \text{ is a concave function with respect to } z_k, \quad t_k B \log_2\left(1+\left(\xi z_k P_{\max} h_k g_k / t_k \left(\eta P_{\max} f_s + \sigma^2\right)\right)\right) \text{ is a concave function jointly with respect to } z_k \text{ and } t_k. \text{ Thus, the objective function is a concave function.} \end{array}$

For the QoS constraint for the ST's transmission in C1'', since $t_k B \log_2(1 + (\xi z_k P_{\max} h_k g_k / t_k (\eta P_{\max} f_s + \sigma^2)))$ is a concave function jointly with respect to z_k and t_k , the QoS constraint for the ST's transmission is convex. For the QoS constraint for the PT's transmission in C1'', $t_k B \log_2(1 + (t_k P_{\max} f_p / z_k P_{\max} h_k f_k + \sigma^2 t_k))$ is neither convex nor concave, leading to the nonconvex QoS constraint for the PT's transmission and the nonconvex constraint C1''.

For the constraint C2'', its convexity depends on the convexity of $t_k f_k ((t_k - z_k)P_{\max}h_k/t_k)$. Based on the perspective function, the convexity of $t_k f_k ((t_k - z_k)P_{\max}h_k/t_k)$ is the same as that of $f_k ((1 - z_k)P_{\max}h_k)$. By taking the first-order derivative of $f_k ((1 - z_k)P_{\max}h_k)$ with respect to $(1 - z_k)P_{\max}h_k$, we have

$$\frac{\partial f_k((1-z_k)P_{\max}h_k)}{\partial (1-z_k)P_{\max}h_k} = \frac{a_k v_k - d_k}{\left((1-z_k)P_{\max}h_k + v_k\right)^2}.$$
 (B.1)

Since the harvested power of the EH circuit increases with the input power, $(\partial f_k((1-z_k)P_{\max}h_k)/\partial(1-z_k)P_{\max}h_k)$ should be always larger than or equal to 0. Therefore, $a_kv_k - d_k \ge 0$ always holds. Then, we take the second-order derivative of $f_k((1-z_k)P_{\max}h_k)$ with respect to z_k ; we have

$$\frac{\partial^2 f_k ((1-z_k) P_{\max} h_k)}{\partial z_k^2} = \frac{-2 (P_{\max} h_k)^2 (a_k v_k - d_k)}{((1-z_k) P_{\max} h_k + v_k)^3}.$$
 (B.2)

According to $a_k v_k - d_k \ge 0$, we have $\partial^2 f_k((1 - z_k)P_{\max}h_k)/\partial z_k^2 \le 0$. Therefore, $f_k((1 - z_k)P_{\max}h_k)$ is a concave function with respect to z_k . Correspondingly, $t_k f_k(((t_k - z_k)P_{\max}h_k/t_k)))$ is also a concave function jointly with respect to z_k and t_k , and the constraint C2'' is convex.

Based on the above analysis, Proposition 1 is obtained, and the proof is complete.

Data Availability

The simulation data used to support the findings of this study are included within the article. The MATLAB code used to support the findings of this study is available from the corresponding author upon request.

Conflicts of Interest

The author declares that there are no conflicts of interest.

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